

**Bogolyubov Kyiv Conference
"Problems of Theoretical and
Mathematical Physics"**

Report of Contributions

Contribution ID: 1

Type: **Oral**

Milky Way globular clusters in cosmological timescale. Probability of the interaction with the Galactic center

Thursday, 26 September 2024 16:10 (20 minutes)

The main idea of the work is to carry out the dynamic evolution of the orbits of Globular Cluster (GC) subsystems sample lookback time up to 10 Gyr. This allows us to estimate the possibility of GCs interaction with the Galactic center that dynamically changed in the past. To reproduce the structure of the Galaxy in time, we used external potentials which dynamically changed in a past and now their characteristics are similar to the physical values of the Milky Way at the present day (mass and size of disk and halo). External potentials were selected from the large-scale cosmological database IllustrisTNG-100 (TNG-TVP). In these potentials, we reproduced the orbits of 147 GCs from Gaia DR3 in 10 Gyr lookback time using our own high-order N-body parallel dynamic code phi-GPU code. To identify clusters that have interaction with the Galactic center, we used the criteria of relative distance: it must be less than 100 pc. Applying this simple criteria, we obtained statistically significant rates of close passages of the GCs with the Galactic center. We identified ten GCs, including NGC 6401, Pal 6, NGC 6681, NGC 6712, NGC 6287, NGC 6642, NGC 6981, HP 1, NGC 1904, and NGC 362, with a high probability of close passages near the Galactic center in all four TNG-TVPs, particularly the first six with a probability of around 100%.

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Session Classification: Afternoon Session 3

Track Classification: ASTROPHYSICS AND COSMOLOGY

Contribution ID: 2

Type: **Oral**

Virial Expansions for Correlation Functions in Canonical Ensemble

The infinite set of coupled integral nonlinear equations for correlation functions in the case of classical canonical ensemble is considered.
Some kind of graph expansions of correlation functions in the density parameter are constructed.
Existing of unique solutions for small value of density and high temperature is discussed.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 3

Type: **Oral**

Dynamics of correlations of many colliding particles

Thursday, 26 September 2024 12:30 (20 minutes)

The talk provides an overview of some advances in the mathematical understanding of the nature of the dynamics of the correlations of many colliding particles. The fundamental equations of modern mathematical physics are studied, in particular the hierarchies of the evolution equations of many hard spheres and their asymptotic behavior described by kinetic nonlinear equations.

First, an approach to describing correlations in a system of colliding particles interacting as hard spheres is discussed, based on a hierarchy of equations for the evolution of a sequence of correlation functions that are cumulants of distribution functions, called the Liouville hierarchy. It is proven that the constructed dynamics of correlations underlie the description of the dynamics of both a finite and an infinite number of hard spheres obeying the BBGKY hierarchies for reduced (marginal) distribution functions or reduced correlation functions.

The structure of expansions representing non-perturbative solutions of the Cauchy problem for these hierarchies of evolution equations is formulated. It has been established that the concept of cumulants of the groups of operators of the Liouville equations underlies non-perturbative expansions of solutions to the hierarchies of fundamental equations describing the evolution of observables and of the state of many hard spheres, as well as forms the basis of the kinetic description of their collective behavior.

In the talk, we also consider a new approach to the problem of a rigorous description of kinetic evolution by means of reduced (marginal) observables governed by the dual BBGKY hierarchy. One of the advantages of the developed approach to the derivation of kinetic equations from the underlying dynamics of many particles is that it provides an opportunity to construct kinetic equations with initial correlations, in particular correlations characterizing the condensed states of a system, and to describe the processes of the propagation of initial correlations within suitable scaling limits.

References

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- [3] Gerasimenko V I and Gapyak I V 2021 Boltzmann–Grad asymptotic behavior of collisional dynamics. *Reviews in Math. Phys.* **33** 2130001 32 doi:10.1142/S0129055X21300016
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Session Classification: Morning Session 3

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 4

Type: **Lecture**

About the works of M. Bogolyubov at the Institute of Mathematics

About the works of M. Bogolyubov at the Institute of Mathematics.

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Presenter: GERASIMENKO, Viktor (Institute of mathematics NAS of Ukraine)

Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 7

Type: **Poster**

Supercritical propagation of nonlinear magnetization wave through an antiferromagnetic magnonic crystal

Tuesday, 24 September 2024 17:30 (5 minutes)

Analytical model of a nonlinear magnetization wave (MW) propagating through one-dimensional antiferromagnetic magnonic crystal comprised of two sorts of antiferromagnets (AFM) is proposed for supercritical mode when the MW velocity exceeds the critical velocity of MW in both antiferromagnets AFMs or at least in one of them. Both AFMs that comprise the magnonic crystal are assumed to be two-sublattice uniaxial ones. The Landau-Lifshitz equations have been used in the sigma model with account for the exchange bias between magnetic sublattices of both AFMs, the magnetic anisotropy, the magnetic dipole-dipole interaction and the Dzyaloshynskii-Moriya interaction. The boundary conditions for the Néel vector (with the exchange bias between magnetic sublattices of both AFMs taken into account) are applied on the interface between two AFMs. The discrete sets of frequencies and velocities for the considered MW are obtained. Analysis of the results shows that the nonlinear MW is reflection-less, phase-coherent and possesses a number of parameters that can be considered as degrees of freedom for encoding information. These findings open up new possibilities of digital data processing utilizing nonlinear MW propagating through antiferromagnetic magnonic crystal in supercritical mode.

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Session Classification: Poster Session

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 8

Type: Oral

Quantum topological effects in magnetization dynamics: the Berry phase, the Aharonov–Casher effect and electric field control of spin waves dynamics

Wednesday, 25 September 2024 10:40 (40 minutes)

Condensed matter physics is revolutionizing by introducing topology-based concepts that characterize a system's physical states and properties. An example of topological effects in magnetization dynamics is the additional quantum mechanical phase, the so-called Berry phase [1], and the Aharonov–Casher (AC) effect [2], acquired by the quantum orbital motion of chargeless bosonic quasiparticles with magnetic dipole moment – e.g., spin waves (SWs) with magnetic moment $\mu_m = \pm g\mu_B$ – in mesoscopic rings in an external electric (E) field. It manifests itself in a shift of the dispersion and the group velocity direction of SW by the E field. In the linear approximation concerning the electric field, the magnonic AC effect can be considered by adding the Dzyaloshinskii-Moriya-like interaction between neighboring spins. This topological quantum phenomenon has been directly detected experimentally for SWs propagating in the classical magnetic insulator Y₃Fe₅O₁₂ [3,4]. The magnitude of the AC phase was two orders larger than previously estimated theoretically for centrosymmetric ferromagnet insulators. This finding allows for tuning the properties of SWs, an essential ingredient for magnonic devices, by the E-field. Through analytical calculations and micromagnetic simulations, we demonstrated that in ferromagnetic, antiferromagnetic, and ferrimagnetic nanoscale films, it is possible to control the SWs characteristics using an external E-field [5-9]. From the fundamental point of view, the discussed quantum phenomena open a new avenue for quantifying topological effects in magnetization dynamics. The E-field control of SW dynamics in magnetic film can also be helpful for the development and designing of new magnonic nanodevices and could be utilized for quantum technologies.

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- [1] M. V. Berry. Quantum phase factors accompanying adiabatic changes. Proc. R. Soc. London, Ser. A 392, 45 (1984).
- [2] Y. Aharonov, A. Casher. Topological quantum effects for neutral particles. Phys. Rev. Lett. 53, 319 (1984).
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- [8] O. Boliasova, V. Krivoruchko. Electric-Field Control of Magnetization Dynamics in Antiferromagnets. 2023 IEEE Nanotechnology Materials and Devices Conference (NMDC), Paestum (Salerno), Italy; DOI:10.1109/NMDC57951.2023.10343910
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Session Classification: Morning Session 2

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 9

Type: **Oral**

Critical point in system of interacting bosons

Tuesday, 24 September 2024 10:20 (40 minutes)

A system of bosons studied within the mean field framework has two fascinating phenomena: a liquid-gas first order phase transition and Bose-Einstein condensation. Interplay between these two phenomena is being investigated. Depending on the mean-field potential parameters one can observe two types of critical points (CP), called "Boltzmann" and "Bose", that belong to different universality classes with distinct sets of critical exponents. As examples of Bose and Boltzmann CPs pion and α matter are considered, respectively. In general, the phase diagram can have one of the CPs or both of them.

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Session Classification: Morning session 1

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 10

Type: **Poster**

AdS/CFT correspondence and and classification of Kaluza-Klein modes within the supergroup

Tuesday, 24 September 2024 16:50 (5 minutes)

Within the framework of AdS/CFT correspondence we considered large N limits of conformal field theories in d dimensions which described in terms of supergravity on the product of AdS space with a compact manifold. An important example of such correspondence is equivalence between N = 4 super Yang-Mills theory in four dimensions and Type IIB superstring theory on $AdS_5 \times S^5$ [1]. The confirmation of this correspondence comes from the fact that the Kaluza-Klein modes of type IIB supergravity on $AdS_5 \times S^5$ coincide with the chiral operators of N = 4 super Yang-Mills theory in four dimensions. Moreover, to describe N = 4 super Yang-Mills theory in four dimensions, one should use low energy supergravity on AdS_5 and the infinite tower of massive Kaluza-Klein states on $AdS_5 \times S^5$ [2]. The supersymmetry group of $AdS_5 \times S^5$, is known to be the same as the superconformal group in 3+1 spacetime dimensions. So, the supersymmetries of Type IIB superstring theory on $AdS_5 \times S^5$ and Yang-Mills theory in four dimensions are given by the same superconformal group $SU(2,2|4)$. We presented the Kaluza-Klein masses and their multiplet classification corresponding to the superconformal group representations.

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Session Classification: Poster Session

Track Classification: HIGH ENERGY PHYSICS AND NUCLEAR MATTER

Contribution ID: 12

Type: **Oral**

Sagnac effect in solids

Thursday, 26 September 2024 10:20 (20 minutes)

The observation of the Sagnac effect for massive material particles offers a significant enhancement in sensitivity when compared to optical interferometers with equal area and angular rotation velocity. For this reason, there have been suggestions to employ solid-state interferometers that rely on semiconductors and graphene. We investigate the Sagnac effect in Dirac materials governed by the relativistic-like quasiparticle dispersion law and show that the fringe shift is still determined by the mass of a free electron. This confirms that graphene is indeed a promising material for creating solid-state Sagnac interferometers. Considering monolayer graphene with its linear dispersion law and comparing it with light provides a deeper understanding of the Sagnac effect.

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Session Classification: Morning Session 3

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 13

Type: Oral

Cubic-quintic interplay in the nonlinear Klein–Gordon model

Tuesday, 24 September 2024 12:50 (20 minutes)

The nonlinear Klein–Gordon (nKG) model,

$$\partial_{tt}\phi - c^2\partial_{xx}\phi + f(\phi) = 0,$$

is a universal model for describing the propagation of nonlinear waves in various physical media. For example, its stationary version describes the macroscopic wave function of the condensed phase (i.e., the order parameter) in the Landau theory of phase transitions. Noteworthy is also an application of the nKG model to modelling the spatially localised oscillating excitations of biological structures such as DNA chains. Here, the unknown real function ϕ is a characteristic of the wave field, t is time, x is coordinate, c is the velocity parameter that deals with the speed of interaction propagation. The function f is a nonlinear function of the wave field that describes the nonlinear response of the medium.

In this work, we are interested in the interplay between the cubic and quintic terms of the nonlinear response function, which we present as a truncated polynomial (corresponding to a ϕ^6 field model), $f(\phi) = \alpha_1\phi + \alpha_3\phi^3 + \alpha_5\phi^5$.

The real coefficient α_1 describes the linear response of the medium. The real coefficients α_3 and α_5 represent the cubic and quintic nonlinearities, respectively.

By reducing the nKG model to an extended cubic-quintic nonlinear Schrödinger equation in Hamiltonian form, we demonstrate that the quintic nonlinearity has a profound effect on the stability of wave packets to long-wave modulations. When there is no quintic nonlinearity (ϕ^4 field model), plain wave packets in such a system are known to be modulationally unstable for any carrier wave number in the case of negative coefficient at cubic nonlinearity. We show that such plain wave packets become modulationally stable for certain carrier wave numbers when the quintic nonlinearity becomes large enough. Such a stabilisation of the wave packet happens at certain critical ratio between the quintic and cubic coefficients of the nKG model.

This work proves that high-order nonlinear effects may play a decisive role in analysing physical phenomena in nonlinear models at certain conditions. This result may have practical implications for nonlinear media that exhibit the generation of higher harmonics and are characterised by a significant quintic nonlinearity (e.g. in polarisation). In particular, such conditions are met for ferroelectrics with first-order phase transition (e.g., BaTiO₃ crystals).

Publications:

1. Sedletsky Yu.V., Gandzha I.S. Hamiltonian form of extended cubic-quintic nonlinear Schrödinger equation in a nonlinear Klein–Gordon model. *Phys. Rev. E* 106, 064212 (2022). <https://doi.org/10.1103/PhysRevE.106.064212>
2. Sedletsky Yu.V., Gandzha I.S. Fifth-order nonlinear Schrödinger equation as Routhian reduction of the nonlinear Klein–Gordon model. *Proc. R. Soc. A* 479, 20230315 (2023). <https://doi.org/10.1098/rspa.2023.0315>

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Session Classification: Morning session 1

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 14

Type: **Oral**

Towards relations between compaction and compressibility of hard sphere mixtures

Thursday, 26 September 2024 14:30 (20 minutes)

The study of the influence of local properties of multi-particle conglomerations on their macroscopic properties is one among of the traditionally relevant problems of statistical physics. Parameterization of local properties can be carried out in various ways, for example, in terms of ordering parameter tensors, Euler invariants, Voronoi tessellations and others. While the macroscopic properties discussed above are the usual ones in statistical physics and thermodynamics, like compressibility, heat capacity, thermal conductivity, and others. In this paper, we study the influence of the compaction factor (packing) on the property of compressibility using the example of a model conglomeration of solid spheres, starting with a mono-disperse system and further, for multi-component mixtures. Using the known equations of state of the Carnahan-Starling type and their generalizations to the case of poly-disperse mixtures, the inverse problem of the influence of the proper parameters of the system (mixture) on the degree of compaction (packing) is considered. Non-monotonicity in the behavior of the packing parameter and the possibility of achieving its maximum value using a consistent selection of relations of the sizes of components and their molar fractions are shown. Application of the above-described approach to two different physical systems - a binary liquid mixture and a two-component granular system - showed quite good agreement between theory and experiment (especially in the case of a granular system). The proposed approach can be generalized without fundamental difficulties to the case of multi-particle conglomerations with an arbitrary number of components.

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Session Classification: Afternoon Session 3

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 16

Type: **Oral**

Quasicrystals in data coding

We discuss methods of modeling n -dimensional quasicrystals and their application to information encoding.

The first application is to use the mapping between the physical and internal spaces of a quasicrystal to evenly distribute data that is lost in the process of transmitting or storing information.

The second application consists in the construction of special quasi-crystals that satisfy the requirements of Vernam cipher keys of any length for the classical method.

Several examples of construction of quasicrystals with predetermined properties and examples of data processing that make the loss of its part uniformly distributed are given.

Below we give an example of information loss during data transmission in the original raster image and in the image encoded with the help of a quasi-crystal.

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[2] Nesterenko M., Patera J., Quasicrystal models in cryptography, *AIP Conf. Proc.*, 1191, 148-159, 2009.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 17

Type: **Oral**

Periodic problem for the nonlinear Schrödinger equation by the Riemann-Hilbert approach

We develop the Riemann-Hilbert (RH) approach to the construction of periodic finite-band solutions to the focusing nonlinear Schrödinger (NLS) equation $iq_t + q_{xx} + 2|q|^2q = 0$. We show that a finite-band solution to the NLS equation can be given in terms of the solution of an associated RH problem, the jump conditions for which are characterized by specifying the endpoints of the arcs defining the contour of the RH problem and the constants (so-called phases) involved in the jump matrices. Moreover, in the case when the finite-band solution of the NLS is periodic in x , we solve the problem of retrieving the phases given the solution of the NLS equation evaluated at a fixed time (as a function of x on the periodicity interval). Our findings are corroborated by numerical examples of phases computation, demonstrating the viability of the method proposed.

[1] Shepelsky D., Karpenko I., Bogdanov S., Prilepsky J.E. Periodic finite-band solutions to the focusing nonlinear Schrödinger equation by the Fokas method: inverse and direct problems. Proc.R.Soc.A 480 (2024), 20230828.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 18

Type: Oral

Representations of solutions of some nonlinear PDEs in the form of series in powers of the δ -function

Representations of solutions of some nonlinear PDEs in the form of series in powers of the δ -function

S.L. Gefter, A.L. Piven', V. N. Karazin Kharkiv National University

Let K be an arbitrary integral domain with identity and let $K[x]$ be the ring of polynomials with coefficients in K . By a *copolynomial* we mean a K -linear mapping $T : K[x] \rightarrow K$. The module of copolynomials is denoted by $K[x]'$. If $T \in K[x]'$ and $p \in K[x]$, then the result of application $T \in K[x]'$ to $p \in K[x]$ is written as (T, p) . The derivative T' of a copolynomial $T \in K[x]'$ is defined in the same way as in the classical theory of generalized functions: $(T', p) = -(T, p')$, $p \in K[x]$. An important example of a copolynomial is the δ -function which is defined by $(\delta, p) = p(0)$, $p \in K[x]$.

The *Cauchy-Stieltjes transform* of a copolynomial $T \in K[x]'$ is defined as the following formal Laurent series from the ring $\frac{1}{s}K[[\frac{1}{s}]]$: $C(T)(s) = \sum_{k=0}^{\infty} \frac{(T, x^k)}{s^{k+1}}$. The mapping

$C : K[x]' \rightarrow \frac{1}{s}K[[\frac{1}{s}]]$ is an isomorphism of K -modules. The multiplication of copolynomials is defined through the multiplication of their Cauchy-Stieltjes transforms.

The theory of linear PDEs over the module $K[x]'[[t]]$ was studied in [1,2]. We prove the following existence and uniqueness theorem for the Cauchy problem for some nonlinear PDEs.

Theorem. *Let $K \supset \mathbb{Q}$, $a \in K$ and let $m_j \in \mathbb{N}_0$ ($j = 0, 1, 2, 3$).*

Then the Cauchy problem

$\frac{\partial u}{\partial t} = au^{m_0} \left(\frac{\partial u}{\partial x}\right)^{m_1} \left(\frac{\partial^2 u}{\partial x^2}\right)^{m_2} \left(\frac{\partial^3 u}{\partial x^3}\right)^{m_3}$, $u(0, x) = \delta(x)$ *has a unique solution in $K[x]'[[t]]$. This solution is of the form*

$u(t, x) = \sum_{k=0}^{\infty} u_k \delta^{n_{k+1}} t^k$, *where $u_k \in K$ and $n = \sum_{j=0}^3 (j+1)m_j - 1$. Moreover, for every $t \in K$ this series converges in the topology of $K[x]'$.*

As examples we consider a Cauchy problem for the Euler-Hopf equation $\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} = 0$, for a Hamilton-Jacobi type equation $\frac{\partial u}{\partial t} = \left(\frac{\partial u}{\partial x}\right)^2$ and for the Harry Dym equation $\frac{\partial u}{\partial t} = u^3 \frac{\partial^3 u}{\partial x^3}$.

This work was supported by the Akhiezer Foundation.

[1] S.L. Gefter, A.L. Piven', Linear Partial Differential Equations in Module of Formal Generalized Functions over Commutative Ring, J. Math. Sci., \textbf{257} (2021), No.5, 579–596.

[2] S.L. Gefter, A.L. Piven', Linear Partial Differential Equations in Module of Copolynomials of Several Variables over a Commutative Ring, <http://arxiv.org/abs/2407.04122>

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 19

Type: **Lecture**

On M. Bogolyubov manuscripts at the Institute of Mathematics

M. Bogolyubov was officially admitted by the Institute of Mathematics as a senior researcher on March 1, 1945. On April 1, he assumed the head of the Department of Asymptotic Methods and Statistical Mechanics. The dismissal order, dated November 1, 1956, was signed by his student Yu.O. Mitropolsky, who was at that time the deputy acting director of the institute, O.S. Parasyuk. However, M. Bogolyubov's fate was intertwined with the Institute long before. He was a student of Professor D.O. Grave, who founded the Institute of Mathematics at the Ukrainian Academy of Sciences in March 1920. From the age of thirteen, M. Bogolyubov became a participant in the well-known mathematical seminar of D.O. Grave. Under its influence, he is forming as a scientist in the field of mathematical and theoretical physics. Later in June 1925, at the request of D.O. Grave, the Small Presidium of Ukrainian Academy of Sciences decided to consider M. Bogolyubov as a graduate student of the research department of mathematics in Kyiv. In 1928, he defended his doctoral dissertation.

The list of references below includes the scientific masterpieces created by Bogolyubov at the Institute of Mathematics.

In his renowned monograph "Problems of Dynamic Theory in Statistical Physics" [1], which was a manuscript of a report for 1945 at the Institute of Mathematics in Kyiv, M. Bogolyubov formulated a consistent approach to the problem of deriving kinetic equations from the dynamics of many particles. Using perturbation theory methods, a strategy was developed for constructing a generalization of the Boltzmann equation, known as the Bogolyubov kinetic equation, and for the first time, other kinetic equations were substantiated. This work clarified the mechanism of irreversibility in the evolution of many-particle systems, whose dynamics are described by time-reversible fundamental evolution equations. These results were extended to quantum many-particle systems [3],[7]. In the pioneering work [6] the superfluidity phenomenon was first described employing the quantum kinetic equation. A little later, in the Proceedings of the Institute of Mathematics [8], M. Bogolyubov published an article on deriving hydrodynamic equations from the Bogolyubov-Born-Green-Kirkwood-Yvon hierarchy of fundamental evolution equations.

The ideas conceived by Bogolyubov at the Institute of Mathematics have laid the groundwork for the theory of kinetic equations and became the cradle of modern statistical mechanics, as noted in our time.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 20

Type: Oral

To 190 years of the Wave of Translation and 50 years of the Davydov's soliton: Soliton dynamics in an oscillating magnetic field.

Tuesday, 24 September 2024 12:30 (20 minutes)

In this talk some less known facts of the discovery of the Wave of Translation will be discussed. A brief review of the advancement of the theory of Davydov's solitons will be given. New results on the study of the dynamics of the Davydov's soliton [1] in an external oscillating in time magnetic field [2,3] will be reported.

It is shown that in the magnetic field, perpendicular to the molecular chain axis, soliton wave function is a superposition of the electron plane wave in the plane perpendicular to the molecular chain, and longitudinal component of the wave function which satisfies the modified Nonlinear Schroedinger equation which is solved using the perturbation method based on the inverse scattering transform. It is shown that soliton width and amplitude are constant, while its velocity and phase are oscillating in time functions with the frequency of the main harmonic determined by the magnetic field frequency. Account of the energy dissipation results in bounding soliton velocity from above due to the balance of the energy gain from the magnetic field, and its loss because of the radiation of linear sound waves and energy dissipation. Soliton radiation due to time-depending velocity is calculated and shown to be the most intensive at the resonant frequency of the magnetic field. It is concluded that such complex impact of time-depending magnetic fields on charge transport, provided by solitons, can affect functioning of the devices based on low-dimensional molecular systems. These results suggest the physical mechanism of the resonant therapeutic effects of oscillating magnetic fields as the resonant impact of the magnetic field on the charge transport processes provided by solitons in the redox processes [4,5].

Acknowledgement:

This work was supported by the fundamental scientific program 0122U000887 of the Department of Physics and Astronomy of the National Academy of Sciences of Ukraine. The author acknowledges the Simons Foundation (NY).

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Session Classification: Morning session 1

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 21

Type: Oral

Application of Langevin dynamics for optimization in machine learning tasks

Wednesday, 25 September 2024 15:30 (20 minutes)

A rapid growth of Machine Learning (ML) applications in different areas has been faced in recent years. Training of ML models is performed by finding such values of their parameters $x = \{x_1, x_2, \dots, x_N\}$ that optimize (minimize) the objective (loss) function $U(x)$. Usually, the number of parameters N is large and the training dataset is massive. Therefore, to reduce computational costs, the gradient $f = -dU(x)/dx$ of the objective function with respect to the model parameters is computed on relatively small subsets of the training data, called mini-batches. If these mini-batches are selected randomly from the training dataset, then the estimated values of the loss $\hat{U}(x)$ and its gradient $\hat{f} = -d\hat{U}(x)/dx$ are the stochastic approximations of their exact values. Therefore, it is natural to apply Langevin dynamics to treat this stochastic optimization problem. We consider the next discrete form of the Langevin equation:

$$\frac{\Delta x_{n+1} - \Delta x_n}{\Delta t^2} = \hat{f}_n - \gamma \frac{\Delta x_{n+1} + \Delta x_n}{2\Delta t}, \quad (1)$$

where n is an iteration number, $\Delta x_{n+1} = x_{n+1} - x_n$, Δt is a time step and $\gamma > 0$ is a viscous friction coefficient.

Now, it is straightforward to obtain the next parameter updating formula:

$$\Delta x_{n+1} = \rho \Delta x_n + \hat{f}_n \cdot \eta, \quad (2)$$

where $\rho = (1 - \gamma\Delta t/2)/(1 + \gamma\Delta t/2)$ is conventionally called a momentum coefficient and $\eta = \Delta t^2(1 + \rho)/2$ a learning rate constant.

Equation (2) was derived in our recent work where we have introduced Coolmomentum – a method for stochastic optimization by Langevin dynamics with simulated annealing [1]. To implement simulated annealing (or slow cooling, in physical terms), we apply a certain schedule for the gradual momentum coefficient decrease in the range

$$0 \leq \rho < 1 \quad (3)$$

In this talk we demonstrate that application of Langevin dynamics (2) with simulated annealing (3) to multidimension optimization tasks gives promising results in artificial intelligence [1], quantum computing [2] and optical engineering [3].

Acknowledgement: OB, MB and IO have received funding through the EURIZON project, which is funded by the European Union under grant agreement No.871072. AS acknowledges support by the National Research Foundation of Ukraine, project No.2023.03/0073.

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Session Classification: Afternoon Session 2

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 22

Type: **Oral**

On structure of the point spectrum in equilibrium states of the dynamical conflict systems

V. Koshmanenko, O. Satur (Institute of mathematics of NAS Ukraine, Kyiv, Ukraine)

On structure of the point spectrum
in equilibrium states of the dynamical conflict systems

The structure of the point spectrum in equilibrium time-limiting states of dynamical conflict systems is studied in terms of probability measures. It is shown that the priority strategy in a single direction is a necessary and sufficient condition for emergence of measures with a point spectrum. In this case, the exponential rate of concentration of distributions with a point spectrum and its density in the phase space is established. The possibility of applying information about the structure of the point spectrum in a new mathematical model of opinion formation among individuals of abstract society is proposed. The presented result is developed the constructions published in [1,2]

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 23

Type: **Oral**

Local nearring extensions

Obviously, the direct product of nearrings with identity is a nearring with identity. At the same time, the direct product of two arbitrary local nearrings is not a local nearring. Naturally, the question arises of defining such a product, the result of which is a local nearring.

The semidirect product of the ring R with the abelian group G , which is a nearring, was given in [1]. We generalized such product to local nearrings, i.e., local nearring extensions.

Acknowledgements. Authors would like to thank to IIE-SRF for supporting of their fellowships at the University of Warsaw.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 24

Type: Oral

Well-posedness of the Cauchy problem for the two-component peakon system

We consider the Cauchy problem for the following two-component peakon system with cubic nonlinearity:

$$\partial_t m = \partial_x [m(u - \partial_x u)(v + \partial_x v)],$$

$$\partial_t n = \partial_x [n(u - \partial_x u)(v + \partial_x v)],$$

$$m = u - \partial_x^2 u, \quad n = v - \partial_x^2 v,$$

where $m = m(t, x)$, $u = u(t, x)$, $v = v(t, x)$ and $t, x \in \mathbb{R}$. We assume that the initial data $u_0(x) = u(0, x)$ and $v_0(x) = v(0, x)$ belong to the space $C^{k+2}(\mathbb{R}) \cap W^{k+2,1}(\mathbb{R})$ with $k \in \mathbb{N} \cup \{0\}$.

Considered peakon system was introduced by Song, Qu and Qiao in [3] as a generalization of the celebrated Fokas-Olver-Rosenau-Qiao (FORQ) equation: taking $u = v$, one obtains the FORQ equation, which has the form

$$\partial_t m = \partial_x [m(u^2 - (\partial_x u)^2)], \quad m = u - \partial_x^2 u.$$

Our major goal is to investigate the local existence, uniqueness and continuous dependence on the initial data of the solution. Revisiting the method of characteristics, developed for addressing the FORQ equation in [1], we establish existence and uniqueness of the solution (u, v) of the Cauchy problem for the two-component system in the class $C([-T, T], C^{k+2}(\mathbb{R}) \cap W^{k+2,1}(\mathbb{R}))$ with $k \in \mathbb{N} \cup \{0\}$ and some $T > 0$ [2]. Notice that the class of regularity corresponded to $k = 0$ is lower than that previously considered in the works for the FORQ equation. The most challenging part of the analysis consists in proving uniqueness in the case $k = 0$. To this end we must demonstrate that a solution satisfies a specific conservation law involving m, n and the characteristic, which, in turn, entails studying the two-component system in a weak sense.

Also we prove the Lipschitz continuity of the data-to-solution map for (m, n) within the space $C^k(\mathbb{R}) \cap W^{k,1}(\mathbb{R})$ with $k \in \mathbb{N} \cup \{0\}$ [2]. To the best of our knowledge, this result was not reported before in the related works for the FORQ equation, wherein the Lipschitz property is established for (u, v) in $W^{1,1}$ under assumption of existence of weak solution (u, v) in $L^\infty([-T, T], W^{2,1}(\mathbb{R}))$, see [4].

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 25

Type: **Oral**

Reading Ernst Ising's dissertation hundred years on

Tuesday, 24 September 2024 11:00 (40 minutes)

The Ising model is an archetype describing collective ordering processes. As such, it is widely known in physics and far beyond. Less known is the fact that the thesis defended by Ernst Ising 100 years ago under supervision of Wilhelm Lenz [1] contained not only the solution of what we call now the 'classical 1D Ising model' but also other problems. Some of these problems are the subject of this report [2,3]. In particular, I will discuss (i) a model proposed in 1922 by Walter Schottky and its relation to the Ising model [2]; (ii) the combinatorial method Ernst Ising used to calculate the partition function for a chain of elementary magnets [3]; (iii) the generalizations of the two-state model suggested in Ernst Ising's thesis but not exposed in his paper [3]. The talk is a part of an ongoing project that aims to prepare a bilingual, commented edition of the doctoral thesis of Ernst Ising [4].

[1]. Beitrag zur Theorie des Ferro- und Paramagnetismus. Dissertation zur Erlangung der Doktorwürde der Mathematisch-Naturwissenschaftlichen Fakultät der Hamburgischen Universität vorgelegt von Ernst Ising aus Bochum. Hamburg 1924; E. Ising. Beitrag zur Theorie des Ferromagnetismus. Zeitschr. f. Phys. 31 (1925) 253–258.

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Session Classification: Morning session 1

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 26

Type: **Poster**

Evaluating Benchmarks for the Effectiveness of Infrared Camouflage Coatings

Tuesday, 24 September 2024 17:35 (5 minutes)

Contemporary research in defense technology focuses extensively on concealing various objects from infrared (IR) reconnaissance. Numerous camouflage coatings are available in the market, designed to mask IR radiation emitted by targets. Manufacturers often claim that these coatings significantly reduce the mean apparent temperature difference (ΔT) between the object and its background. However, a critical scientific question remains: how does the reduction in ΔT correlate with the actual decrease in maximum detection range (MDR) achieved by thermal imaging systems?

A wide range of cooled and uncooled portable thermal imagers exists for the 3-5 μm and 8-12 μm spectral ranges. Their detection capabilities are constrained by both spatial resolution and thermal sensitivity, characterized by the noise equivalent temperature difference (NETD). To estimate the MDR reduction due to target temperature contrast masking, it is valuable to evaluate the MDR for several commercially available thermal imagers at distances where their sensitivity for chosen object size is not restricted by spatial resolution. According to NATO Standard STANAG 4347, the MDR for a target can be determined by graphically solving an equation. The left-hand side of this equation represents the simple exponential decay of ΔT with distance, while the right-hand side denotes the minimum resolvable temperature difference (MRTD) of the thermal imager, which is also dependent on distance and target dimensions. The MRTD for a high-resolution thermal imager in the 3-5 μm range was obtained from literature [1].

Our modeling aimed to assess how a 50% reduction in target ΔT affects the MDR and to evaluate the significance of this change relative to potential variations due to adverse weather conditions. We modeled targets with $\Delta T = 4 \text{ K}$ (uncamouflaged) and $\Delta T = 2 \text{ K}$ (camouflaged), using atmospheric absorption coefficients of $k = 0.2 \text{ 1/km}$ (good transmission conditions) and $k = 1 \text{ 1/km}$ (limited transmission conditions). The dimensions of the test target were set at $1 \times 1 \text{ m}^2$.

The modeling results for the 3-5 μm range are presented in the Figure 1. The MDR is determined at the intersection point of the ΔT and MRTD curves. Our findings indicate that a 50% decrease in ΔT has only a slight impact on MDR reduction under any weather conditions. Consequently, effective IR camouflage coatings should provide a substantially greater reduction in the observed temperature difference between the target and background. Furthermore, our modeling revealed that the MDR for a target with a fixed ΔT can vary by several times depending on weather conditions. Similar modeling was also conducted for the 8-12 μm range.

This study was supported by NRFU project #2023.04/0026.

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Fig.1. The modeling results for the 3–5 μm range MDR for variable weather conditions, for camouflaged and uncamouflaged targets.

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Session Classification: Poster Session

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 27

Type: **Oral**

Chemical freeze-out curve in heavy-ion collisions and the QCD critical point

Wednesday, 25 September 2024 16:40 (20 minutes)

The chemical freeze-out curve in heavy-ion collisions is investigated in the context of QCD critical point (CP) search at finite baryon densities. Taking the hadron resonance gas picture at face value, chemical freeze-out points at a given baryochemical potential provide a lower bound on the possible temperature of the QCD CP. We first verify that the freeze-out data in heavy-ion collisions are well described by a constant energy per particle curve, $E/N = \text{const}$, under strangeness neutrality conditions ($\mu_S \neq 0, \mu_Q \neq 0$). We then evaluate the hypothetical freeze-out curve based on this criterion in the absence of strangeness neutrality ($\mu_S = 0, \mu_Q = 0$) and confront it with recent predictions on the CP location. We find that recent estimates based on Yang-Lee edge singularities from lattice QCD data on coarse lattices place the CP significantly below the freeze-out curve and are thus disfavored by the heavy-ion data. On the other hand, predictions based on functional methods and holography place the CP slightly above the freeze-out curve, indicating that the QCD CP may be located very close to the chemical freeze-out in A+A collisions at $\sqrt{s_{NN}} = 3.5 \div 5$ GeV.

The report is based on a recently published article: <https://arxiv.org/abs/2408.06473>

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Session Classification: Afternoon Session 2

Track Classification: HIGH ENERGY PHYSICS AND NUCLEAR MATTER

Contribution ID: 28

Type: Poster

Fitting of the Cumulative Function for a Distribution of Statistic from the One-Sample Anderson-Darling Test

The Anderson-Darling test uses a statistic:

$$W_n^2 = n \int_{-\infty}^{+\infty} (F_n(x) - F(x))^2 \psi(F(x)) dF(x), \quad (1)$$

where $u = F(x)$ is cumulative function of a known distribution; $F_n(x)$ is cumulative function of an empirical distribution; $\psi(u)$ is weight function; n is sample size [1],

to estimate the amount of an empirical distribution deviation from a given distribution.

The statistic (1) with weight function $\psi(u) \equiv 1$ for large samples has a distribution with a cumulative function, which is approximately expressed by the formula:

$$A_1(z) = \frac{1}{\pi\sqrt{z}} \sum_{j=0}^{\infty} \frac{\Gamma(j+\frac{1}{2})}{j!\Gamma(\frac{1}{2})} \cdot \sqrt{4j+1} \cdot \exp\left(-\frac{(4j+1)^2}{16z}\right) \cdot K\left(\frac{1}{4}, \frac{(4j+1)^2}{16z}\right), \quad (2)$$

where $\Gamma(x)$ is gamma function; $K(\mu, x)$ is modified Bessel function of the second kind [1].

The complexity of calculating the significance points for a given significance level, the dependence of the expression of function (2) on the type of theoretical distribution when its parameters are unknown, led to the absence of the Anderson-Darling test, for example, in the Excel spreadsheet editor Maple math software. In practice, tabulated values of significance points are mostly used [2].

In these theses, it is shown that a cumulative function $A_1(z)$ can be fitting with satisfactory accuracy by a cumulative function belonging to a generalized family of cumulative functions as:

$$F(z) = (1 + \nu)^\omega \cdot \left(\frac{G(z)}{\nu + G(z)}\right)^\omega, \quad (3)$$

where $\nu > 0$, $\omega > 0$, $G(z)$ is cumulative function of a continuous distribution [3].

It is proposed to choose the cumulative function of Weibull distribution as the function $G(z)$:

$$G(z) = 1 - \exp\left(-\left(\frac{z}{\theta}\right)^c\right), \quad (4)$$

where $z \geq 0$, $\theta > 0$, $c > 0$.

It is shown that at the values of the coefficients: $c = 1.1365$, $\theta = 0.2263$, $\nu = 0.0217$, $\omega = 20.5000$ the mean square error of approximating the cumulative distribution function (2) using functions (3) and (4) is $Q = 1.7359 \cdot 10^{-7}$. Calculations were performed with double precision in Maple software. The given numerical values are rounded to the fourth decimal place.

When using the proposed fitting, the significance points of the Anderson-Darling test coincide with those previously published up to and including the second decimal place.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 29

Type: **Oral**

Systems of Eikonal Equations - Construction of General Solutions.

The eikonal equation is a first-order nonlinear partial differential equation $u_\mu u_\mu = f(x_\mu, u)$. Such equations are used to describe various physical processes, in particular, ray propagation in optics. We consider equations in the space of independent variables x_μ , where the indices μ span from 0 to some arbitrary n . Here lower indices of functions mean differentiation under x_μ , and we use a standard summation in the Minkovski metric.

Much literature exists on numerical solutions of systems of both coupled and separate eikonal equations. Using hodograph and contact transformations, we construct general exact solutions of such systems as parametric formulae, similar to our results in [1,2]. We also consider the relationship between these general parametric solutions and known exact solutions obtained by the Lie symmetry methods. General solutions of the systems of eikonal equations are useful in the symmetry analysis of partial differential equations, as these systems enter into reduction conditions of many higher-order relativistic PDE.

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2. Iryna Yehorchenko, Eikonal Equation 0.1, arXiv:2212.09914

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 30

Type: Oral

Recursive Method for Calculating T-Matrix of Electron Scattering on Arbitrary Many-Particle Clusters in Strongly Correlated Systems

Thursday, 26 September 2024 11:00 (20 minutes)

The generalized recursive method for calculating the T-matrix of electron scattering on arbitrary many-particle clusters for determining the Green's function of the strongly correlated system is developed. This approach is extended to the studying electronic spectra in both direct (Wannier) and reciprocal (Bloch) representations with taking into account the influence of atomic and magnetic correlations arising in the system at a temperature of 0 K. The one-band Hubbard model, the correlated random field approximation, and the one-site coherent potential approximation for the effective Hamiltonian of system are also used in this approach. The spectral density in reciprocal space is calculated in the same way (the same scheme) as in direct space, using the appropriate expressions for the effective Green's function, which includes contributions from all crystal sublattices. Calculation of the small parameter of the cluster expansion of the Green's function in direct and reciprocal representations shows its smallness for different parameters of b.c.c alloys. This ensures the convergence of obtained recursive formulas for T-matrix of scattering on many-particle clusters and the applicability of pairwise approximation for T-matrix. It should be noted that to calculate the configuration-averaged Green's function it is necessary to use at least the pairwise approximation of T-matrix for describing the influence of the cluster environment of each atom on the redistribution of charge and spin densities on atoms, as well as atomic and magnetic correlations. In addition, the possibility of nanoclusters formation and their influence on the magnetic state was investigated in the b.c.c. alloy with strong electron correlations. The calculation of electronic spectra in the reciprocal (as in direct) representation showed the high sensitivity to the changes in the characteristics and composition of the b.c.c. alloy including the nanoclusters formation as well as to the change of resulting short-range atomic and magnetic orders. This method could be useful to analyze experimental data obtained, for example, in positron spectroscopy to study electronic structure, defects, chemical composition, and various correlations in systems.

Key words: Green's function for strongly correlated alloys, recursive expression for T-matrix, arbitrary many-particle clusters, short-range atomic and magnetic ordering.

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Session Classification: Morning Session 3

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 31

Type: **Lecture**

New identities for differential-polynomial structures built from Jacobian determinants

The Nambu-determinant Poisson brackets on \mathbb{R}^d are expressed by the formula

$$\{f, g\}_d(x) = \rho(x) \det(\partial(f, g, a_1, \dots, a_{d-2}) / \partial(x^1, \dots, x^d)),$$

where a_1, \dots, a_{d-2} are smooth functions and x^1, \dots, x^d are global coordinates (e.g., Cartesian), so that $\rho(x) \partial_{x^i}$ is the top-degree multivector.

For an example of Nambu–Poisson bracket in classical mechanics, consider the Euler top with $\{x, y\}_3 = z$ and so on cyclically on \mathbb{R}^3 .

Independently, Nambu's binary bracket $\{-, -\}_d$ with Jacobian determinant and $d-2$ Casimirs a_1, \dots, a_{d-2} belong to the Nambu (1973) class of N -ary multi-linear antisymmetric polyderivational brackets $\{-, \dots, -\}_d$ which satisfy natural N -ary generalizations of the Jacobi identity for Lie algebras.

In the study of Kontsevich's infinitesimal deformations of Poisson brackets by using 'good' cocycles from the graph complex, we detect case-by-case that these deformations preserve the Nambu class, and we observe new, highly nonlinear differential-polynomial identities for Jacobian determinants over affine manifolds. In this talk, several types of such identities will be presented.

(Work in progress, joint with M.Jagoe Brown, F.Schipper, and R.Buring; special thanks to the Habrok high-performance computing cluster.)

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 32

Type: **Oral**

Thermodynamics of the kagome Heisenberg antiferromagnets

Wednesday, 25 September 2024 11:40 (20 minutes)

Kagome-lattice Heisenberg antiferromagnet is a paradigmatic model in the field of frustrated magnetism that allows us to study the interplay of geometrical frustration and quantum as well as thermal fluctuations in two and three dimensions. Distinctive spectrum of this model manifest itself in the thermodynamic properties throughout the peculiar low-temperature behavior of the specific heat.

We use 16 terms of a high-temperature series expansion complemented by the entropy-method interpolation to examine the specific heat and the uniform susceptibility of the Heisenberg model on the three-dimensional kagome (hyperkagome) lattice. We obtain thermodynamic quantities for several scenarios determined by the behavior of the specific heat as the temperature tends to zero. All scenarios give rise to a low-temperature peak in $c(T)$ well below the main high-temperature peak. The functional form of the uniform susceptibility $\chi(T)$ below about $T = 0.5$ depends strongly on the chosen scenario. An estimate for the ground-state energy e_0 depends on the adopted specific scenario but is expected to lie between -0.441 and -0.435 . In addition to the entropy-method interpolation, we use the finite-temperature Lanczos method to calculate $c(T)$ and $\chi(T)$ for finite lattices of $N = 24$ and 36 sites.

This project is funded by the National Research Foundation of Ukraine (2023.03/0063, Frustrated quantum magnets under various external conditions).

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Session Classification: Morning Session 2

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 34

Type: **Poster**

Invisible states Potts model

Tuesday, 24 September 2024 17:40 (5 minutes)

The Potts model with invisible states was introduced to explain discrepancies between theoretical predictions and experimental observations of phase transitions in some systems where Z_q symmetry is spontaneously broken [1]. It differs from the ordinary q -state Potts model in that each spin, besides the usual q visible states, can be also in any of r so-called invisible states. Spins in an invisible state do not interact with their neighbours but they do contribute to the entropy of the system. As a consequence, an increase in r may cause a phase transition to change from second to first order. Potts models with invisible states describe a number of systems of interest in physics and beyond and have been treated by various tools of statistical and mathematical physics. We aim to give a review of this fundamental topic based on our results [2-4]. Mainly, our goal was to investigate the energy-entropy interplay influence on the phase transition in the Potts model with invisible states in 1D case [2] as well as on different graph topologies [3].

We acknowledge support from the National Research Foundation of Ukraine, Project 2023.03/0099 “Criticality of complex systems: fundamental aspects and applications”.

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Session Classification: Poster Session

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 35

Type: **Oral**

Adomian decomposition method for nonlinear boundary-value problems unsolved with respect to the derivative in the critical case

We establish constructive necessary and sufficient conditions of solvability and a scheme for the construction of solutions for a nonlinear boundary-value problem unsolved with respect to the derivative in the critical case [1], [2], [3].

On the basis of the Adomian decomposition method [4], [5] we are constructed convergent iterative schemes for finding approximations to solutions of a nonlinear boundary-value problem unsolved with respect to the derivative [3]. As an example of application of the proposed iterative scheme, we find approximations to the solutions of periodic boundary-value problems for a Rayleigh-type equation unsolved with respect to the derivative, in particular, in the case of a periodic problem for the equation that is used to describe the motion of satellites on elliptic orbits [3].

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[5] *Chuiko S.M., Chuiko O.S., Popov M.V.* Adomian decomposition method in the theory of nonlinear boundary-value problems. Journal of Mathematical Sciences. 2023, **27 7(2)**, P. 338-351.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 36

Type: Oral

Approximation of the solutions of nonlinear matrix equations using the Newton–Kantorovich method

The study of nonlinear matrix equations, in particular, the algebraic matrix Riccati equation [1,2,3], is connected with numerous applications of such equations in solving the differential matrix Riccati equation [2,3], in the theory of nonlinear oscillations, in mechanics, biology, and radiotechnology, the theory of control and stability of motion, and others. We used the Newton-Kantorovich method [3] and the Adomian decomposition method to find approximations for the solutions of nonlinear matrix equations in the case of an unknown rectangular matrix [4,5].

This work was partially supported by a grant from the Simons Foundation (PD-Ukraine-00010584, K.S. Shevtsova).

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[5] *Chuiiko S.M., Chuiiko O.S., Popov M.V.* Adomian decomposition method in the theory of nonlinear boundary-value problems. *Journal of Mathematical Sciences.* 2023, **277(2)**, P. 338-351.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 37

Type: Oral

Extremal decomposition problem for points on an arbitrary ellipse

Let \mathbb{C} be the complex plane, $\overline{\mathbb{C}} = \mathbb{C} \cup \{\infty\}$ be its one point compactification. A function $g_B(z, a)$ which is continuous in $\overline{\mathbb{C}}$, harmonic in $B \setminus \{a\}$ apart from z , vanishes outside B , and in the neighborhood of a has the following asymptotic expansion $g_B(z, a) = -\log|z - a| + \gamma + o(1)$, $z \rightarrow a$, is called the (classical) Green function of the domain B with pole at $a \in B$. The inner radius $r(B, a)$ of the domain B with respect to a point a is the quantity e^γ . By using the variational method G.M. Goluzin established that for functions $f_k(z)$ which univalently map the disc $|z| < 1$ onto mutually non-overlapping domains, $k \in \{1, 2, 3\}$, exact estimate holds $\left| \prod_{k=1}^3 f'_k(0) \right| \leq \frac{64}{81\sqrt{3}} |(f_1(0) - f_2(0))(f_1(0) - f_3(0))(f_2(0) - f_3(0))|$. Equality is attained only for functions $w = f_k(z)$ which conformally and univalently map the disc $|z| < 1$ onto the angles $2\pi/3$ with vertex at point $w = 0$ and bisectors of which pass through points $f_k(0)$, $|f_k(0)| = 1$. E.V. Kostyuchenko proved that the maximum value of multiplication of inner radii for three simply connected non-overlapping domains in the disk is attained for three equal sectors. However, this statement remains valid for multiply connected domains D_k . We have considered an extremal problem on the maximum of product of the inner radii on a system of n mutually non-overlapping multiply connected domains D_k containing the points a_k , $k = 1, \dots, n$, located on an arbitrary ellipse $\frac{x^2}{d^2} + \frac{y^2}{t^2} = 1$ for which $d^2 - t^2 = 1$.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 38

Type: **Poster**

AUTONOMOUS BOUNDARY-VALUE PROBLEM UNSOLVED WITH RESPECT TO THE DERIVATIVE IN THE CRITICAL CASE

We establish constructive necessary and sufficient conditions of solvability and propose a scheme for the construction of solutions of a nonlinear autonomous boundary-value problem unsolved with respect to the derivative [1,2,3] in the critical case.

We also construct convergent iterative schemes for finding approximations to the solutions of a nonlinear autonomous boundary-value problem unsolved with respect to the derivative. As examples of application of the obtained iterative schemes, we find approximations to the solutions of periodic boundary-value problems for Lienard-type equations unsolved with respect to the derivative [3].

The proposed procedure for the investigation of the conditions of solvability and the construction of solutions to autonomous boundary-value problems unsolved with respect to the derivative can be generalized to the case of autonomous boundary-value problems with impulsive influence [4].

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Primary author: Ms DIACHENKO, D.D.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 39

Type: **Poster**

ADOMIAN DECOMPOSITION METHOD IN THE THEORY OF NONLINEAR BOUNDARY VALUE PROBLEMS WITH DELAY IN THE CRITICAL CASE

We obtained constructive conditions for the solvability and a scheme for constructing solutions of a nonlinear boundary value problem with concentrated delay in the case of parametric resonance using the Adomian decomposition method. The original function of the differential system with delay contains an unknown eigenfunction that ensures the solvability of the weakly nonlinear boundary value problem [1,2]. By employing the Adomian decomposition method [3], we derived conditions for solvability and constructed a new iterative scheme to find solutions of the weakly nonlinear boundary value problem for a system of differential equations with delay, as well as its eigenfunction in the case of parametric resonance. We obtained constructive convergence conditions for the constructed iterative scheme towards the solution of the weakly nonlinear boundary value problem, as well as its eigenfunction. The research scheme for investigating boundary value problem with concentrated delay can be extended to matrix boundary value problems with concentrated delay [4].

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 40

Type: **Oral**

Resetting random walks in a bounded chain

Wednesday, 25 September 2024 15:10 (20 minutes)

The search of a target of unknown location is often random and ineffective, especially when the search domain is spacious and there is a lot of detrimental trajectories. To get rid of them, thereby improving the search, interruptions of the latter with starting it from scratch can be a good strategy. Called resetting, such a manner is in fact inherent to many search processes at very diverse levels of organization.

Initiated by the seminal work [1] devoted to diffusion with resetting along an infinite chain, the study of resetting effects in various model systems has quickly become a flourishing branch of the theory of stochastic processes. The vast majority of corresponding works, however, concerns spatially continuous models, whereas their discrete counterparts – such as random walks in lattices or networks – are not less important. For the latter, there were practically no exact results even in one dimension.

In the present talk, the recent results [2] on the resetting effects in one of the basic model – classical random walks with Poissonian resetting in a one-dimensional lattice – are expounded at length. The model is analyzed in its general version, for arbitrary initial and boundary conditions, which lead to a variety of optimization scenarios illustrated by non-standard behavior of the main observables (splitting probabilities, mean first passage times, coefficients of variation). A quantum analog of the model is briefly discussed.

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Session Classification: Afternoon Session 2

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 41

Type: **Poster**

The some solution of the Boltzmann equation

The Boltzmann equation [1] that describes the evolution of rarefied gases is one of the main equations of the kinetic theory of gases. For a model of hard spheres, the equation has the form:

$$D(f) = Q(f, f),$$

where the left-hand side of the equation is the differential operator:

$$D(f) \equiv \frac{\partial f}{\partial t} + \left(V, \frac{\partial f}{\partial x} \right),$$

and the right-hand side of the Boltzmann equation is the collision integral, which for the hard spheres model is as follows:

$$Q(f, f) \equiv \frac{d^2}{2} \int_{\mathbb{R}^3} dV_1 \int_{\Sigma} d\alpha |V - V_1, \alpha| \left[f(t, x, V_1') f(t, x, V') - f(t, x, V) f(t, x, V_1) \right],$$

where $f(t, x, V)$ is the distribution function of particles.

The problem of determination of the exact and approximate solutions of the Boltzmann equation in the explicit form is quite urgent. At present, the sole known exact solution of the Boltzmann equation is an expression usually called the Maxwell distribution or simply Maxwellian (after J. C. Maxwell, Scottish physicist). In the case of Maxwellians M , we get

$$D(f) = 0, \quad Q(f, f) = 0.$$

The solution to this equation will be looked for in the next form:

$$f(t, x, V) = \sum_{i=1}^{\infty} \varphi_i(t, x) M_i(t, x, V).$$

As a measure of the deviation between the parts of the Boltzmann equation we will consider a uniform-integral error of the form:

$$\Delta = \sup_{(t,x) \in \mathbb{R}^4} \int_{\mathbb{R}^3} dV \left| D(f) - Q(f, f) \right|.$$

In the paper [2], we were obtained sufficient conditions for the coefficient functions and hydrodynamic parameters appearing in the distribution, which enable one to make the analyzed error as small as desired.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 42

Type: **Oral**

Towards the study of quantum properties of the Borromean rings complement in the Poincaré ball

Guided by physical needs, we deal with the rotationally isotropic Poincaré ball, when considering the complement of Borromean rings embedded in it [1]. We describe the geometry of the complement and realize the fundamental group as isometry subgroup in three dimensions. According to Penner, we construct the Teichmüller space of the decorated ideal octahedral surface related to the quotient space of the fundamental group action. Using the conformality of decoration, we define six moduli and the mapping class group generated by cyclic permutations of the ideal vertices. Intending to quantize the geometric area, we state the connection between the induced geometry and the sine-Gordon model. Due to such a correspondence we obtain the differential two-form in the cotangent bundle. Focusing on a starlike body formed by regular ideal squares in three orthogonal planes (discs), we analyze quantum fluctuations of the body area, using the canonical quantization of the sine-Gordon model resulting in the Mathieu differential equation. Since, according to general predictions in quantum geometry [2], the area quantum fluctuations arise at the boundaries of geometric regions, we associate them with the decorated cuspidal tails of the surface. Using the (single) quantum state generated by the Hamiltonian constraint, we still get an indication of the presence of a gap in the spectrum of the area [2].

Keywords: Borromean rings complement; fundamental group; decorated Teichmüller space; sine-Gordon equation; area quantization; Mathieu equation

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 45

Type: **Oral**

Development and analysis of novel integrable nonlinear dynamical systems on quasi-one-dimensional lattices. Parametrically driven nonlinear system of pseudo-excitations on a two-leg ladder lattice

Thursday, 26 September 2024 11:40 (20 minutes)

Following the main principles of developing the evolutionary nonlinear integrable systems on quasi-one-dimensional lattices we suggest the novel nonlinear integrable system of parametrically driven pseudo-excitations on a regular two-leg ladder lattice. The initial (prototype) form of the system is derivable in the framework of semi-discrete zero-curvature equation with the spectral and evolution operators specified by the properly organized 3×3 square matrices. Although the lowest conserved local densities found via the direct recursive method do not prompt us the algebraic structure of system's Hamiltonian function, but the heuristically substantiated search for the suitable two-stage transformation of prototype field functions to the physically motivated ones has allowed to disclose the physically meaningful nonlinear integrable system with time-dependent longitudinal and transverse inter-site coupling parameters. The time dependencies of inter-site coupling parameters in the transformed system are consistently dened in terms of the accompanying parametric driver formalized by the set of four homogeneous ordinary linear differential equations with the time-dependent coefficients. The physically meaningful parametrically driven nonlinear system permits its concise Hamiltonian formulation with the two pairs of field functions serving as the two pairs of canonically conjugated field amplitudes. The explicit example of oscillatory parametric drive is described in full mathematical details.

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Session Classification: Morning Session 3

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 46

Type: **Oral**

Initial value problem in the case of multivalued dispersion equations

Thursday, 26 September 2024 15:50 (20 minutes)

Dispersion equations and relations are the key subjects of linear theories involving waves and collective excitations. However, in some systems, dispersion equations contain multivalued functions and their solutions are ambiguous. To resolve such uncertainty we suggest analyzing the initial value problem that gives the unambiguous solution.

As an example, we considered the excitation of the Dirac plasmons in graphene on a polar substrate and analyzed a strong coupling between plasmons in graphene and surface optical phonons of the substrate. Due to square-root singularity in graphene polarizability [1], the dispersion equation for this system contains branch points on the plane of complex frequency, ω . The use of the initial value problem gives a unique solution and clarifies the physical picture of coupled oscillations. Particularly, we found that lower plasmon-phonon mode, which in terms of dispersion can have a good quality factor, is almost absent in excitation spectra. The main physical reason for the mode collapse is the suppression of space-time-dependent electric fields near $\omega = v_F k$, where v_F is the Fermi velocity and k is the plasmon wavenumber [2]. The evidence of the collapse can be seen in the relevant experiments [3, 4].

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Presenter: KUKHTARUK, Serhii (V. E. Lashkaryov Institute of Semiconductor Physics NAS of Ukraine)

Session Classification: Afternoon Session 3

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 47

Type: **Poster**

A model of a conflict society with separate support for individual clusters

We study the mathematical model of an abstract society $calS = \{a_i\}_{i=1}^m$, $1 < m < \infty$ (a_i - players, opponents or their association) in the form of a complex dynamical system with a conflict interaction between its elements. The states of society S are described by stochastic vectors of players energy $\mathbf{p}^t = (p_1^t, \dots, p_i^t, \dots, p_m^t)$, $t = 0, 1, \dots$, which evolve according to the law of conflict interaction. Such models were studied in [1], [2], [3], for example.

Our new step is that we divide the set $calS$ into two clusters of individuals $calS = calS_J \cup calS_I$, where $J = \{j_1, \dots, j_n\}$ denotes a subset of such indices that individuals a_j receive external support at each step $t > 0$ in the form of an additive shift: $p_j^t \rightarrow p_j^t + b$, $b > 0$ and for $I = \{i_1, \dots, i_{m-n}\}$ individuals a_i remain without external support.

Thus, the dynamic system is given by difference equations:

$$p_i^{t+1} = \frac{p_i^t(1-r_i^t)}{z^t}, \quad p_j^{t+1} = \frac{(p_j^t+b_j)(1-r_j^t)}{z^t}, \quad i \in I, \quad j \in J, \quad t = 0, 1, \dots, \text{where } b_j = b > 0, \quad z^t = \sum_k (p_k^t + b \cdot \mathbf{1}_J(k))(1 - r_k^t), \quad \mathbf{1}_J(k) - \text{indicator function of a subset } J. \text{ Using of value } r_i^t = \frac{\sum_{k \neq i} p_k^t}{m-1} = \frac{1-p_i^t}{m-1} \text{ corresponds to the repulsive interaction of each individual } a_i \text{ with the rest of society } calS_{a_i}^\perp \text{ in the mean field sense. Denominator } z^t \text{ provides stochastic normalization.}$$

The main results concern systems with three elements (players). In this case, a description of all equilibrium states is given and their stability is investigated with depending on the parameter of external influence. Besides basins of attraction for point attractors are partially described and illustrated.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 48

Type: **Oral**

Orbital perturbation theory in Schwarzschild space-time

Thursday, 26 September 2024 16:30 (20 minutes)

In our work, we obtain a set of Gaussian orbital perturbation equations in the Schwarzschild space-time in terms of Weierstrass elliptic functions, and solve it for several external forces in linear approximation. We consider forces defined from: the cosmological constant in the Schwarzschild–de Sitter space-time, various quantum gravity corrections, angular momentum from the Kerr space-time and some others. From this we obtain several observables, in particular, we consider a simple “kludge” scheme for gravitational waveforms.

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Session Classification: Afternoon Session 3

Track Classification: ASTROPHYSICS AND COSMOLOGY

Contribution ID: 49

Type: Oral

Pauli resonances in single- and many-channel systems

Thursday, 26 September 2024 15:10 (20 minutes)

In this report, we present results of systematic investigations of peculiarities of redundant solutions of the resonating group method (RGM), which are known as the Pauli resonance states. Such resonance states appear when one tries to use more advanced (more precise) wave functions describing internal structure of interacting clusters. It is generally recognized that the Pauli resonance states are spurious solutions which blur real physical quantities such as phase shifts, cross sections. Their appearance cannot be attributed to enlarging of centrifugal and Coulomb barriers, they also appear in a single-channel approximation and thus the Pauli resonance cannot be considered as the Feshbach resonances.

The subject of our investigations is continuous spectrum states of light nuclei ${}^6\text{Li}$, ${}^7\text{Li}$, ${}^8\text{Be}$, ${}^9\text{Be}$ and ${}^{10}\text{B}$, which are considered as two-cluster systems. Special attention is paid to the Pauli resonance states which appear in interaction of ${}^6\text{Li}$ with neutrons, deuterons, tritons and alpha particles. All investigations are carried out in a three-cluster microscopic model, which was formulated in Ref. [1]. In this model dominant three-cluster configuration is transformed into a set of binary channels. One of the constituents of the binary channel is considered as a two-cluster subsystem. Spectrum of bound states and corresponding wave functions of the subsystem are obtained by solving the two-cluster Schrödinger equation. This allows us to use more adequate wave functions describing the internal structure of the two-cluster subsystem. This is rather important for two-cluster subsystems with a small separation energy, such as deuteron, ${}^6\text{Li}$ and so on. Within the model, Gaussian functions are used to describe relative motion of clusters in bound states of a two-cluster subsystem and oscillator functions are utilized to expand wave function of continuous spectrum states of compound nucleus. At the first stage of our investigation, we use single-channel approximation in order to detect and analyze the Pauli resonance states.

It is found that the Pauli resonance states in selected nuclei lie in the energy range between 11 and 45 MeV, and their widths are varied from 8 keV to 8 MeV. The most dense area of resonance states are concentrated in the interval $16 < E < 21$ MeV. Two dense area of widths of resonance states are located in intervals $0.008 < \Gamma < 0.22$ MeV and $0.9 < \Gamma < 1.2$ MeV. In many cases only one Pauli resonance state appeared in a binary channel. We also determined several cases with two resonance states. It was demonstrated, the number of the Pauli resonance states are correlated with number of the Pauli forbidden states in a simple version of the RGM, when simple functions of the many-particle shell-model are employed for describing internal motion of nucleons within each cluster.

We also investigate properties of the Pauli resonances in a many-channel model of ${}^6\text{Li}$. This nucleus is studied within a three-cluster model which involves two three-cluster configurations $\alpha + p + n$ and $t + d + p$. These cluster configurations allowed us to take into account all dominant binary decay channels of the nucleus. It is shown that the Pauli resonances are observed in the $\alpha + d$, ${}^5\text{He} + p$, ${}^5\text{Li} + n$, ${}^3\text{He} + t$ channels when they are treated separately. When channels are coupled, the Pauli resonances migrate from one to another channel and substantially change their energy and width. We demonstrated how Pauli resonances in single- and many-channel systems can be effectively eliminated with minimal effects on the ground and shape resonance states.

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Session Classification: Afternoon Session 3

Track Classification: HIGH ENERGY PHYSICS AND NUCLEAR MATTER

Contribution ID: 50

Type: Oral

Effect of the photon subsystem on the magnetic properties of quantum gases in equilibrium with radiation

Wednesday, 25 September 2024 14:30 (40 minutes)

We study the impact of the photon subsystem on the magnetic properties of a mixture of quantum gases in thermodynamic equilibrium with it. Having proposed a simple model of the system, we obtain general equations describing the thermodynamic equilibrium of quantum gases of two-level atoms with photons. The resulting equations are solved at a temperature higher than the degeneracy temperature of all three components. The analysis of the solutions shows the non-trivial dependence of magnetic properties on photon density and intensity of the external magnetic field. An increase in photon density due to external sources can lead to an increase in both magnetization and density of excited atoms. Such a conclusion is not a priori trivial since a photon in a vacuum does not have a magnetic moment.

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Session Classification: Afternoon Session 2

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 51

Type: **Oral**

Impurity-induced localized modes in parallel Josephson junction arrays

Thursday, 26 September 2024 10:40 (20 minutes)

We consider inhomogeneous underdamped one-dimensional parallel Josephson junction arrays. Inhomogeneity is introduced either as a non-uniformly applied dc bias current or as variations in the junctions' critical currents. We investigate the frequency of the localized modes induced by the presence of such inhomogeneities, in particular the frequency's dependence on the parameters that characterise inhomogeneities.

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Session Classification: Morning Session 3

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 52

Type: **Poster**

Constraints on the parameters of HNL and baryon asymmetry of the Universe

Tuesday, 24 September 2024 17:00 (5 minutes)

One of the simplest renormalizable extensions of the SM is the minimal neutrino extension of the Standard Model ν MSM, proposed in 2005 [1, 2]. This modification introduces three righthanded neutrinos or heavy neutral leptons (HNL). The lightest sterile neutrino is identified as a dark matter particle. The other two sterile neutrinos are much heavier, with nearly identical masses, and are responsible for generating the baryon asymmetry observed in the Universe. The observable parameters of the ν MSM Lagrangian are given in [3]

$$S_{\alpha\beta} \equiv (FM^{-1*}M^{-1}F^\dagger)_{\alpha\beta} = \sum_I S_{\alpha\beta}^I = \sum_I F_{\alpha I} F_{I\beta}^\dagger M_I^{-2}, \quad (1)$$

$$R_{\alpha\beta} = \sum_I R_{\alpha\beta}^I = \sum_I S_{\alpha\beta}^I \ln \frac{M_I}{M_W} = \sum_I F_{\alpha I} F_{I\beta}^\dagger M_I^{-2} \ln \frac{M_I}{M_W}. \quad (2)$$

In the ν MSM framework, the lightest sterile neutrino, which serves as a long-lived dark matter particle, is undetectable in collider experiments. Therefore, we focus on a simplified scenario that extends the SM by incorporating only two heavy sterile neutrinos. A straightforward relationship has been derived between the experimentally observed quantities (the elements of the matrices $S_{\alpha\beta}$ and $R_{\alpha\beta}$). This relationship holds for cases where active neutrinos have non-zero masses and where the masses of the heavy sterile neutrinos vary.

$$S_{\alpha\beta} \left(M_1 \ln \frac{M_2}{M_W} + M_2 \ln \frac{M_1}{M_W} \right) = R_{\alpha\beta} (M_1 + M_2), \quad S_{\alpha\alpha} S_{\beta\beta} = |S_{\alpha\beta}|^2 \quad R_{\alpha\alpha} R_{\beta\beta} = |R_{\alpha\beta}|^2. \quad (3)$$

Building on the results of [1], we have translated the constraints on baryon asymmetry generation in the early Universe into observable parameters $S_{\alpha\beta}$ and $R_{\alpha\beta}$. We concluded that the actual values of elements of \hat{R} and \hat{S} matrices are many orders of magnitude less than existing experimental constraints. Results of our investigation are presented in detail in [4].

Acknowledgment. The work of V.G. and O.Kh. was supported by the National Research Foundation of Ukraine under project No.2023.03/0149.

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Session Classification: Poster Session

Track Classification: HIGH ENERGY PHYSICS AND NUCLEAR MATTER

Contribution ID: 53

Type: **Poster**

The electric field quantum control of spin-waves dynamics in easy-axis antiferromagnets

*Tuesday, 24 September 2024 17:25 (5 minutes)*O. O. Boliashova^{1,2} and V. N. Krivoruchko³¹State Research Institution «Kyiv Academic University»

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Magnetic materials are widely used in current computers and have the potential to expand their applicability [1]. The most important step for practical applications is understanding how to manipulate spin dynamics in magnetic materials efficiently. One method that has been actively discussed is using an electric field. It is well known that spin waves with different chirality exist in antiferromagnets, however, in the absence of external influence these spin waves are degenerated. An electric, E , field can split them and manipulate each polarization differently. This phenomenon is an example of a topological effect known as the Aharonov-Casher effect [2,3]. In the linear order approximation, this effect can be accounted for by adding a term to the system's free energy expression like the Dzyaloshinskii-Moriya interaction.

We present the results on the E -field effect on chirality-dependent spin-waves dynamics in a two-sublattice easy-axis antiferromagnet [4,5]. The research was conducted using a phenomenological approach based on the Landau-Lifshitz-Gilbert equations. It was shown that the electric field can split spin waves of different chirality, and the magnitude of the splitting is proportional to the magnitude of the electric field. This splitting can be further enhanced by applying a magnetic field. More details are provided on the E -field effect on the propagation of spin waves and their damping length. The electric field affects the propagation of the right-handed and left-handed spin waves differently, while a small magnetic field doesn't influence the damping length. These findings could be useful for field-effect transistors or interferometric devices [6] based on spin waves. Since the application of the electric field is easier than that of a large magnetic field, the Aharonov-Casher effect has great potential for practical applications.

The authors acknowledge the financial support by the STCU, project "Magnetism in Ukraine Initiative", project Agreement No. 9918.

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Session Classification: Poster Session

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 54

Type: Oral

Asymptotic analysis of spectral problems for nonlocal operators

Many mathematical biology and population dynamics models involve nonlocal diffusion corresponding to long-range interactions in a system. These models are typically described by evolution problems with convolution-type integral operators and their qualitative and quantitative properties can be obtained by studying of the corresponding spectral problems.

We consider spectral problems

$$-\frac{1}{\varepsilon^d} \int_{\Omega} J\left(\frac{x-y}{\varepsilon}\right) \kappa(x, y) \rho_{\varepsilon}(y) dy + a(x) \rho_{\varepsilon}(x) = \lambda_{\varepsilon} \rho_{\varepsilon}(x) \quad (1)$$

in a bounded domain in $\Omega \subset \mathbb{R}^d$, where $J(z) \geq 0$ is a continuous function on \mathbb{R}^d decaying sufficiently fast as $|z| \rightarrow \infty$, $\kappa \in C^2(\overline{\Omega} \times \overline{\Omega})$, $\kappa > 0$ and (the potential) $a \in C^2(\overline{\Omega})$; $\varepsilon > 0$ is a scaling parameter. We study the asymptotic behavior of eigenvalues and eigenfunctions of (1) in the limit of small parameter ε .

We focus on the self-ajoint case when $J(z) = J(-z)$, $\kappa(x, y) = \kappa(y, x)$ and show that the principal eigenvalue of (1) exists for sufficiently small ε and converges to the minimum $m(x^*) = \min_{\overline{\Omega}} m(x)$, where $m(x) = a(x) - \kappa(x, x)$. More precise asymptotic description is obtained when m satisfies some non-degeneracy conditions at x^* . Namely, if the minimum is strict and the point x^* is an inner point of Ω then we suppose the positiveness of Hessian and via rescaling by $\varepsilon^{1/2}$ we derive a limit differential spectral problem of the form:

$$-\operatorname{div} A \nabla \rho + \partial_{ij}^2 m(x^*) z_i z_j \rho = \mu \rho \quad \text{in } \mathbb{R}^d. \quad (2)$$

We prove that $\lambda_{\varepsilon} = m(x^*) + \mu_k \varepsilon + \bar{o}(\varepsilon)$, where μ_k are eigenvalues of (2). The case $x^* \in \partial\Omega$ is more sophisticated and we consider the situation when Ω is a polyhedron and $m(x)$ attains its strict minimum at x^* on a face of $\partial\Omega$. Without loss of generality, we assume that $x^* = 0$ and locally Ω is given by $x_1 > 0$ in a neighborhood of 0. Then the non-degeneracy condition reads: $\partial_{x_1} m(0) > 0$, $\partial_{x_i x_j}^2 m(0) \xi_i \xi_j > 0 \forall \xi' \in \mathbb{R}^{d-1} \setminus \{0\}$. Under these conditions, we establish the following asymptotic formula for the eigenvalues $\lambda_{\varepsilon} = m(0) + \Lambda_1 \varepsilon^{2/3} + (\beta + \mu_k) \varepsilon + \bar{o}(\varepsilon)$, where Λ_1 is the principal eigenvalue of the 1D problem $-\theta \phi_0''(t) + \alpha t \phi_0(t) = \Lambda_1 \phi_0(t)$ on \mathbb{R}_+ , $\phi_0(0) = 0$, μ_k are eigenvalues of a harmonic oscillator in \mathbb{R}^{d-1} . In this case, eigenfunctions have the asymptotic form $\rho_{\varepsilon}(x) = \phi_0(\varepsilon^{-2/3} x_1) v(\varepsilon^{-1/2} x') + \dots$, that reveals emergence of two fine scales $\varepsilon^{2/3}$ and $\varepsilon^{1/2}$.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 55

Type: **Oral**

Critical Behavior of Structurally Disordered Systems Magnets with Long-Range Interaction

Wednesday, 25 September 2024 11:20 (20 minutes)

Our research aims to examine critical behavior of a magnetic system under the influence of two competing factors: long-range interaction and weak structural disorder (e.g., weak quenched dilution). We analyze ferromagnetic ordering in a structurally-disordered magnet within an n -vector model in d -dimensional space, where the long-range interaction decays with distance x as $J(x) \sim x^{-d-\sigma}$, where with σ as is the control parameter. Field-theoretical renormalization group methods (RG) are used to identify the system's universality classes, and the universal characteristics of critical behavior depending on the global parameters d, n, σ . We demonstrate that there exists a parameter region (d, n, σ) , where the interplay of long-range interaction and structural disorder leads to emergence of a new structural-disorder-induced long-range universality class. Using fixed spatial dimension approach we extract values of correlation length critical exponent ν characterizing this class from perturbative RG functions at $d = 3$ applying asymptotic series resummation methods.

This work was supported by the National Research Foundation of Ukraine, Project 246/0099 "Criticality of complex systems: fundamental aspects and applications".

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Session Classification: Morning Session 2

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 56

Type: **Oral**

Non-perturbative solutions of BBGKY hierarchy of evolution equations for colliding particles

From the moment the BBGKY hierarchy (Bogolyubov–Born–Green–Kirkwood–Yvon) was formulated in 1946 until the last decade, the solution to such a hierarchy of evolution equations has been represented in the form of an iteration series, i.e., expansion into a series constructed by perturbation theory methods. In particular, this representation of the solution is applied for the derivation of kinetic equations, the generally accepted method of derivation of which is the construction of the scaling asymptotics of the solution to the BBGKY hierarchy.

Recently, an approach has been developed for the rigorous derivation of kinetic equations for many particles interacting as hard spheres, based on the description of the evolution of observables and states [1-4]. This approach was successfully developed due to the use of non-perturbative solutions of the BBGKY hierarchy for systems of interacting particles.

In this talk, the structure of expansions that represent a non-perturbative solution of the Cauchy problem for the dual BBGKY hierarchy for observables of many hard spheres is substantiated, as well as expansions into series that represent a non-perturbative solution of the BBGKY hierarchy for their states.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 57

Type: **Oral**

Kinetic model of the formation of STM-induced electrofluorochromism in molecular junctions

Thursday, 26 September 2024 12:50 (20 minutes)

Experimental data on STM-induced electroluminescence in monomolecular junctions have led to the need to elucidate the physics of the formation of optoelectronic processes at the atomic-molecular level, taking into account both dynamic and relaxation processes. A mechanism for the formation of electrofluorochromism based on a kinetic model has been proposed [1]. In this model, the description of the optoelectronic process in a photoactive molecular junction takes into account the fact that the formation of electron current and electroluminescence (EL) is controlled not only by the shift of the orbital energies of the molecule relative to the Fermi levels of both electrodes, but also by the probability of the realization of many-body states of the molecule at different values and polarities of the bias voltage. Therefore, when current and EL are generated, the electronic states of charged forms of fluorophore molecules can act not only as mediators of electron transfer, but also become responsible for electrofluorochromism. It became clear that the EL in a molecular junction reflects the light emission of a fluorophore molecule not only between the singlet states of a neutral molecule, but also between the states of its charged forms. Thus, we show that electron transfer occurs through the transmission channels associated with electronic states of the neutral molecule and its cationic and anionic forms, which, at a definite bias voltages, are involved in electron transfer. The occupancies of these states are determined by kinetic processes in the molecular junction and therefore depend on the ratio of charge exchange rates between the molecule and the electrodes, the rates of non-radiative intramolecular transitions caused by inelastic interelectrode tunneling of electrons, as well as the rates of intramolecular radiative transitions enhanced by the plasmonic response. Analytical results are obtained using the tight-binding Hamiltonian for a molecule. The kinetic model made it possible to explain the features of EL in a monomolecular junction with the ZnPc fluorophore. Thus, it was shown that the description of EL based on the kinetic approach can serve as an effective tool for understanding the physics of optoelectronic processes in single-molecule structures.

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Session Classification: Morning Session 3

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 58

Type: **Poster**

Spin-boson description of the temporal behavior of the dynamical system with time-dependent coupling to the environment

Tuesday, 24 September 2024 16:35 (5 minutes)

This work shows how a kinetic process is formed in a dynamic system that is in a non-stationary coupling with the environment. It is assumed that the environment has a large number of degrees of freedom and therefore transitions in a dynamic system do not change the state of the environment. However, due to the openness of a dynamic system, the environment is capable of modifying both the states of the system and its energy levels. We are considering a quantum dynamic system, where the exchange of energy between the system and the environment is carried out through vibrational quanta (phonons). Using the method of nonequilibrium statistical mechanics, kinetic equations are obtained that describe the time evolution of the density matrix of a dynamic system under conditions of strong (polaron) coupling with vibrational modes of both the environment and the system. The difference from a similar type of research is that the coupling between the electronic states of the system and its vibration states is assumed to be time-dependent. We proposed a unitary-transformation, which made it possible to take into account this non-stationary coupling directly in the operator responsible for transitions between states of the system. This opened up the possibility of using the perturbation method to derive the master equation for the probabilities of occupying system states. As an example of the application of non-stationary polaron transformation, the kinetics of establishing the probabilities of occupation of electronic states of an open TLS is considered.

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Session Classification: Poster Session

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 60

Type: Oral

Domains and domain boundaries structure of benzene adsorbed on graphene

Wednesday, 25 September 2024 12:50 (20 minutes)

In our report, we review the domain boundaries in the structure of benzene monolayer adsorbed on a graphene sheet. It is shown in [1] that the monolayer's structure can be complicated even for benzene, the simplest representative of the cyclic hydrocarbons. It was found in [2] that there exist two different energy states of the adsorbed benzene molecule: 1) the symmetric (hollow) unstable state, where the benzene molecule is placed right over the graphene hexagon; 2) the non-symmetric (stacked) stable configuration, where the benzene molecule's center is placed above one of graphene atoms. The low-symmetry structure is characterized by the presence of six domains, known as star domains. The representatives of these domains at the graphene hexagonal layer are star vectors that describe transitions from symmetric high energy state into the stable low symmetric position.

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Session Classification: Poster Session

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 62

Type: **Poster**

Nonequilibrium protection effect and spatial localization of noise-induced fluctuations: gas flow scattering on partially penetrable obstacle

Tuesday, 24 September 2024 16:40 (5 minutes)

The scattering of gas flow on an obstacle can lead to the formation of nonequilibrium steady states (NESS), such as stationary obstacle wakes. These systems may undergo nonequilibrium phase transitions, resulting in the emergence of nonlinear steady-state gas structures under critical conditions. One notable example is the formation of a stratum-like, or two-domain, gas structure ahead of the obstacle due to the blockade effect in the gas [1-5]. This structure can be interpreted as the growth of a dense gas phase nucleus near the obstacle, which acts as a nucleation center.

In our study, we focus on a quasi-one-dimensional driven lattice gas doped with static impurities within a narrow channel with ring topology [1]. The obstacle is modeled as a transverse channel cell partially occupied by impurity particles, and the system is driven by a nonconservative field. We utilize a combination of the local equilibrium approach and mean-field approximation to describe the NESSs and gas fluctuations near them.

Our findings reveal that this nonequilibrium transition is associated with the emergence of a local invariant. Specifically, the state of the obstacle behaves as a local first integral (or adiabatic invariant), becoming insensitive to fluctuations in the gas and the external driving noise.

Below the transition, the gas flow is scattered by the impurity, the structural defect of the lattice. Above the transition, the gas flow is scattered by the gas domain wall, the defect of the gas density distribution. This leads to the protection effect of the obstacle state against gas fluctuations, manifesting as a strong localization of fluctuations near the topological defect (domain wall) and their complete suppression at the obstacle. Additionally, gas fluctuations demonstrate strong anti-correlated behavior at the left and right sides of the impurity. These effects are similar to the skin effect and edge-edge correlation effect in non-Hermitian systems [6].

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Session Classification: Poster Session

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 63

Type: Oral

Stimulating excitable membrane of ORN with stochastic Markov process

Thursday, 26 September 2024 11:20 (20 minutes)

Excitable membrane of olfactory receptor neuron (ORN) is populated with up to several millions of identical receptor proteins (R) able to bind / release odor (O) molecules. The affinity of R to O depends on the odor presented, and this is the initial mechanism which is required for the olfactory selectivity to exist.

Figure 1: Simplified R structure. Modified from [3].

The affinity of R to O depends on the odor presented, and this is the very first step the olfactory selectivity builds up. Recently, [1], it was shown for a so called membrane-less ORN model that its selectivity can be much better than that of its R. A more realistic ORN model should include an excitable membrane with its electric transients. This introduces time parameter into the ORN's response to stimulation. The latter renders inappropriate used in [1] reasoning in terms of binomial distribution, and necessitates consideration of temporal properties of O binding-releasing and the membrane charging-discharging-firing.

In this contribution, we develop an approach in which the number of R bound with O $n(t)$, is modeled as a Markov stochastic process. With each bound R, as it is observed for insects [2], Fig. 1, we associate an open channel having conductance 0.015 nS, which injects a depolarizing current through the membrane.

The further membrane evolution is governed by the leaky integrate-and-fire neuronal model, see Eq. (1).

$$c_M \frac{dV(t)}{dt} = -g_l(V(t) - V_{rest}) - n(t)g_R(V(t) - V_e),$$

where $V(t)$ – is the membrane voltage; V_{rest} – is the resting voltage;

c_M – is the total capacity of ORN's membrane;

g_l – is the total leakage through it;

V_e – is the reversal potential for current through open R;

$n(t)$ – is the fluctuating number of open channels at moment t due to odor molecules bound with R;

g_R – is the conductance of a single open channel.

A fast, very efficient method is developed for generating stochastic trajectories $n(t)$ and solving Eq. (1) numerically, see Fig. 2. The first, introductory simulations based on this method, [4], support the conclusion made in [1] and before, that ORN's selectivity can be much better than that of its receptors R, provided that odors are presented in low concentrations.

Figure 2: An example of realization of stochastic process $n(t)$ and corresponding membrane voltage, with three spikes emitted. Here, the total number of R per the ORN is $N = 2.5 \cdot 10^6$

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Session Classification: Morning Session 3

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Asymptotic behaviour of solutions of the differential equation of the form $y^{(4)} = \alpha_0 p(t) \varphi(y)$ with rapidly varying nonlinearity in the case of $\lambda_0 = 1$.

1. Introduction.

In this paper we study the asymptotic behaviour of solutions of a fourth order differential equation of the form $y^{(4)} = \alpha_0 p(t) \varphi(y)$ (1). The purpose of this paper is to obtain the asymptotics $P_\omega(Y_0, \lambda_0)$ solutions of the differential equation (1) for the special case when $\lambda_0 = 1$.

2. Object of research.

Consider a differential equation of the form (1) where $\alpha_0 \in \{-1, 1\}$, $p : [a, \omega[\rightarrow]0, +\infty[$ is a continuous function, $-\infty < a < \omega \leq +\infty$, $\varphi : \Delta_{Y_0} \rightarrow]0, +\infty[$ is a twice continuously differentiable function such that $\varphi'(y) \neq 0$ where $y \in \Delta_{Y_0}$, $\lim_{y \in \Delta_{Y_0}} \varphi(y) = \begin{cases} \text{or } 0, \\ \text{or } +\infty, \end{cases} \lim_{y \in \Delta_{Y_0}} \frac{\varphi(y) \varphi''(y)}{\varphi'^2(y)} =$

$$1,$$

Y_0 is equal to either 0, or $\pm\infty$, Δ_{Y_0} is a one-sided neighbourhood of Y_0 .

3. Basic definitions and notations.

The solution y of the differential equation (1) is called $P_\omega(Y_0, \lambda_0)$ -solution, where $-\infty \leq \lambda_0 \leq +\infty$, if it is defined on the segment $[t_0, \omega[\subset [a, \omega[$ and satisfies the following conditions $y(t) \in \Delta_{Y_0}$ at $t \in [t_0, \omega[$, $\lim_{t \uparrow \omega} y(t) = Y_0$,

$$\lim_{t \uparrow \omega} y^{(k)}(t) = \begin{cases} \text{or } 0, \\ \text{or } \pm\infty, \end{cases} (k = 1, 2, 3), \quad \lim_{t \uparrow \omega} \frac{[y^{(3)}(t)]^2}{y^{(2)}(t)y^{(4)}(t)} = \lambda_0.$$

Let us introduce additional auxiliary notations

$$J_0(t) = \int_{A_0}^t p_0^{\frac{1}{4}}(\tau) d\tau, \quad q(t) = \frac{(\Phi^{-1}(\alpha_0 J_0(t)))'}{\alpha_0 J_3(t)}, \quad H(t) = \frac{\Phi^{-1}(\alpha_0 J_0(t)) \varphi'(\Phi^{-1}(\alpha_0 J_0(t)))}{\varphi(\Phi^{-1}(\alpha_0 J_0(t)))},$$

$J_1(t) = \int_{A_1}^t p_0(\tau) \varphi(\Phi^{-1}(\alpha_0 J_0(\tau))) d\tau$, $J_2(t) = \int_{A_2}^t J_1(\tau) d\tau$, $J_3(t) = \int_{A_3}^t J_2(\tau) d\tau$, where the integration boundary A_i is either ω or constant and is defined so that the integral tends either to 0 or to $\pm\infty$.

4. Main results.

The following two theorems are valid for equation (1).

Theorem 1. For the existence $P_\omega(Y_0, 1)$ -solutions of differential equation (1) that the inequalities $\alpha_0 \nu_2 > 0$, $\alpha_0 \mu_0 J_0(t) < 0$, at, $t \in]a, \omega[$, $\alpha_0 \nu_0 < 0$, or, $Y_0 = 0$, $\alpha_0 \nu_0 > 0$, or, $Y_0 = \pm\infty$ (2),

and conditions $\frac{\alpha_0 J_3(t)}{\Phi^{-1}(\alpha_0 J_0(t))} \sim \frac{J_1'(t)}{J_1(t)} \sim \frac{J_2'(t)}{J_2(t)} \sim \frac{J_3'(t)}{J_3(t)} \sim \frac{(\Phi^{-1}(\alpha_0 J_0(t)))'}{\Phi^{-1}(\alpha_0 J_0(t))}$ at $t \uparrow \omega$, $\alpha_0 \lim_{t \uparrow \omega} J_0(t) = Z_0$,

$\lim_{t \uparrow \omega} \frac{\pi_\omega(t) (\Phi^{-1}(\alpha_0 J_0(t)))'}{\Phi^{-1}(\alpha_0 J_0(t))} = \pm\infty$, $\lim_{t \uparrow \omega} \frac{\pi_\omega(t) J_0'(t)}{J_0(t)} = \pm\infty$ (3). Moreover, for each such solution, the asymptotic representations at $y(t) = \Phi^{-1}(\alpha_0 J_0(t)) \left[1 + \frac{o(1)}{H(t)} \right]$, $y'(t) = \alpha_0 J_3(t) [1 + o(1)]$,

$$y''(t) = \alpha_0 J_2(t) [1 + o(1)], \quad y'''(t) = \alpha_0 J_1(t) [1 + o(1)] \quad (4).$$

Theorem 2. Let $p_0 : [a, \omega[\rightarrow]0, +\infty[$ is a continuously differentiable function and along with the

(2) - (3) conditions $\lim_{t \uparrow \omega} \frac{q'(t) J_2(t) |H(t)|^{\frac{1}{4}}}{J_2'(t)} = 0$, $\lim_{y \in \Delta_{Y_0}} \frac{\left(\frac{\varphi'(y)}{\varphi(y)} \right)' \left| \frac{y \varphi'(y)}{\varphi(y)} \right|^{\frac{3}{4}}}{\left(\frac{\varphi'(y)}{\varphi(y)} \right)^2 \left| \frac{\varphi'(y)}{\varphi(y)} \right|} = 0$ then the dif-

ferential equation (1) contains at $\alpha_0 \mu_0 = -1$ a two-parameter family of $P_\omega(Y_0, 1)$ -solutions which admit at $t \uparrow \omega$ asymptotic representations (4) and furthermore such first, second and third order derivatives of which satisfy at $t \uparrow \omega$ the asymptotic relations $y'(t) = \alpha_0 J_3(t) \left[1 + \right.$

$\frac{o(1)}{|H(t)|^{\frac{3}{4}}}$], $y''(t) = \alpha_0 J_2(t) \left[1 + \frac{o(1)}{|H(t)|^{\frac{1}{2}}} \right]$, $y'''(t) = \alpha_0 J_1(t) \left[1 + \frac{o(1)}{|H(t)|^{\frac{1}{4}}} \right]$. The question of whether the differential equation (1) has $P_\omega(Y_0, \lambda_0)$ - solutions admitting at $t \uparrow \omega$ asymptotic representations (4) in the case when $\alpha_0 \mu_0 = 1$ is still open.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 65

Type: Poster

Solving Classical Systems of Linear Equations with the Help of Non-Classical Gradient and Classical Algebraic Methods

Since the beginning of time, before to start implementation of some ideas that people had planned earlier, they have made some optimal, more or less, decision. Initially this decision was made without any special analysis, it was based only on pure human experience. But over time it was no longer possible to realize this action without special mathematical methods that carry out global search for necessary optimum. Nowadays, in crazy time of active computerization, these methods allow us to take, in fact, innovative look at various complicated problems of classical mathematics.

The given paper presents basic results of analysis of classical Gauss method and new optimization method of gradient descent for solving general systems of linear algebraic equations, obtained after testing special program, written in "Visual Basic for Applications".

Gradient methods are numerical methods for solving unconditional optimization problems with the help of gradient. These methods are reduced to finding maximum or minimum of some function. An essence of our proposed numerical optimization method of gradient descent is that solving any system of linear algebraic equations of the following matrix form $A\vec{x} = \vec{b}$ is reduced to searching of minimizer \vec{x}^* , i.e. such vector, that $\min_{\vec{x} \in \mathbb{R}^n} f(\vec{x}) = f(\vec{x}^*)$, for the next residual function

$$f(\vec{x}) = (A\vec{x} - \vec{b}, A\vec{x} - \vec{b}) = \|A\vec{x} - \vec{b}\|^2, A = \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \dots & \dots & \dots & \dots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} \in \mathbb{R}^{m \times n}, \vec{b} = \begin{pmatrix} b_1 \\ b_2 \\ \dots \\ b_m \end{pmatrix} \in \mathbb{R}^m, m \leq n.$$

Formally, the method consists in iterative generation of some sequence of such points $\{\vec{x}_k\}_{k \geq 0}$ (i.e. some descent trajectory, that is sometimes called a *relaxation trajectory*, that converges to our real solution \vec{x}^* while $k \rightarrow \infty$), that $f(\vec{x}_{k+1}) \leq f(\vec{x}_k)$, $k \geq 0$, according to the following iterated scheme.

1. An arbitrary point is selected as an initial approximation \vec{x}_0 .
2. The point \vec{x}_{k+1} , $k \geq 0$, is determined by the formula $\vec{x}_{k+1} = \vec{x}_k - \lambda_k \cdot \text{grad}(f(\vec{x}_k))$, $\lambda_k > 0$, $k \geq 0$.

At each step we have movement along the vector of anti-gradient $-\text{grad}(f(\vec{x}_k))$, $k \geq 0$, in the direction of the fastest decrease of f , and, as a result, we get our necessary solution. Namely, if it turns out that modulus of our anti-gradient is zero (more precisely, less than predetermined accuracy), then we are at the minimum point we are looking for. If the criterion for the end of the iteration is not true (modulus of our anti-gradient is more than predetermined accuracy), then we return to the first step, otherwise we return the exact value of \vec{x}_{k+1} , $k \geq 0$. In this formula λ_k , $k \geq 0$, determines the distance between \vec{x}_k and \vec{x}_{k+1} , $k \geq 0$.

The main problem in the process of choosing this step λ_k , $k \geq 0$, is to ensure that the rule $f(\vec{x}_{k+1}) \leq f(\vec{x}_k)$, $k \geq 0$, is true. There are different ways to choose this step multiplier λ_k , $k \geq 0$. Depending on this, different variants of numerical optimization method of gradient descent can be obtained. We have considered the next four methods: the method with adaptive step selection, the method with adaptive step correction, the modified descent method with adaptive step selection, and the fastest descent method. All these methods contribute to the accelerated approximation of our converging sequence $\{\vec{x}_k\}_{k \geq 0}$ to necessary real solution \vec{x}^* we are looking for.

The result of classical Gauss method is some conclusion about solvability or unsolvability of our system under consideration, based on application of the Kronecker-Capelli theorem from classical

algebra to the reduced system. The result of the optimization part of the program is necessary solution, found by proposed gradient descent method, our method running time, as well as accuracy of calculations.

A comparative analysis of these methods has been carried out when the program has been testing different systems of linear algebraic equations. The Gaussian method algorithm gives results in a fraction of seconds, while the optimization method produces the most accurate result in a short time not for every system. For some systems the program just starts to loop. This is an experimental proof that effectiveness of our descent method depends on exact value of its step: in optimal area significant "yawings" may occur due to need to correct the step value of the descent method.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 67

Type: **Poster**

Influence of the unit cell size of periodic electromagnetic metamaterials on their optical properties

Tuesday, 24 September 2024 17:55 (5 minutes)

To date, the most of metamaterials used in diverse applications (from nanooptics and plasmonics to mobile communication and biophysics) are periodic structures consisting of spatially arranged inclusions. In the theory of metamaterials, they are treated as homogeneous media, if their unit cell size d (the lattice constant) is much smaller than the wavelength λ of the incident electromagnetic wave the metamaterials operate with, $d \ll \lambda$. A number of homogenization theories have been proposed to calculate metamaterial's effective parameters, such as the effective permittivity ϵ_{eff} , permeability μ_{eff} , and index of refraction n_{eff} , based on the geometry and material parameters of the metamaterial's inclusions. In practice, however, condition $d \ll \lambda$, or, equivalently, $d/\lambda \ll 1$, is not always met.

In the present work, the properties of metamaterials are analyzed in a wider range of their relative unit cell size d/λ values for several types of the metamaterials' inclusions of practical interest. The optical reflectance R and transmittance T of the metamaterials are numerically calculated based on the Lorentz volumetric averaging of the local electric and magnetic fields inside the unit cells, rather than using recent metamaterials homogenization theories proposed in the last two decades.

It is shown that behavior of the optical properties of metamaterials declines more and more from what is expected based on the homogenization concept, as the relative unit cell size increases from small values $d/\lambda \ll 1$ (the quasistatic regime) to the unity (the intermediate operating regime). In the latter regime, a crucial role in the optical properties formation play the diffraction and interference effects in the metamaterials, and the properties exhibit an oscillating behavior which cannot be predicted within the homogenization concept.

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Session Classification: Poster Session

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 68

Type: Oral

Optimization of Parameters of Input Pulses for Passive Photonic-Crystal-Based Electromagnetic Energy Compressors

Electromagnetic (EM) energy compression is a process of converting long-duration low-amplitude input pulses into much shorter output pulses with significantly higher amplitude. There are two primary approaches to this: active and passive compression [1]. Active compressors accumulate the input in resonant cavities over a relatively long accumulation stage, followed by a rapid release of the accumulated energy as a very short, high-power output pulse [2]. Passive compression, which is the focus of this study, occurs when an input pulse increases in amplitude and decreases in duration as it travels through a waveguide with specific geometric and/or material properties [3]. This is achieved by exploiting the dispersion of waveguides, which causes different frequency components to propagate with different velocities, and by tuning the frequency modulation of an input pulse so that these components arrive synchronously at the output. EM energy compressors are used in particle accelerators, radars, data transmission, energy transfer, plasma heating, biophysical applications, EM launch systems, essentially, in any field that requires high-power electromagnetic pulses (EMP).

Accurately computing the time signature of input pulses is crucial for the efficient passive compression of EMP. In this work, we employ the time reversal method (TRM) for these computations. TRM is based on the possibility to change the sign of the time variable in the Maxwell's equations, enabling the reconstruction of a pulse's evolution up to its arrival at the output with a set-in-advance temporal profile, regardless of the type of dispersion elements used [4]. In this work, we detail the specific aspects of TRM application and address the optimization of the excitation pulse's parameters through the linearization of its frequency modulation.

A 2D photonic crystal with a waveguiding defect is considered as a test-bed dispersive waveguide. The absence of metal components (the crystal is constructed of sapphire rods) makes it particularly inviting for compressing microwave pulses.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 69

Type: Oral

Spectral Theory Approach to the Analysis of Diffraction Radiation Generated on a Metal-Backed Graphene Layer with Periodic Interface

Graphene stays in the spotlight for its exceptional properties and versatile applications, one of which is the development of flexible metamaterials. Its ability to integrate seamlessly with other components and adapt to nonplanar structures makes graphene a key material in advancing innovative flexible meta devices and functional metasurfaces [1]. This motivates us to focus on the interaction of the electromagnetic field with a graphene layer that has a periodic interface, with the ultimate goal of controlling the resonance properties of the structure electromagnetically. A periodic boundary at the graphene layer's external interface plays a crucial role in shaping the scattered field, which consists of an infinite set of spatial harmonics and exhibits complex resonance properties that could be exploited [2, 3].

The interaction of the electromagnetic field with a graphene layer is modeled (in the approximation of a given current) as a two-dimensional problem of diffraction of a plane monochromatic electromagnetic wave on the structure of interest. Employing the analytical regularization method (based on the modified C-method) and tools from the scattering matrix technique [3, 4], the original boundary value problem is transformed into an infinite system of linear algebraic equations with respect to the amplitudes of the spatial harmonics of the diffraction field. This method performs the analytical continuation of the solution of the diffraction problem into the domain of complex parameter values. Such an approach enables the unambiguous association of the resonant behavior of diffraction radiation with the excitation of natural oscillations of the periodic structure, which functions as an open resonator in this scenario. It has been established that the main mechanism underlying this behavior is the so-called synchronism of the phase velocities of the eigenwaves propagating along the structure and the phase velocities of the spatial harmonics of the diffraction field [2].

In this work, we detail the application of the aforementioned approach to the graphene structures of interest, present and discuss a set of detected resonances and the means to control them electromagnetically.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 70

Type: **Oral**

Extended symmetry analysis of (1+2)-dimensional fine Kolmogorov backward equation

Following [1], we discuss advances in the classical group analysis of the Kolmogorov backward equation with quadratic diffusivity

$$(1) \quad u_t + xu_y = x^2 u_{xx}.$$

This equation belongs to the class of (1+2)-dimensional ultraparabolic linear equations denoted by $\bar{\mathcal{F}}$ in [1] and is distinguished within this class $\bar{\mathcal{F}}$ by its excellent symmetry properties. More specifically, modulo the point equivalence, it is a unique equation in the class $\bar{\mathcal{F}}$ whose essential Lie invariance algebra is five-dimensional and nonsolvable.

We compute the point symmetry pseudogroup of the equation (1) using the advanced version of the direct method and analyze its structure. In particular, we single out the essential subgroup of this pseudogroup and identify its independent discrete elements, which are two involutions alternating the signs of the space and dependent variables, respectively. We exhaustively classify all subalgebras of the corresponding essential Lie invariance algebra up to inner automorphisms and up to the action of the essential point-symmetry group. This allowed us to classify Lie reductions and Lie invariant solutions of the equation (1). We also discuss the generation of its solutions using point and linear generalized symmetries and carry out its peculiar generalized reductions. Consequently, we construct wide families of its solutions parameterized by an arbitrary finite number of arbitrary solutions of the (1+1)-dimensional linear heat equation or one or two arbitrary solutions of (1+1)-dimensional linear heat equations with inverse square potentials.

[1] Koval S.D. and Popovych R.O., Extended symmetry analysis of (1+2)-dimensional fine Kolmogorov backward equation, *Stud. Appl. Math.* **153** (2024), e12695, arXiv:2402.08822.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 71

Type: **Oral**

On controllability problems for the heat equation controlled by the Dirichlet boundary condition

Consider the following control system:

$$w_t = w_{xx}, x \in (0, +\infty), t \in (0, T),$$

$$w(0, \cdot) = u, t \in (0, T),$$

$$w(\cdot, 0) = w^0, x \in (0, +\infty),$$

where $T > 0$ is a constant, w^0 is a given function, $u \in L^\infty(0, T)$ is a control. The control system is considered in Sobolev spaces.

An initial state w^0 of control system (1)-(3) is said to be null-controllable in a given time $T > 0$ if we can find a control $u \in L^\infty(0, T)$ such that the state of the solution to the control system at $t = T$ satisfies the condition $w(\cdot, T) = 0$. An initial state w^0 of control system (1)-(3) is said to be approximately controllable to a target state w^T in a given time $T > 0$ if for each neighbourhood of a target state w^T there exists a control $u \in L^\infty(0, T)$ such that the end state of the solution to the control system (at $t = T$) belongs to this neighbourhood of w^T .

We prove that any initial state of the control system (except the zero one) is not null-controllable in a given time $T > 0$.

We also prove that each initial state of the control system is approximately controllable to any target state in a given time $T > 0$.

The results are illustrated by examples.

The results on controllability of the heat equation controlled by the Dirichlet boundary condition was published in [1-3].

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- [3] L. Fardigola and K. Khalina, Controllability problems for the heat equation in a half-plane controlled by the Dirichlet boundary condition with a point-wise control, *J. Math. Phys. Anal. Geom.* 18 (2022), 75-104.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 72

Type: **Oral**

Kontsevich graph γ_3 -flow of Nambu-Poisson brackets: triviality established in 2D, 3D, and now, in 4D

Kontsevich constructed a map from suitable cocycles in the graph complex to infinitesimal deformations of Poisson bivectors. Are such deformations trivial, meaning, do they amount to a change of coordinates along a vector field? We examine this question for Nambu-Poisson brackets deformed by the tetrahedron γ_3 , the smallest nontrivial graph cocycle in the Kontsevich graph complex.

We use Kontsevich's graph calculus, in which directed graphs encode differential formulas on \mathbb{R}^d . In particular, we use dimension-specific micro-graphs, in which each vertex represents an element of the Nambu-Poisson bracket.

The (non)trivialisation problem gives us a sequence of overdetermined inhomogeneous linear algebraic systems on the coefficients of micro-graphs over \mathbb{R}^d , for $d \geq 2$. We use the SageMath package *gcaops* for computations. For a chosen good graph, namely the tetrahedron γ_3 , Kontsevich knew that the linear system is solvable for $d = 2$ (1996). In 2020, Buring and Kiselev proved that the linear system is solvable for $d = 3$. Building on these discoveries, we now establish that for the γ_3 -flow, the linear system is solvable for $d = 4$.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 73

Type: **Oral**

Squeezing and amplification in open quantum systems with color centers using the multilevel Janes-Cummings model

Wednesday, 25 September 2024 12:30 (20 minutes)

The ability to couple cavity-confined microwave modes to diamond slabs or films containing large numbers of color centers opens up potential new methods for noise reduction, processing, and even generating quantum states of microwaves. The unique feature of various diamond color centers is that they can be prepared in their ground states by illuminating them with light in the optical band. The color centers then become a very low noise (effectively very low temperature) system for processing and manipulating microwaves.

Ensembles of few-level emitters are able to generate nonlinearities for electromagnetic fields. Often, this is done by arranging the level structure and driving to simultaneously induce the electromagnetically induced transparency to eliminate most of the absorption that can accompany nonlinearities due to the decay of the emitter energy levels. For color centers, the lowest lying spin levels, e.g., three levels for nitrogen-vacancy (NV) centers, have very long lifetimes, so this is not a significant issue. Ensembles of emitters will also generate nonlinearities for single modes, but the produced nonlinearities are limited to the maximal ones that can be generated by single emitters. Essentially, for the purpose of generating nonlinearities, having an ensemble effectively increases the coupling rate: if the coupling of each emitter is g_0 , then an ensemble with N emitters acts as a single emitter with a coupling rate $g = \sqrt{N}g_0$, which is valid for the off-resonant generation of nonlinearities.

An ensemble of two-level emitters off-resonant with a single mode generates a series of nonlinearities with effective Hamiltonians given by powers of the mode energy operator $a^\dagger a$. The first term in this series generates a frequency shift for the cavity mode proportional to g^2/Δ , where Δ is a detuning between the NV-centers and the cavity mode. Modulating the frequency of a mode induces parametric amplification.

In this study we investigate the optimal modes of operation of a N -level atomic system interacting with the cavity mode to obtain squeezed states and amplification of the electromagnetic cavity mode signal. This is performed in the framework of the Janes-Cummings model for the N -level atomic system within the rotating wave approximation. For this purpose, perturbation theory, namely the Magnus expansion for the evolution operator, up to and including second order of smallness, was used.

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Session Classification: Morning Session 2

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 74

Type: Oral

IDENTIFICATION OF UNKNOWN PARAMETERS OF A FULLY CONTROLLED NOISY GYROSCOPIC SYSTEM

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IDENTIFICATION OF UNKNOWN PARAMETERS OF A FULLY CONTROLLED NOISY GYROSCOPIC SYSTEM

The work is devoted to the identification of unknown parameters of a fully controlled gyroscopic object with noise at the input and in the system. Such gyroscopic objects are described by the following system of equations

$$\begin{aligned} &= (A_0 + \varepsilon A_1)x + \varepsilon Bu + v, \quad (1) \\ &y = Cx + f, \end{aligned}$$

where $x \in \mathfrak{R}_{2n}$ – dimensional state vector, $A_0 = -A_0^T \in \mathfrak{R}_{2n \times 2n}$ – skew-symmetric non-degenerate matrix, $A_1 \in \mathfrak{R}_{2n \times 2n}$ – disturbance matrix, $u \in \mathfrak{R}_m$ – control vector, $B \in \mathfrak{R}_{2n \times m}$ – control matrix, $\varepsilon > 0$ – small parameter, $y \in \mathfrak{R}_l$ – observation vector, $C \in \mathfrak{R}_{l \times 2n}$, $v \in \mathfrak{R}_{2n}$ – noise in the system, which is not measured, $f \in \mathfrak{R}_l$ – noise in observations. The elements of matrices A_0 , A_1 , B and C are all or partially unknown.

Gyroscopic objects have a special structure, this structure is defined by a matrix - which is a skew-symmetric non-degenerate matrix. Since the state vector has a size of $2n$, the author used the invariant immersion method to restore A_0 , A_1 , B and C [1]. As it was mentioned, the appearance of the gyroscopic system (1) is determined by the matrix A_0 , this made it possible to develop and significantly simplify the algorithm of the invariant immersion method in comparison with the general case.

These algorithms have been improved to restore unknown matrices of system (1). Algorithms are given in the work, which in an analytical form make it possible to obtain unknown parameters of the system (1). Solving such a problem makes it possible to apply previously developed analytical methods of optimal control and monitoring, in particular [2], [3] to system (1). This approach made it possible to manage and restore the state vector of system (1) when the matrices A_0 , A_1 , B and C are all or partially unknown.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 75

Type: **Oral**

Equivalence method for the construction of exact solutions of generalized Korteweg-de Vries equations

The transformational properties of two classes of generalized Korteweg-de Vries (KdV) equations with coefficients dependent on the time variable are investigated, and the effectiveness of the equivalence method for constructing exact solutions to such equations is demonstrated. Specifically, the equivalence groupoids for both classes of equations are identified, and it is proven that both classes are normalized. A criterion for the reducibility of variable-coefficient equations from the class $u_t + f(t)u^2u_x + g(t)u_{xxx} + h(t)u + p(t)u_x + k(t)uu_x + l(t) = 0$ to the standard modified Korteweg-de Vries equation is established. For the second class of equations, $u_t - 3Mg(t)uu_x + g(t)u_{xxx} + 2q(t)u + (p(t) + q(t)x)u_x = 0$, full similarity to the classical Korteweg-de Vries equation is demonstrated. It is shown that the equivalence method for finding exact solutions is more effective for these classes of equations compared to methods used by other authors previously. Consequently, formulas for generating exact solutions of generalized Korteweg-de Vries equations with variable coefficients are derived, and examples of constructing exact solutions using these formulas are provided.

The talk is based on the work:

Vaneeva, O., Brahinets, O., Zhalij, O., & Magda, O. (2023). EXACT SOLUTIONS OF GENERALIZED KORTEWEG-DE VRIES EQUATIONS WITH VARIABLE COEFFICIENTS. Reports of the National Academy of Sciences of Ukraine, (6), 3–11. <https://doi.org/10.15407/dopovidi2023.06.003>

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 76

Type: **Oral**

Generalized symmetries of Burgers equation

Despite the number of relevant considerations in the literature, the algebra of generalized symmetries of the Burgers equation has not been exhaustively described.

We fill this gap, presenting a basis of this algebra in an explicit form and proving that the two well-known recursion operators of the Burgers equation and two seed generalized symmetries, which are evolution forms of its Lie symmetries, suffice to generate this algebra. The core of the proof is essentially simplified by using the original technique of choosing special coordinates in the associated jet space.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 77

Type: **Poster**

Polaronic model of the Giant Dielectric and Pyroelectric Responses of Ferroelectric Fine-Grained Ceramics

Tuesday, 24 September 2024 17:10 (5 minutes)

We described the anomalous temperature behavior of the giant dielectric response and losses using the core-shell model for ceramic grains and modified Maxwell-Wagner approach. We assume that core shells and grain boundaries, which contain high concentration of space charge carriers due to the presence of graphite inclusions in the inter-grain space, can effectively screen weakly conductive ferroelectric grain cores.

We considered several possible mechanisms, which can lead to the giant values of the relative dielectric permittivity accompanied by the very high values of dielectric losses in the strongly inhomogeneous ferroelectric-semiconducting ceramics.

The first mechanism is the effect of “geometric” capacitance, which could appear in the highly porous mixtures of the insulating and conducting inclusions. In this case the effective surface area of the capacitor could be much larger than the electrodes area, and the effective area could accumulate the space charge. Note that the geometric capacitance effect contribution could be verified by measuring the capacitance of the ceramic samples of different cutting angles, thickness, electrode area, frequency, and temperature.

The second mechanism is the Maxwell-Wagner effect [1], which could lead to the apparent enhancement of the dielectric response in the dielectric-semiconducting mixture in the presence of insulating polar grains, screening shells and conductive graphite inclusions. In principle all conductivity effects in the inhomogeneous media are strongly inter-wined and closely related with possible electric percolation effects. The possible roles and relative contributions of the different conductivity effects were considered with the help of the different theoretical models.

According to the effective media model proposed by Liu et al. [2], the one can consider two (or more) layers representing all grain cores, their screening shells and grain boundaries, graphite inclusions and inter-grain space in the Maxwell-Wagner approach. One of the “effective” layers corresponds to weakly-conductive grain cores, and the other corresponds to all stronger conductive regions (such as screening shells, grain boundaries and/or inter-grain space). The layers are characterized by the effective dielectric permittivity and conductivity for grain cores, grain boundaries and/or inter-grains. These effective parameters are temperature and/or frequency dependent.

The superparaelectric-like state with a giant dielectric response can appear in the paraelectric shells and inter-grain space due to the step-like thermal activation of localized polarons in the spatial regions, being in agreement with experimentally observed frequency-dependent transition of the electro-transport mechanism [3]. Obtained results can be the key for the description of complex electrophysical properties inherent to the strongly inhomogeneous media with electrically coupled insulating ferroelectric nanoregions and semiconducting superparaelectric-like regions.

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Session Classification: Poster Session

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 78

Type: Oral

Modeling temperature dynamics in non-uniform biological tissues under cryogenic impact

Wednesday, 25 September 2024 13:10 (20 minutes)

Physical and mathematical modeling is widely used to simulate cryoapplication processes. Mathematical modeling of this process [1,2] allows us to predict the temperature field of the frozen region. This makes it possible to determine the cryo-application time sufficient to destroy target cells and minimize damage to healthy cells under various experimental conditions. Moreover, simulation also predicts the depth of the cryoapplication impact, which can be difficult to measure in some situations in the living tissues. Then, we use temperature-dependent thermodynamical parameters of biological tissues to compare simulation with thermal imaging.

The problem with moving phase boundary is known as the Stefan problem. There are several ways to numerically solve that problem. One of them is gradually changing thermodynamic parameters close to the phase change boundary. This approach is effectively describing the freezing dynamics of a biological tissues. The appearance of solutes in water leads to change the freezing temperature in a range of temperatures around (-10C..-0.1C) due to change of solute concentration. By combining the usual thermal capacity with latent heat, we can define an effective thermal capacity. That allows us to solve the heat equation in 2D cylindrical geometry, see Fig. 1.

Generally thermodynamic properties of the biological tissues are highly dependent on temperature, so we have a non-uniform heat equation $\frac{\partial T}{\partial t} = \frac{1}{\rho C_p} \nabla k \nabla T$. To solve this equation numerically, we use the finite differences method on a rectangular mesh to calculate the thermal balance of each node. Then we compare our results with thermal imaging of cryoapplication impact on rat skin [3].

Fig. 1. (a) Principal scheme of the cryo-application problem for 2D cylindrical geometry with radial symmetry, where there is the cryo-applicator with a temperature of liquid Nitrogen pressed 1-2mm inside the soft tissues. (b) Dynamics of the maximum radius and depth of the ice spot for several isotherms. Typically consists of 4 phases, I-freezing, II-thawing thin layer of ice around the main ice spot, III-usual thawing, IV-finish thawing.

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Session Classification: Morning Session 2

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 80

Type: **Oral**

Discrete symmetries of differential equations

Discrete symmetries of differential equations are not so well studied objects as continuous ones. We discuss the notion of discrete symmetries and the methods of their computation. Then we analyze common errors in such computations and show connection of these errors with those in solving other problems of classical group analysis of differential equations, including the classification of Lie reductions and the construction of Lie-invariant solutions.

The main illustrative example is given by the (1+1)-dimensional linear heat equation. We derive a nice representation for its point symmetry transformations and properly interpret them. This allows us to prove that the pseudogroup of these transformations has exactly two connected components. That is, the heat equation admits a single independent discrete symmetry, which can be chosen to be alternating the sign of the dependent variable. We introduce the notion of pseudo-discrete elements of a Lie group and show that alternating the sign of the space variable, which was for a long time misinterpreted as a discrete symmetry of the heat equation, is in fact a pseudo-discrete element of its essential point symmetry group. As a result, the classification of subalgebras of the essential Lie invariance algebra of the heat equation is enhanced.

The developed approach to point-symmetry groups whose elements have components that are linear fractional in some variables can directly be extended to many other linear and nonlinear differential equations. We also consider the Burgers equation because of its relation to the heat equation and prove that it admits no discrete point symmetries. Further examples are the Harry Dym equation and a nonlinear diffusion equation with a special power diffusion coefficient.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 82

Type: **Poster**

On the solution of the problem of the cosmological constant

Tuesday, 24 September 2024 16:10 (5 minutes)

Calculation of the vacuum energy density in quantum field theory gives a value 10^{122} times higher than the observed one, and many proposed approaches have not solved this problem and have not calculated its real value. However, the application of the microscopic theory of superconductivity to the description of the physical vacuum on the Planck scale made it possible to solve the problem of the cosmological constant and obtain a formula for the observed vacuum density or dark energy. Its numerical value is $6.09 \cdot 10^{-30} g/cm^3$, and it is in complete agreement with observations, since the experimental value is $(6.03 \pm 0.13) \cdot 10^{-30} g/cm^3$ (J. Prat, C. Hogan, C. Chang, J. Frieman, 2022).

The cosmological model with superconductivity (CMS), proposed by the author, also implies a description of the earliest stage of the Universe evolution preceding the inflation stage. It describes the formation of the inflaton field as a special condensate of primordial fermions with the Planck mass, followed by the inflationary expansion of the early Universe. The current expansion of the Universe and its evolution are described as an ongoing second-order phase transition, and the flow of physical cosmological time is a consequence of processes occurring on Planck scales. The value of the Hubble parameter $H_0 = 69.76 km \cdot s^{-1} Mpc^{-1}$ calculated in CMS corresponds to the average value for most values of this parameter obtained by different methods. CMS also describes black holes as a quantum condensate of primary fermions with Planck mass.

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Session Classification: Poster Session

Track Classification: ASTROPHYSICS AND COSMOLOGY

Contribution ID: 83

Type: **Poster**

Low temperature behavior of the heat capacity of MWCNTs with Ø9.4 nm: component of flexural dispersion for phonons

Tuesday, 24 September 2024 17:55 (5 minutes)

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Low-temperature specific heat $C(T)$ of multi-walled carbon nanotubes (MWCNTs) was studied. Two sets of modified, milled and milled-oxidized MWCNTs with an average outer diameter of 9.4 nm were used to measure specific heat in the temperature range of 1.8 to 275 K. The experimental results were compared with literature data for different carbon systems: bundles of single-walled carbon nanotubes (SWCNTs), graphite and other MWCNTs.

The initial MWCNTs were obtained by the CVD method. The length of MWCNTs and parameters of defects (number and types) in MWCNTs were changed: 1) grinding of the initial nanotubes in a ball mill; 2) the initial nanotubes were first oxidized and then milled. The figure shows low-temperature experimental heat capacity curves of ground (Sm), ground-oxidized (Sm-o) MWCNTs with outer diameters of Ø9.4 nm, as well as, for comparison, original nanotubes (Si), bundles of SWCNTs (Ø1.1 nm) and graphite. The analysis of the low-temperature behavior of the heat capacity of carbon materials below 3 K was carried out under the assumption that $C(T)$ is determined primarily by phonons with sufficiently long wavelengths (deformation waves). The specific heat $C(T)$, described by the equation $C(T) = AT + BT^3 + D^*T^5$. The coefficients A, B and D were calculated and analyzed. The decrease in the length of nanotubes and the appearance of defects as a result of both grinding and oxidation with subsequent grinding lead to an increase in heat capacity in the low-temperature region. The obtained negative D parameter indicated flexural dispersion for phonons. It was found that the magnitudes of the Debye (B) and flexural dispersive components (D) depend on the structural parameters of nanotubes: such as the diameter of individual nanotubes, the average diameter of the bundle and the size of agglomerates.

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Session Classification: Poster Session

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 84

Type: **Poster**

Asymptotic solutions of boundary value problem for singularly perturbed differential algebraic equations

This paper deals with the boundary value problem for a singularly perturbed differential algebraic system of the second order. The case of simple roots of the characteristic equation is studied. The sufficient conditions for existence and uniqueness of a solution of the boundary value problem for DAEs are found. Technique of constructing the asymptotic solutions is developed.

Primary author: САМУСЕНКО, Петро (НТУУ "КПІ імені Ігоря Сікорського")

Presenter: САМУСЕНКО, Петро (НТУУ "КПІ імені Ігоря Сікорського")

Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 85

Type: **Oral**

On a crossover between two mechanisms of sound propagation in liquids

Wednesday, 25 September 2024 10:00 (40 minutes)

Hydrodynamic theory forms the basis for our understanding of the macroscopic propagation of sound in liquids, while viscoelasticity points out solid-like elastic features at large frequencies. However, there is no understanding how the viscoelasticity manifests in the mechanism of propagation of mesoscopic and short-wavelength acoustic excitations in liquids.

We report solutions of the generalized Langevin equation for density-density time correlation functions of a liquid system in terms of dynamic eigenmodes within viscoelastic and thermo-viscoelastic dynamic models. A comparison with molecular dynamics computer simulations for supercritical Ar is performed. It is shown by analysis of extended dynamic eigenmodes in liquids how the crossover from hydrodynamic mechanism of sound propagation to elastic one takes place. Our analysis of wavenumber-dependent eigenvector components of the sound modes makes evidence that the viscoelasticity of sound excitations is originated by gradual replacement of contribution from hydrodynamic density fluctuations by non-hydrodynamic stress fluctuations. A consequence of the sound viscoelasticity for emergence of structural relaxation is shown.

Primary author: BRYK, Taras**Presenter:** BRYK, Taras**Session Classification:** Morning Session 2**Track Classification:** CONDENSED MATTER PHYSICS

Contribution ID: 86

Type: Oral

Geometric properties and exact solutions of dispersionless Nizhnik equation

The dispersionless (potential symmetric) Nizhnik equation has interesting algebraic and geometric properties. We computed the point- and contact-symmetry pseudogroups of this equation using an original megaideal-based version of the algebraic method. Note that this approach was used for the first time to find the contact-symmetry pseudogroup of a differential equation. By the same method, we also constructed the point-symmetry pseudogroups of the nonlinear Lax representation of the dispersionless Nizhnik equation and of the dispersionless counterpart of the symmetric Nizhnik system. We checked whether certain subalgebras of the maximal Lie invariance algebra \mathfrak{g} of the dispersionless Nizhnik equation and of its contact invariance algebra define point and contact transformations stabilizing these algebras. In addition, we described all the third-order partial differential equations in three independent variables that possess the algebra \mathfrak{g} as invariance algebra. We found geometric properties that single out the dispersionless Nizhnik equation from the entire set of third-order partial differential equations with three independent variables. They include the maximal Lie invariance algebra and three conservation laws with simplest characteristics.

We also classified one- and two-dimensional subalgebras of the algebra \mathfrak{g} and codimension-one and -two Lie reductions of the dispersionless Nizhnik equation. Lie and point symmetries of reduced equations were comprehensively studied, including the analysis of which of them correspond to hidden symmetries of the original equation. We constructed wide families of new exact invariant solutions of the dispersionless Nizhnik equation in closed form in terms of elementary, Lambert and hypergeometric functions as well as in parametric or implicit form. Multiplicative separation of variables was used to present an example of finding non-Lie solutions of the dispersionless Nizhnik equation that generalize invariant solutions.

1. Boyko V.M., Popovych R.O. and Vinnichenko O.O. Point- and contact-symmetry pseudogroups of dispersionless Nizhnik equation. *Commun. Nonlinear Sci. Numer. Simul.* **132** (2024), 107915, arXiv:2211.09759.
2. Vinnichenko O.O., Boyko V.M. and Popovych R.O. Lie reductions and exact solutions of dispersionless Nizhnik equation. *Anal. Math. Phys.* **14** (2024), 82, arXiv:2308.03744.

Primary authors: VINNICHENKO, Oleksandra (Institute of Mathematics of NAS of Ukraine); BOYKO, Vyacheslav (Institute of Mathematics of NAS of Ukraine); POPOVYCH, Roman (Silesian University in Opava & Institute of Mathematics of NAS of Ukraine)

Presenter: VINNICHENKO, Oleksandra (Institute of Mathematics of NAS of Ukraine)

Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 87

Type: **Oral**

On Lie symmetries of linear systems of second-order ordinary differential equations

We review our recent results on transformation properties of normal linear systems of second-order ordinary differential equations with an arbitrary number of dependent variables under several appropriate gauges of the arbitrary elements parameterizing these systems. We also present principal properties of Lie symmetries of the systems under consideration and outline ways for completely classifying these symmetries.

1. Boyko V.M., Lokaziuk O.V. and Popovych R.O., Admissible transformations and Lie symmetries of linear systems of second-order ordinary differential equations, *J. Math. Anal. Appl.* **539** (2024), 128543, 51 pp., arXiv:2105.05139.

Primary authors: BOYKO, Vyacheslav (Institute of Mathematics of NAS of Ukraine); LOKAZIUK, Oleksandra (Institute of Mathematics of NAS of Ukraine & Borys Grinchenko Kyiv Metropolitan University); POPOVYCH, Roman (Silesian University in Opava & Institute of Mathematics of NAS of Ukraine)

Presenter: BOYKO, Vyacheslav (Institute of Mathematics of NAS of Ukraine)

Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 89

Type: **Poster**

Influence of the pH of aqueous sodium chloride solutions with dissolved carbon dioxide on the temperature interval of human vital activity

Tuesday, 24 September 2024 17:45 (5 minutes)

Temporal changes in the temperature and concentration dependences of the pH value in aqueous sodium chloride solutions contacting with atmospheric carbon dioxide have been studied experimentally. The measurements are carried out in a temperature interval of (294–323) K for ion concentrations corresponding to (180–1600) water molecules per sodium or chlorine ion.

The pH value for dilute aqueous solutions of sodium chloride is a sum of two components: reducible and irreducible. The reducible component depends linearly on the temperature and, therefore, cannot be responsible for the specific details of the human and mammalian life activities. Therefore, the main parameters of the latter have to be characterized by the irreducible pH component, which is an order of magnitude smaller than the reducible component. The proportionality between the irreducible pH component value and the sodium chloride concentration may testify that minor pH changes are associated with corresponding changes in the salt composition of blood plasma that affect the state of human organism.

The pH relaxation time in aqueous NaCl solutions with dissolved atmospheric carbon dioxide and its dependence on the temperature and the ion concentration are calculated. The analysis of the obtained temperature dependences of the pH relaxation time testifies that they are similar for various concentrations of NaCl ions in water. The principle of natural selection of the optimal states of aqueous salt solutions characterized by the temperature and the irreducible component of pH has been formulated for the first time: optimal are those states in which the pH relaxation time in aqueous salt solutions is minimum.

The minimum points in the curves of the irreducible pH component for aqueous sodium chloride solutions are directly related to the temperatures that can be interpreted as the lower (approx. 30°C) and upper (approx. 42°C) limits of the temperature interval of the human and mammalian life activities. At the same time, the minimum in a vicinity of the temperature of 37°C can be interpreted as the optimal temperature for the vital activity of humans and mammals.

Since the reducible and irreducible pH components behave themselves differently, of particular importance becomes the issue concerning the conformational modifications of human serum albumin and other proteins, which depend on the pH value. The addition of proteins will change the reducible pH component, and the conformational modification of albumin will be primarily induced by the electric fields of hydrogen cations, which will directly affect the irreducible pH component.

[1] L.A. Bulavin, N.P. Malomuzh, O.V. Khorolskyi. Reducible and irreducible components of the pH value in dilute aqueous solutions of sodium chloride. *Ukrainian Journal of Physics*, 2023, 68(3), 177–183. <https://doi.org/10.15407/ujpe68.3.177>

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Session Classification: Poster Session

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 90

Type: **Poster**

Spontaneous magnetization and effective interactions in QGP at high temperature

Tuesday, 24 September 2024 16:55 (5 minutes)

In quark-gluon plasma (QGP), at higher deconfinement temperatures $T \geq T_d$ the spontaneous generation of color magnetic fields, $b^3(T), b^8(T) \neq 0$ (3, 8 are color indexes), and usual magnetic field $b(T) \neq 0$ happens. Simultaneously, the Polyakov loop and/or algebraically related to it $A_0(T)$ condensate, which is solution to Yang-Mills imaginary time equations, are also created.

Usually, in analytic quantum field theory these effects are investigated independently of each other within the effective potentials having different mathematical structures.

The common generation of these condensates was detected in lattice Monte Carlo simulations.

Recently, with the new type two-loop effective potential, which generalizes the known integral representation for the Bernoulli polynomials and takes into consideration the magnetic background, this effect has been derived analytically.

The corresponding effective potential $W(T, b^3, A_0)$ was investigated either in SU(2) gluodynamics or full QCD. The gauge fixing independence of it was proved within the Nielsen identity approach. The values of magnetic field strengths at different temperatures were calculated and the mechanism of stabilizing fields due to $A_0(T)$ condensate has been discovered. In the present review, we describe this important phenomenon in more details, as well as a number of specific effects happening due to vacuum polarization at this background. They could serve as the signals of the QGP creation in the heavy ion collision experiments.

Key words: spontaneous magnetization, high temperature, asymptotic freedom, effective potential, A_0 condensate, effective charge, effective vertexes.

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Session Classification: Poster Session

Track Classification: HIGH ENERGY PHYSICS AND NUCLEAR MATTER

Contribution ID: 91

Type: Oral

Approximation by interpolation trigonometric polynomials in Weyl-Nagy classes $W_{\beta,1}^r$

Let L_p , $1 \leq p \leq \infty$, and C be the spaces of 2π -periodic functions with standard norms $\|\cdot\|_{L_p}$ and $\|\cdot\|_C$, respectively. Further, let $W_{\beta,p}^r$, $r > 0$, $\beta \in \mathbb{R}$, $1 \leq p \leq \infty$, be classes of 2π -periodic functions f that can be represented in the form of convolution

$$f(x) = \frac{a_0}{2} + \frac{1}{\pi} \int_{-\pi}^{\pi} \varphi(x-t) B_{r,\beta}(t) dt, \quad a_0 \in \mathbb{R}, \quad (1)$$

with Weyl-Nagy kernels of the form $B_{r,\beta}(t) = \sum_{k=1}^{\infty} k^{-r} \cos\left(kt - \frac{\beta\pi}{2}\right)$, of function φ satisfying the condition

$$\varphi \in B_p^0 = \left\{ \varphi \in L_p : \|\varphi\|_{L_p} \leq 1, \int_{-\pi}^{\pi} \varphi(t) dt = 0 \right\}.$$

The classes $W_{\beta,p}^r$ are called the Weyl-Nagy classes, and the function φ in representation (1) is called the (r, β) -derivative of the function f in the Weyl-Nagy sense and denoted by f_{β}^r .

Let $f \in C$. By $\tilde{S}_{n-1}(f; x)$ we denote a trigonometric polynomial of degree $n-1$, that interpolates $f(x)$ at the equidistant nodes $x_k^{(n-1)} = 2k\pi/(2n-1)$, $k \in \mathbb{Z}$, i.e., such that

$$\tilde{S}_{n-1}(f; x_k^{(n-1)}) = f(x_k^{(n-1)}), \quad k \in \mathbb{Z}.$$

Theorem 1. Let $r > 2$, $\beta \in \mathbb{R}$, $x \in \mathbb{R}$ and $n \in \mathbb{N}$. The following estimate is true

$$\text{cal} E_n(W_{\beta,1}^r; x) = \sup_{f \in W_{\beta,1}^r} \left| f(x) - \tilde{S}_{n-1}(f; x) \right| = \left| \sin \frac{(2n-1)x}{2} \right| n^{-r} \left(\frac{2}{\pi(1-e^{-r/n})} + \mathcal{O}(1)\delta_{r,n} \right),$$

where $\mathcal{O}(1)$ is a quantity uniformly bounded in all analyzed parameters,

$$\delta_{r,n} = \begin{cases} 1 + \frac{n}{r(r-2)}, & 2 < r \leq n+1, \\ \frac{r}{n^2} e^{-r/n}, & n+1 \leq r \leq n^2, \\ e^{-r/n} & r \geq n^2. \end{cases}$$

This work was partially supported by the VolkswagenStiftung project ‘‘From Modeling and Analysis to Approximation’’ and by the grant from the Simons Foundation (1290607, AS) and (1290607, IS).

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Presenter: SOKOLENKO, Ihor (Institute of Mathematics of NAS of Ukraine)

Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 92

Type: **Poster**

Features of the temperature dependences of the thermal conductivity of composites and the Meyer-Neldel rule

Tuesday, 24 September 2024 17:50 (5 minutes)

An analysis of the temperature dependences of thermal conductivity $\kappa(T)$ of composite materials - graphene-multilayer graphene, semiconductor composites Bi_{0.5}Sb_{1.5}Te₃ and In_{0.53}Ga_{0.47}As, was carried out as well as a comparison of their temperature dependences of $\kappa(T)$ with the thermal conductivity of similar materials, which are formed by superlattices, nanowires and hybrid nanostructures. The temperature dependence of the thermal conductivity $\kappa(T)$ of these materials can be presented as the sum of two contributions – quasi-particle κ_p and coherence contributions κ_c :

$$= p + c, (1)$$

which corresponds to two main mechanisms of heat transfer [1]. In the case of orientationally ordered crystals, thermal conductivity, as a rule, can be represented as:

$$= AT - 1 + 0, (2)$$

where the first term is determined by the three-phonon scattering processes of quasiparticles (phonons), and the second term is related to the wave properties of phonons and their ability to tunnel between phonon bands corresponding to the acoustic and optical phonon branches in the real dispersion law [1].

In the case where long-range order is present, the value of the coherent contribution κ_c is usually small compared to the quasi-particle contribution κ_p , but it becomes significant when no translation order - then it takes place the glass-like behavior of thermal conductivity – and it can be presented through an exponential dependence of the Arrhenius type:

$$c = 0 \exp(-E/T) (3)$$

with two characteristic parameters: pre-exponential factor κ_0 and energy E . It was shown that the temperature dependences of thermal conductivity with glassy behavior are quite well described by expression (3). Also, it is established that the pre-exponential factor κ_0 depends linearly on the energy E . Such a relationship between these values was previously discovered in the electrical conductivity of semiconductors (Meyer-Neldel rule) [2, 3].

References:

- [1] A.I. Krivchikov, Y.V. Horbatenko, O.A. Korolyuk, O.O. Romantsova, O.O. Kryvchikov, D. Szewczyk & A. Jezowski. Exponential approximation of the coherence contribution to the thermal conductivity of complex clathrate-type crystals. *Materialia*, 32, 101944 (2023).
- [2] A.I. Krivchikov & O.A. Korolyuk. Empirical universal approach to describing the thermal conductivity of amorphous polymers: Effects of pressure, radiation and the Meyer–Neldel rule. *Low Temperature Physics*, 50(4), 328-341 (2024).
- [3] W.V. Meyer and H. Neldel. Relation between the energy constant and the quantity constant in the conductivity–temperature formula of oxide semiconductors, *Z. tech. Phys.*, 18(12): 588–593 (1937).

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Presenter: Dr HORBATENKO, Yuliia (B.Verkin Institute for Low Temperature Physics and Engineering of the National Academy of Sciences of Ukraine)

Session Classification: Poster Session

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 94

Type: **Oral**

General hydrodynamic approach for a cold Bose gas

Tuesday, 24 September 2024 15:30 (20 minutes)

The aim of this paper is to derive the hydrodynamics for a cold Bose gas from the microscopic platform based on the many-body Schrödinger equation and general assumptions of the hydrodynamic approach (HA) applicable to any dimension. We develop a general HA for a cold spatially inhomogeneous Bose gas assuming two different temporal and spatial scales and obtain the energy as a functional of both fast inner quantum mode and slow macroscopic mode. The equations governing the fast and slow modes are obtained from this functional by their independent variations. The fast mode is the wave function in the stationary state at local density which can be ground, excited with a nonzero atom momenta, or a superposition of more than one states. The energy eigenvalue (or expectation value) of this local wave function universally enters the hydrodynamic equation for the slow mode in the form of the local chemical potential which incorporates the inner local momentum. For zero inner momenta and particular choices of this eigenvalue as a function of gas density, this equation reduces to the known equations based on the local density approximation. If however the inner momenta are nonzero, the equation includes the interaction between these momenta and the slow mode velocity. Relation between this general HA and the standard local density approximation is elaborated. Two effects of the local momenta and their density dependence on the soliton solutions are demonstrated.

(To appear in the Physical Review A, arXiv:2408.12363v1).

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Presenter: PERGAMENSHCHIK, Victor (Institute of Physics, NANU, Kyiv, Ukraine & Center for Theoretical Physics, PAN, Warsaw, Poland)

Session Classification: Afternoon Session 1

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 95

Type: **Oral**

Asymptotic step-like solutions of the Burgers equation with variable coefficients and singular perturbation

The talk deals with the singular perturbed Burgers equation with variable coefficients

$$\varepsilon u_{xx} = a(x, t, \varepsilon)u_t + b(x, t, \varepsilon)uu_x, \quad (1)$$

where $a(x, t, \varepsilon)$, $b(x, t, \varepsilon)$ are given as asymptotic series in a small parameter ε . Equation (1) is straightforward generalization of the Burgers equation

$$u_{xx} = u_t + \nu uu_x \quad (2)$$

that has been known since 1906 and has attracted the attention of researchers, because in one-dimensional case the equation is a simple form of Navier–Stokes equation. At the end of the 30-th years of the past century J.M.Burgers studied this equation as the simplest model unifying typical nonlinearity and viscosity ν which describes phenomenon of hydrodynamic turbulence. Model (2) is one of the simplest describing nonlinear effects, in particular, appearance and evolution of shock waves.

We consider asymptotic solution of equation (1) that is a discontinuous step-like function in limits case as $\varepsilon \rightarrow 0$. Such solution is called an asymptotic step-like solution. We present a general algorithm of constructing these solutions and prove the theorems on the accuracy with which the main term and the first approximation satisfy equation (1). These results are demonstrated on an example, for which the first asymptotic step-like approximation is explicitly found. The asymptotic solution is global, and has a form of the shock wave type function. There are also given graphs of these approximate solutions for certain numerical parameters.

The talk presents results published in [1].

[1]. Samoilenko, V., Samoilenko, Yu., Zappale, E., Asymptotic step-like solutions of the singularly perturbed Burgers equation. *Phys Fluids*, 35(6), 067106 (2023).
<https://doi.org/10.1063/5.0150685>

Primary authors: SAMOILENKO, Valerii (Institute of Mathematics of NAS of Ukraine); SAMOILENKO, Yuliia (Claude Bernard Lyon 1 University); Dr ZAPPALE, Elvira (Dipartimento di Scienze di Base ed applicate per l'Ingegneria, Sapienza – Università di Roma)

Presenter: SAMOILENKO, Valerii (Institute of Mathematics of NAS of Ukraine)

Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 96

Type: Oral

Soliton- and peakon-like solutions to the modified Camassa-Holm equation with variable coefficients

We consider asymptotic soliton- and peakon-like solutions to the modified Camassa-Holm equation with variable coefficients and a singular perturbation

$$a(x,t,\varepsilon)u_t - \varepsilon^2 u_{xxt} + b(x,t,\varepsilon)u^2 u_x - 2\varepsilon^2 u_x u_{xx} - \varepsilon^2 u u_{xxx} = 0. \quad (1)$$

Here ε is a small parameter and the coefficients $a(x, t, \varepsilon)$ and $b(x, t, \varepsilon)$ with $(x, t) \in \mathbf{R} \times [0; T]$ for some $T > 0$ can be presented as:

$$a(x, t, \varepsilon) = \sum_{k=0}^N \varepsilon^k a_k(x, t) + O(\varepsilon^{N+1}), \quad b(x, t, \varepsilon) = \sum_{k=0}^N \varepsilon^k b_k(x, t) + O(\varepsilon^{N+1}).$$

This equation is a generalization of the well-known modified Camassa-Holm equation [1, 2], which is an integrable system having both smooth and peaked soliton solutions, named peakons. We present an approach of constructing asymptotic solutions for equation (1) and we study their accuracy [3].

The results are illustrated by nontrivial examples of both asymptotic soliton- and peakon-like solutions, for which we compute the main and the first terms of their expansions. We also present graphics illustrating the obtained solutions for various values of small parameter. The proposed technique can be applied to construct wave-like solutions of different types for other equations [4].

Acknowledgement

The research is partially supported by Programme PAUSE and the ANR, project N.~ANR-22-PAUK-0038-01.

[1]. Camassa R., Holm D., An integrable shallow water equation with peaked soliton, *Phys. Rev. Lett.*, 1993, September, Vol.71, N.11, pp.1661-1664.

<https://doi.org/10.1103/PhysRevLett.71.1661>

[2]. Chen R.M., Hu T., Liu Y., The shallow-water models with cubic nonlinearity, *J. Math. Fluid Mech.*, 2022, Vol. 24., Article number: 49. <https://doi.org/10.1007/s00021-022-00685-4>

[3]. Brandolese L., Samoilenko Yu., Samoilenko V. Asymptotic soliton- and peakon-like solutions of the modified Camassa-Holm equation with variable coefficients and singular perturbation, arXiv:2307.11578.

[4]. Samoilenko V., Samoilenko Yu., Zappale E., {Asymptotic step-like solutions of the singularly perturbed Burgers equation}, *Phys. Fluids*, 2023, Vol.~35, N.~6, 067106.

<https://doi.org/10.1063/5.0150685>

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Presenter: SAMOILENKO, Yuliia (Claude Bernard Lyon 1 University)

Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 97

Type: Oral

Analytical Description of Size Effects, Strains and Ferro-ionic Coupling in Si-Compatible Nanosized Ferroelectrics

Thursday, 26 September 2024 10:00 (20 minutes)

The analytical methods based on the Landau-Ginzburg-Devonshire (LGD) approach and variational principle allow the analytical description of size effects, strain and ferro-ionic coupling in low-dimensional ferroelectric materials, such as thin films and small nanoparticles. The validity of LGD approach is corroborated by experimental evidence of the size- and strain-induced transitions as well as the related phenomena in the low-dimensional ferroelectric materials. For the correct description of these effects in ferroelectric thin films and small nanoparticles the LGD approach should be combined with the classical electrostatics and elasticity theory, and variational principle. It is important to determine how the LGD expansion coefficients depend on various factors, such as temperature, size, elastic stresses and/or strains, and ionic-electronic charge density and distribution. For classical ferroelectric films with a pronounced temperature-dependent and strain-dependent soft mode, the first expansion coefficients have a linear dependence on the temperature and elastic strain.

The significant attention is devoted to the comparison with experimental results and finite element modelling, as well as on the theoretical predictions of the size-, strain- and ionic- control of polar and dielectric properties of nanosized ferroelectric materials.

As the first example, we consider ultra-thin layers and nanoflakes of van der Waals ferroelectric CuInP_2S_6 covered by an ionic surface charge and reveal the appearance of polar states with relatively high polarization and stored free charge, which can mimic “mid-gap” states related with a surface field-induced transfer of Cu and/or In ions in the van der Waals gap [1]. The changes of the ionic screening degree and mismatch strains can induce the transitions between paraelectric phase, antiferroelectric, ferroelectric, and ferroelectric-like states in CuInP_2S_6 nanoflakes. Due to the emergence of manyfold-degenerated metastable states of spontaneous polarization the ultra-thin layers of CuInP_2S_6 reveal features of the controllable negative capacitance effect [2], which make them attractive for advanced electronic devices, such as nano-capacitors and gate oxide nano-materials with reduced heat dissipation.

As the second example, we use the LGD model to quantify the strain-charge-polarization coupling in nanosized $\text{Hf}_x\text{Zr}_{1-x}\text{O}_2$. A key factor ruling the observed polar properties of nanosized $\text{Hf}_x\text{Zr}_{1-x}\text{O}_2$ is the presence of the polar orthorhombic phase. This phase is metastable compared to the bulk monoclinic phase, leading to problems with the ferroelectric phase stability in nanoscale. The electrophysical properties of the $\text{Hf}_x\text{Zr}_{1-x}\text{O}_2$ thin films and nanoparticles are very sensitive to the elastic strain induced by the substrate, annealing conditions, deposition method, film thickness, content x and dopants. Depending on the interplay of these factors, the nanosized $\text{Hf}_x\text{Zr}_{1-x}\text{O}_2$ exhibits dielectric, ferroelectric, or antiferroelectric behavior.

The used model [3] incorporates parametrized Landau expansion coefficients for the polar and antipolar orderings. Obtained results agrees with the recent existing experimental data for $\text{Hf}_x\text{Zr}_{1-x}\text{O}_{2-y}$ thin films and oxygen-deficient HfO_{2-y} nanoparticles [4], namely the X-ray diffraction confirmed the formation of a ferroelectric orthorhombic phase in the HfO_{2-y} nanoparticles under special favorable annealing conditions.

The analytical LGD approach correctly predicts the phase diagrams, ground and metastable states, alongside the domain structure morphology, associated polar and structural properties of $\text{Hf}_x\text{Zr}_{1-x}$

xO₂-y thin films and nanoparticles with different shapes and sizes. The successful application of the analytical LGD approach can be useful for the prediction of the silicon-compatible ferroelectric nanomaterials based on HfxZr_{1-x}O_{2-y}.

The work is funded by the National Research Foundation of Ukraine (projects “Manyfold-degenerated metastable states of spontaneous polarization in nanoferroics: theory, experiment and perspectives for digital nanoelectronics”, grant N 2023.03/0132 and “Silicon-compatible ferroelectric nanocomposites for electronics and sensors”, grant N 2023.03/0127).

[1]. Anna N. Morozovska, Sergei V. Kalinin, Eugene A. Eliseev, Svitlana Kopyl, Yulian M. Vysochanskii, and Dean R. Evans. Ferri-ionic Coupling in CuInP₂S₆ Nanoflakes: Polarization States and Controllable Negative Capacitance (2024), <https://doi.org/10.48550/arXiv.2405.14368>

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[3]. Anna N. Morozovska, Maksym V. Strikha, Kyle P. Kelley, Sergei V. Kalinin, and Eugene A. Eliseev. Effective Landau-type model of a HfxZr_{1-x}O₂-graphene nanostructure, *Phys. Rev. Applied* 20, 054007 (2023) <https://doi.org/10.1103/PhysRevApplied.20.054007>

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Presenter: Prof. MOROZOVSKA, Anna (Institute of Physics, National Academy of Sciences of Ukraine)

Session Classification: Morning Session 3

Track Classification: CONDENSED MATTER PHYSICS

Microscopic derivation of the generalized Bohr Hamiltonian

Tuesday, 24 September 2024 17:05 (5 minutes)

The Bohr's Hamiltonian is one of the main cornerstones of the nuclear structure theory. It was derived by Bohr [1], treating the nucleus as a liquid spherical drop with uniform density and sharp surface, performing quadrupole vibrations with small amplitude. During such oscillations at any moment of time the nucleus attains an ellipsoidal shape, retaining its volume constant due to small compressibility of the nuclear matter.

Following the microscopic theory [2], where the kinetic energy operator of the nucleus has been expressed in terms of the independent set of $3N$ collective variables, we constructed the collective Hamiltonian for nuclei with arbitrary deformation [3], which recovers the results of Bohr [1] at $\beta \ll 1$. First the classical kinetic energy T of N nucleons in the center-of-mass frame is expressed in terms of the Jacobi vectors \mathbf{q}_i , where $i = 1, 2, \dots, n = N - 1$. Then we introduce the rotating frame with axes ξ, η, ζ directed along the principal axes of the nuclear tensor of inertia. Its orientation is determined by the Euler angles φ, ϑ, ψ . In this case the off-diagonal elements of the inertia tensor vanish, so that

$$\sum_{i=1}^n a_{i\xi} a_{i\eta} = \sum_{i=1}^n a_{i\xi} a_{i\zeta} = \sum_{i=1}^n a_{i\eta} a_{i\zeta} = 0,$$

where $a_{i\nu}$ denote the projections of the Jacobi vectors on the axes frame ξ, η, ζ . We introduce an abstract Euclidian space with basis orthonormal vectors \mathbf{e}_i and define there three vectors \mathbf{A}_ν with components $a_{i\nu}$ and lengths a_ν . The above constraint can be treated as an orthogonality condition for these vectors, while their lengths a_1, a_2, a_3 serve as three collective coordinates, specifying size and shape of the nucleus. It is natural to determine the remaining $3n-6$ internal coordinates as any rotational variables, which describe orientation of three vectors in the n -dimensional hyperspace. For this aim we take the generalized Euler angles θ_{jk} , introduced by Vilenkin.

Following Bohr's model [1], we demand that the vibrations and rotations only change a shape of the ellipsoidal nucleus keeping unchanged its volume, i.e., we demand that at arbitrary deformations the product of radii R_κ of the nuclear ellipsoid is related to the radius R_0 of the sphere with the same volume by $R_1 R_2 R_3 = R_0^3$ at $R_0 = \text{const}$. The radii, meeting this condition, we chose as [3] $R_\kappa = R_0 \text{cal}E_\kappa(\beta, \gamma)$, with $\text{cal}E_\kappa(\beta, \gamma) = \exp\left[\tilde{\beta} \cos\left(\gamma - \frac{2\pi}{3}\kappa\right)\right]$ and $\tilde{\beta} = (5/4\pi)^{1/2}\beta$. When $\beta \ll 1$, the above expressions for R_κ coincide with well known ones and respectively our generalized parameters β, γ coincide with Bohr's variables. Expressing the kinetic energy T in the suggested collective coordinates and then quantizing it, we derived the Hamiltonian, depending on the exactly determined inertia functions $b_{\lambda\lambda'}(\beta, \gamma)$, in contrast to existing in literature Hamiltonians, written ad hoc with unknown inertia parameters.

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Session Classification: Poster Session

Track Classification: HIGH ENERGY PHYSICS AND NUCLEAR MATTER

Contribution ID: **101**Type: **Oral**

The Painlevé I equation and Virasoro algebra

In this talk, I will explain how rank $5/2$ representations of Virasoro algebra can be used to compute asymptotic expansion of the tau function of Painlevé 1 equation near irregular singularity. The talk is based on recent paper of Hasmik Poghosyan and Rubik Poghossian, where they introduced conformal block with irregular vertex of rank $5/2$ and conjectured that it is related to the partition function of H_0 Argyres–Douglas theory. Additionally, I will present some improvements of this construction, which is the part of ongoing paper in collaboration with Oleg Lisovyy, Nikolai Iorgov and Kohei Iwaki.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: **102**Type: **Oral**

Entanglement of the diamond spin cluster

Tuesday, 24 September 2024 13:10 (20 minutes)

The entanglement of diamond spin systems in thermodynamic equilibrium has been studied in various papers (for, example, [1, 2, 3, 4]). We focus on the evolution of entanglement in a diamond spin-1/2 cluster. This cluster consists of two central spins described by the anisotropic Heisenberg model, which interact with two side spins via an Ising interaction. The influence of the interaction coupling with the side spins on the entanglement of the central spins is investigated [5, 6]. It is demonstrated that the behavior of entanglement between the central spins can be controlled by choosing the appropriate value of this coupling. Additionally, we examine the influence of a bosonic bath on the entanglement of the central spins.

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Session Classification: Morning session 1

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 103

Type: **Poster**

Lattice models of ionic liquids in conducting slit nanoconfinement

Tuesday, 24 September 2024 16:25 (5 minutes)

Confined ionic liquids exhibiting exciting physics are essential in modern technologies. The narrow conducting confinements cause exponential screening of the electrostatic interactions between ions, allowing the development of models with short-range interactions that can provide analytical insights into the charge storage mechanisms. In this contribution, we present a lattice model for ionic liquids confined in ultranarrow slit-shaped pores admitting a single layer of ions. In the case of next-nearest interactions, it can be mapped onto the well-known three-state Blume-Capel model, which obeys an analytical solution within the Bethe-lattice approximation [1]. Analyzing phase behavior and pore charging in terms of pore ionophilicity, interionic interactions, and applied potential difference, we obtained a phase diagram comprising the lines of first- and second-order, direct and re-entrant phase transitions, manifested by singularities in the capacitance-voltage dependence [2]. These analytical results are corroborated by lattice Monte Carlo simulations [3]. However, it is known that, at least in the quasi-one-dimensional case of single-file pores, the results of the lattice model with short-range interactions differ even qualitatively from the exact results of the corresponding continuous model [4]. We will discuss possible ways to improve the lattice model by considering further interactions and analyzing changes in the phase diagram depending on the interaction parameters.

This research is supported by bilateral project № M/72-2024 between Ministry of Education and Science of Ukraine and Polish National Agency for Academic Exchange (NAWA) as well as U. S. Department of Energy (DOE), Office of Science, Basic Energy Sciences, Materials Science and Engineering Division, under Award No. DE-SC0013599 (Subaward No. UTAUS-SUB00000795)

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Session Classification: Poster Session

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 104

Type: Oral

Four types of phase transitions in interacting boson system at high temperatures

Wednesday, 25 September 2024 16:20 (20 minutes)

Within the framework of the mean-field model, the thermodynamics of the relativistic bosonic system of interacting particles and antiparticles in the presence of a Bose-Einstein condensate is investigated. It is assumed that the total isospin (charge) density is conserved. It is shown that the particle-antiparticle boson system reveals four types of phase transitions into the condensate phase. Three types belong to the phase transition of the second order and one to the first order. We show that the grand canonical ensemble is not suitable for describing a bosonic system of particles and antiparticles in the presence of condensate, but an adequate study can be carried out within the framework of the canonical ensemble, where the chemical potential is a thermodynamic quantity that depends on the canonical free variables.

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Session Classification: Afternoon Session 2

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 105

Type: Oral

Dissipative magnetic 2D Zakharov system in bounded domain

We consider the dissipative magnetic Zakharov system in a smooth (2D) bounded domain $\Omega \subset \mathbb{R}^2$ of the form

$$\begin{aligned} iE_t + \Delta E - nE + iE \times B + i\gamma_1 E &= g_1(x, t), & x \in \Omega, \\ n_{tt} + \gamma_2 n_t - \Delta (n + |E|^2) &= g_2(x, t), & x \in \Omega, \\ B_{tt} - \gamma_3 \Delta B_t + \Delta^2 (B + iE \times \bar{E}) &= g_3(x, t), & x \in \Omega, \end{aligned}$$

where $n(x, t)$ and $B(t, x) = (0, 0, B_3(t, x))$ are the real functions and $E(x, t) = (E_1(t, x), E_2(t, x), 0)$ is a complex one.

If we omit magnetic field B , then the above system is reduced to the dissipative Zakharov system. This system has been studied by many authors (see [1] and references therein).

In the case $\Omega = \mathbb{R}^d$ for $d = 2, 3$ the Cauchy problem for the above system has been considered in [2]. It was obtained local existence and uniqueness results. Our main result is the global well-posedness of the considered problem in some Sobolev type classes and existence of a global attractor.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 106

Type: Poster

Model of effective permittivity for dense ferroelectric nanocomposites

Tuesday, 24 September 2024 17:15 (5 minutes)

Existing theoretical models of ferroelectric nanocomposites use the effective medium approximation to describe their dielectric and conductive properties. The most common effective medium models (Landau linear mixture approximation, Maxwell-Garnett model, Bruggeman model, etc.) may be invalid for dense nanocomposites when the volume fraction of ferroelectric inclusions exceeds 20-30%. We have proposed several modifications, such as averaging over particle size, finite conductance of the screening shell, and the dipole-dipole cross-interaction effects between the electric polarization (i.e., their electric dipoles) of different ferroelectric nanoparticles separated by shells and a matrix.

The Lichtenecker-Rotter model, which is free from the volume fraction limitations, was used to estimate the effective dielectric constant ϵ_{eff} of the nanocomposite without taking into account the effects of cross-interaction. However, the presence of small particles (size 30 nm or less) should be taken into account, as dipole-dipole cross-interactions can lead to the formation of polar clusters, where the ferroelectric dipoles of single-domain nanoparticles are strongly correlated, and the correlations determine the effective dielectric response of the composite.

The presence for larger submicron particles (size 300 nm or more), which usually split into ferroelectric domains, the cross-interaction effects can lead to correlated motion of ferroelectric domain walls in neighboring nanoparticles, which, in turn, make a significant contribution to the temperature and frequency behavior of the dielectric response of the composite.

The dependence on $\epsilon_P(T, \theta, \omega)$ of the frequency ω and the temperature of the local transition θ of nanoparticles and their polar clusters in a ferroelectric polymer nanocomposite was analyzed taking into account the dipole-dipole cross-interactions. As a result, the equation for θ was obtained. This equation was successfully applied to calculate the dielectric constant of dense PVDF nanocomposites with 20-30 vol.% of barium titanate nanoparticles. The obtained results can be used for the prediction and development of the flexible and cheap nanocomposite with superior polar and dielectric properties for usage in non-volatile memory cells, energy-saving elements, modulators and sensors.

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Presenter: BEREZNYKOV, Oleksii

Session Classification: Poster Session

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 107

Type: **Oral**

Painleve I equation and modular forms

The isomonodromic tau function of the Painleve I equation can be presented as a Fourier transform of the partition function of the Argyres-Douglas theory of type H_0 . A possible way to derive this partition function is to use the holomorphic anomaly equation (HAE) as a recursive relation for the topological expansion of corresponding free energy (logarithm of the partition function). The solution of HAE is given in terms (quasi)modular forms of $SL(2, \mathbb{Z})$. We propose a basis in the space of modular forms, allowing us to prove the uniqueness of HAE's solution.

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Presenter: IORGOV, Nikolai (Bogolyubov Institute for Theoretical Physics)

Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 108

Type: Oral

Application of Chebyshev polynomials for optimal differentiation and summation.

In our research, we study the problems of numerical differentiation and summation of univariate functions. Many works are devoted to these problems, among which we highlight [1-4].

As is known, in assessing the effectiveness of approximate methods, their optimality plays an important role. At the same time, in NDS, until recently the optimality of methods was understood only in the sense of their accuracy. The point is that the optimal accuracy can be achieved by using different amounts of discrete information. Therefore, it makes sense to also study information complexity of NDS. In other words, it is very important to research NDS methods that achieve optimal accuracy by using the minimal possible amount of discrete input data. To solve NDS problems, we propose an approach based on the truncation method. The essence of this method is to replace the infinite Fourier series with a finite sum. It is only necessary to properly select the order of this sum, which plays the role of a regularization parameter here. Moreover, the proposed approach allows us to construct algorithms that achieve the optimal order of accuracy by using the minimum amount of discrete information in the form of perturbed values of the Fourier-Chebyshev coefficients. In addition, the use of Chebyshev polynomials makes it possible to construct quadrature formulas for specially selected nodes, the number of which is the minimum possible. In other words, the proposed approach ensures the stability of approximations, leads to a reduction in computational costs without loss of accuracy, and does not require cumbersome computational procedures. Moreover, of interest to researchers is the question of determining the conditions under which the numerical summation problem is well-posed. The authors have found an answer to this question for the classes of functions under consideration.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: **109**

Type: **Poster**

On modern applications of Lie algebras

This work reviews modern applications of Lie algebras, such as: limiting transitions between different models, new classes of orthogonal special functions, and the construction of quasicrystals using root systems. We also provide a list of unsolved but promissive problems that have important applications.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 111

Type: Poster

The development of Bogolyubov reduced description method in the application to spin and quasispin systems

Tuesday, 24 September 2024 16:45 (5 minutes)

The development of Bogolyubov reduced description method in the application to spin and quasispin systems

Sokolovsky A. I., Lyagushyn S. F.

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The reduced description method (RDM) is based on the Bogolyubov's idea that at large time the non-equilibrium state evolution of a macroscopic system can be described with the limited number of parameters. The way to the right choice of such parameters and constructing the equations of time evolution for them was opened by the works of Kharkiv school in statistical physics [1]. Since early 2000-ies the authors deal with applying the proposed technique to Dicke superradiance – the unique phenomenon of emitter system self-organization in the process of reaching the equilibrium state from excited one. We are interested in a more detailed picture of correlation development both in emitter and field subsystems. The problem of correlator decoupling which arises in the Bogolyubov method of boson variable elimination [2], seems worthy of attention. In RDM, including the binary correlation functions into the set of reduced description parameters (RDPs) results in the necessity of calculating the averages with quasi-equilibrium Hamiltonians where such new parameters are present. Usually, two-level electromagnetic emitters are described using the quasispin operators constructed with Pauli matrices. While considering the acoustic superradiance, spin and phonon operators are necessary for the Hamiltonian construction. The operator forms prove to be the same for boson fields of different nature. Thus, we face the problem of averaging in the case when the exponential statistical operator includes a quadratic form of spin operators in the exponent that cannot be done exactly.

In our recent papers [3, 4], a new approach consisting of introducing additional small parameter in the theory of relaxation processes in spin systems has been proposed. While the spin-boson interaction constant is a customary small parameter in the specified theory, we put forward the idea of accounting for small deviations of correlation functions taken as RDPs from their values calculated in the picture with the only RDP describing the state of a spin (quasispin) system – the excitation degree of the emitter subsystem η_1 ($s^z = \sum_{1 \leq i \leq N} s_i^z$ in usual designations). Restricting ourselves with the concentrated Dicke model, we can use the known equation for s^z possessing the integral of motion including the binary correlation function $\langle \hat{s}^+ \hat{s}^- \rangle$. In the theory of superradiance using $\langle \hat{s}^+ \hat{s}^- \rangle$ as an independent RDP η_2 ($\hat{\eta}_2 = \hat{s}^+ \hat{s}^-$), we construct the quasi-equilibrium statistical operator of RDM $\rho_q = e^{\Omega - Z_1 \hat{\eta}_1 - Z_2 \hat{\eta}_2}$ implying the condition of smallness of the deviation $\delta\eta_2 = Sp(\rho_q - \rho_q^0) \hat{\eta}_2$, i.e. difference between correlation function obtained with such operator and those of RDM model with η_1 only $\rho_q^0 = e^{\Omega - Z_1 \hat{\eta}_1}$. We use $\delta\eta_2$ as a new small parameter of the order μ and the statistical operator ρ_q can be expressed via ρ_q^0 in the form of μ power expansion. Thus, we obtain expressions for spin average deviations with an error up to μ^3 and evolution equations for η_1 , η_2 , and boson RDPs n_k . The solved problem relates to cumbersome calculations but only averages with linear forms of spin operators and quadratic forms of boson operators are needed. The technique of averaging for spin operators was improved in the framework of our activities. The results are applicable for different versions of Dicke model and Wagner model of acoustic superradiance.

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Session Classification: Poster Session

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 113

Type: **Poster**

DNA condensation induced by Li⁺ counterions

Tuesday, 24 September 2024 17:20 (5 minutes)

DNA is a highly charged molecule that is neutralized by positively charged metal or molecular ions (counterions). The neutralization of DNA by these counterions induces various effects, including the formation of DNA-DNA contacts that lead to further condensation of the macromolecule. The effect of DNA condensation has been widely observed for highly charged counterions ($\geq 3+$). For divalent counterions, DNA condensation is sometimes observed, whereas with monovalent ions, it is generally considered impossible due to insufficient neutralization of the double helix's charge required to form stable DNA-DNA contacts. However, the idea that DNA cannot condense with monovalent ions overlooks the interplay between water molecules in the DNA hydration shell and those in the hydration shell of counterions, which can play an essential role in the interaction of DNA duplexes. Li⁺ is highly hydrated and it is localized within a stable tetrahedron formed by four oxygen atoms of water molecules. Considering the structural complementarity of the DNA phosphate groups to the hydration shell of Li⁺ ions [1], the formation of Li-mediated DNA-DNA contacts may occur. To elucidate the possibility of forming stable Li⁺ crosslinks between different DNA double helices, the molecular mechanisms of their formation are studied in the present work. Atomistic molecular dynamics simulations of five DNA fragments in a simulation box with LiCl concentration 0.1 M and 1.0 M of salt were carried out. As a result of our study, the possible configurations of crosslinks between phosphate groups of different DNA fragments were determined. To validate the obtained results, the vibrational spectra of characteristic complexes were calculated using quantum-chemical methods and compared with existing experimental data. This work demonstrates that DNA-DNA contacts mediated by Li⁺ can form in aqueous solutions with a high concentration of DNA and LiCl salt, supporting the idea of DNA condensation by Li⁺ counterions.

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Session Classification: Poster Session

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 114

Type: Oral

Effects of metallic and molecular counterions in structural dynamics of the DNA double helix

Tuesday, 24 September 2024 15:10 (20 minutes)

The structure of the DNA double helix is stabilized by water molecules and positively charged metallic or molecular ions, which form an ion-hydration shell around the macromolecule. The ions neutralize the negatively charged phosphate groups of the DNA backbone and thus act as counterions. Despite the extensive number of experimental and theoretical studies, the specific effects of counterions on the structural dynamics of the DNA double helix and its ion-hydration shell remain incompletely understood. This contribution will overview the most recent findings on this topic based on molecular dynamics simulation results. Specifically, the effects of hydration of Li^+ , Na^+ , K^+ , Rb^+ , Cs^+ and Mg^{2+} counterions localized in different regions of the DNA macromolecule will be discussed, along with the interplay of water molecules around the ions and within the hydration shell of the double helix [1,2]. In the case of molecular ions, the role of conformational effects of flexible polyamines (putrescine²⁺, spermidine³⁺, and spermine⁴⁺) for the interaction with the DNA double helix and the formation of stable DNA-DNA contacts will be described [3-6]. The results will be discussed in the context of understanding the physical mechanisms behind DNA's biological functioning and the development of DNA-based materials for nanotechnological applications.

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Session Classification: Afternoon Session 1

Track Classification: CONDENSED MATTER PHYSICS

Two-dimensional central extensions of some superconformal loop Lie algebra generalization and compatibly bi-Hamiltonian $(2|N + 1)$ -dimensional systems on functional supermanifolds

For $N \in \{1, 2, 3\}$ there is considered the semi-direct sum $\tilde{\mathcal{G}} \ltimes \tilde{\mathcal{G}}_{reg}^*$ of the loop Lie algebra $\tilde{\mathcal{G}}$, consisting of the even left superconformal vector fields on a supercircle $\mathbb{S}^{1|N}$ in the form $\tilde{a} := a\partial/\partial x + \frac{1}{2} \sum_{i=1}^N (D_{\vartheta_i} a) D_{\vartheta_i}$, where $a := a(x, \vartheta; \lambda) \in C^\infty(\mathbb{S}^{1|N} \times (\mathbb{D}_+^1 \cup \mathbb{D}_-^1))$; Λ_0 is holomorphic in the “spectral” parameter $\lambda \in \mathbb{D}_+^1 \cup \mathbb{D}_-^1 \subset \mathbb{C}$, $\mathbb{D}_+^1, \mathbb{D}_-^1$ are the interior and exterior regions of the unit centrally located disk $\mathbb{D}^1 \subset \mathbb{C}$ respectively, $a(x, \vartheta; \infty) = 0$, $(x, \vartheta) \in \mathbb{S}^{1|N} \simeq \mathbb{S}^1 \times \Lambda_1^N$, $\Lambda := \Lambda_0 \oplus \Lambda_1$ is a commutative Banach superalgebra over the field $\mathbb{C} \subset \Lambda_0$, $\partial/\partial x$ is a partial derivative by the commuting variable x , $\vartheta := (\vartheta_1, \vartheta_2, \dots, \vartheta_N)$, $\partial/\partial \vartheta_i$ is a left partial derivative by the anticommuting variable $\vartheta_i \in \Lambda_1$, $D_{\vartheta_i} := \partial/\partial \vartheta_i + \vartheta_i \partial/\partial x$, $i = \overline{1, N}$, and its regular dual space $\tilde{\mathcal{G}}_{reg}^*$ with respect to the parity $(\tilde{a}, \tilde{l})_0 = \text{res}_{\lambda \in \mathbb{C}} \int_{\mathbb{S}^{1|N}} dx d\vartheta_1 \dots d\vartheta_N (a\tilde{l})$, where $\text{res}_{\lambda \in \mathbb{C}}$ denotes the coefficient at λ^{-1} in the corresponding Laurent series, $\tilde{l} \in \tilde{\mathcal{G}}_{reg}^*$ is a right superdifferential 1-form on $\mathbb{S}^{1|N}$ such as $\tilde{l} := (dx - \sum_{i=1}^N (d\vartheta_i)\vartheta_i)l(x, \vartheta; \lambda) \in \tilde{\mathcal{G}}_{reg}^*$, $l := l(x, \vartheta; \lambda) \in C^\infty(\mathbb{S}^{1|N} \times (\mathbb{D}_+^1 \cup \mathbb{D}_-^1))$; Λ_s is holomorphic in the “spectral” parameter $\lambda \in \mathbb{D}_+^1 \cup \mathbb{D}_-^1$, $l(x, \vartheta; \infty) = 0$, $s = 1$ if N is an odd natural number and $s = 0$ if N is an even one. The loop Lie algebra $\tilde{\mathcal{G}}$ is splitting into the direct sum $\tilde{\mathcal{G}} = \tilde{\mathcal{G}}_+ \oplus \tilde{\mathcal{G}}_-$ of its Lie subalgebras for which $\tilde{\mathcal{G}}_{+,reg}^* \simeq \tilde{\mathcal{G}}_-$, $\tilde{\mathcal{G}}_{-,reg}^* \simeq \tilde{\mathcal{G}}_+$, where $a(x, \vartheta; \infty) = 0$ for any $\tilde{a} \in \tilde{\mathcal{G}}_-$. On $\tilde{\mathcal{G}} \ltimes \tilde{\mathcal{G}}_{reg}^*$ one determines the commutator $[\tilde{a} \ltimes \tilde{l}, \tilde{b} \ltimes \tilde{m}] := [\tilde{a}, \tilde{b}] \ltimes (ad_{\tilde{a}}^* \tilde{m} - ad_{\tilde{b}}^* \tilde{l})$ for any $\tilde{a}, \tilde{b} \in \tilde{\mathcal{G}}$ and $\tilde{l}, \tilde{m} \in \tilde{\mathcal{G}}_{reg}^*$, where $[\tilde{a}, \tilde{b}] := \tilde{c}$, $\tilde{c} \in \tilde{\mathcal{G}}$, $c := a(\partial b/\partial x) - b(\partial a/\partial x) + \frac{1}{2} \sum_{i=1}^N (D_{\vartheta_i} a)(D_{\vartheta_i} b)$, ad^* is the coadjoint action of $\tilde{\mathcal{G}}$ with respect to the parity $(\cdot, \cdot)_0$, as well as the symmetric bilinear form $(\tilde{a} \ltimes \tilde{l}, \tilde{b} \ltimes \tilde{m})_0 = (\tilde{a}, \tilde{m})_0 + (\tilde{b}, \tilde{l})_0$. One constructs the central extensions $\tilde{\mathcal{G}} := \tilde{\mathcal{G}} \oplus \mathbb{C}^2$ of the Lie algebra $\tilde{\mathcal{G}} := \prod_{z \in \mathbb{S}^1} (\tilde{\mathcal{G}} \ltimes \tilde{\mathcal{G}}_{reg}^*)$ by the superanalogs of the Ovsienko-Roger 2-cocycle such as $\omega_2(\tilde{a} \ltimes \tilde{l}, \tilde{b} \ltimes \tilde{m}) := (\omega_2^1(\tilde{a} \ltimes \tilde{l}, \tilde{b} \ltimes \tilde{m}), \omega_2^2(\tilde{a} \ltimes \tilde{l}, \tilde{b} \ltimes \tilde{m}))$, where $\omega_2^1(\tilde{a} \ltimes \tilde{l}, \tilde{b} \ltimes \tilde{m}) = \text{res} \int_{\mathbb{S}^1} dz \int_{\mathbb{S}^{1|N}} dx d^N \vartheta (a(\mathcal{P}b))$, $\omega_2^2(\tilde{a} \ltimes \tilde{l}, \tilde{b} \ltimes \tilde{m}) = \int_{\mathbb{S}^1} dz ((a, \partial m/\partial z)_0 - (b, \partial l/\partial z)_0)$, $(\tilde{a} \ltimes \tilde{l}), (\tilde{b} \ltimes \tilde{m}) \in \tilde{\mathcal{G}}$, $z \in \mathbb{S}^1$, and $\mathcal{P} = D_{\vartheta_1} \partial^2/\partial^2 x$ when $N = 1$, $\mathcal{P} = D_{\vartheta_1} D_{\vartheta_2} \partial/\partial x$ when $N = 2$, $\mathcal{P} = D_{\vartheta_1} D_{\vartheta_2} D_{\vartheta_3}$ when $N = 3$.

Since the Lie algebra $\tilde{\mathcal{G}}$ permits the standard splitting $\tilde{\mathcal{G}} := \tilde{\mathcal{G}}_+ \oplus \tilde{\mathcal{G}}_-$ into a direct sum of its Lie subalgebras $\tilde{\mathcal{G}}_+ := \prod_{z \in \mathbb{S}^1} (\tilde{\mathcal{G}}_+ \ltimes \tilde{\mathcal{G}}_{-,reg}^*)$ and $\tilde{\mathcal{G}}_- := \prod_{z \in \mathbb{S}^1} (\tilde{\mathcal{G}}_- \ltimes \tilde{\mathcal{G}}_{+,reg}^*)$, on its dual space $\tilde{\mathcal{G}}^*$ with respect to the symmetric bilinear form $\langle \cdot, \cdot \rangle_0 := \int_{\mathbb{S}^1} dz (\cdot, \cdot)_0$ one can introduce for any smooth by Frechet functionals $\mu, \nu \in \mathcal{D}(\tilde{\mathcal{G}}^*)$ the \mathcal{R} -deformed Lie-Poisson bracket $\{\mu, \nu\}_{\mathcal{R}}(\tilde{a} \ltimes \tilde{l}) = \langle \tilde{a} \ltimes \tilde{l}, [R\nabla_r \mu(\tilde{a} \ltimes \tilde{l}), \nabla_l \nu(\tilde{a} \ltimes \tilde{l})] + [\nabla_r \mu(\tilde{a} \ltimes \tilde{l}), R\nabla_l \nu(\tilde{a} \ltimes \tilde{l})] \rangle_0 + \langle e, \omega_2(R\nabla_r \mu(\tilde{a} \ltimes \tilde{l}), \nabla_l \nu(\tilde{a} \ltimes \tilde{l})) + \omega_2(\nabla_r \mu(\tilde{a} \ltimes \tilde{l}), R\nabla_l \nu(\tilde{a} \ltimes \tilde{l})) \rangle$, where $e = (e_1, e_2) \in \mathbb{C}^2$, the brackets $\langle \cdot, \cdot \rangle$ denote the scalar product on \mathbb{C}^2 , $\mathcal{R} = (P_+ - P_-)/2$, P_+ and P_- are projectors on $\tilde{\mathcal{G}}_+$ and $\tilde{\mathcal{G}}_-$ respectively, $\nabla_l h(\tilde{a} \ltimes \tilde{l}) := (\nabla_l h_{\tilde{l}} \ltimes \nabla_l h_{\tilde{a}}) \in \tilde{\mathcal{G}}$ and $\nabla_r h(\tilde{a} \ltimes \tilde{l}) := (\nabla_r h_{\tilde{l}} \ltimes \nabla_r h_{\tilde{a}}) \in \tilde{\mathcal{G}}$ are left and right gradients of an arbitrary smooth functional $h \in \mathcal{D}(\tilde{\mathcal{G}}^*)$ at $(\tilde{a} \ltimes \tilde{l}) \in \tilde{\mathcal{G}}^*$, which due to the Adler-Kostant-Symes theory generates the hierarchy of Hamiltonian flows on $\tilde{\mathcal{G}}^* \simeq \tilde{\mathcal{G}}$ in the form $\partial(\tilde{a} \ltimes \tilde{l})/\partial t_p = \{\tilde{a} \ltimes \tilde{l}, h^{(p)}(\tilde{a} \ltimes \tilde{l})\}_{\mathcal{R}}$, $p \in \mathbb{Z}_+$, where $h^{(p)}(\tilde{a} \ltimes \tilde{l}) = \lambda^p h(\tilde{a} \ltimes \tilde{l})$, for the Casimir invariant $h \in I(\tilde{\mathcal{G}}^*)$. The reductions of this hierarchy on polynomial type coadjoint orbits of the Lie algebra $\tilde{\mathcal{G}}$ are shown to lead to hierarchies of compatibly bi-Hamiltonian $(2|N + 1)$ -dimensional systems on functional supermanifolds.

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Session Classification: MATHEMATICS

Track Classification: MATHEMATICS

Contribution ID: 117

Type: **Oral**

Polarization mechanism of bacteria motion in aquatic media

Thursday, 26 September 2024 13:10 (20 minutes)

A new mechanism is proposed to explain the reasons for the bacteria's motion in the aquatic environment. The mathematical model of this mechanism is based on the hydrodynamic equations of active matter and takes into account the dynamics of the environment polarization and polarization of individual bacteria. It is assumed that the flow of light and the active motion of dielectric regions with different refractive indices inside the bacterium lead to the formation of a nonuniform distribution of dipole moments at the interface between the bacterium and the aqueous medium. This distribution is nonequilibrium and evolves along the bacterium and rotates. The interaction of this distribution with the environment due to surface deformation or due to ponderomotive force leads to the bacteria's motion. Such a motion can be represented as a type of turbine effect without attachment or as an interaction of the polarization current with a change in the local polarization of the medium. This mechanism differs significantly from the flagella motion mechanism and can explain the motility of flagellate bacteria. In addition, such a mechanism depends on the concentration of charged particles in the medium. Namely, with an increase in their concentration, the polarized region motion increases, which creates a greater bacterial surface deformation and causes a redistribution of polarization. Moreover, the collective bacteria motion can cause water mixing.

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Presenter: Dr CHERNIAK, Oleksandr (Bogolyubov Institute for Theoretical Physics)

Session Classification: Morning Session 3

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 118

Type: **Poster**

Subensembles of magnetized particles in random electric fields

Tuesday, 24 September 2024 16:30 (5 minutes)

Transport processes of a passive scalar in random velocity fields are observed in plasma systems, atmosphere, oceanic currents, etc. The task of the theoretical description is to reproduce the temporal evolution of an ensemble of particles moving in such a field based on the known statistical characteristics of the velocity or force fields. The most known example is Brownian motion, the feature of which is the presence of two time scales. That is, the time of collisions, or the time of correlations of random fields, is much shorter than the time of system, or the particle distribution function, evolution. Then, as is known, the mean squared displacement of the particles, or the second moment of the distribution function, is proportional to the system evolution time. The distribution of particles, which at the initial moment of time were concentrated at the origin of the coordinates, preserves the Gaussian shape, which evolves according to the mean squared displacement, and the particle diffusion coefficient in such fields is a constant value.

More complicated and more interesting is the transport of particles in random fields, the correlation time of which is not small compared to the time of evolution of the system. An example of such a system is charged particles drifting in a random electric field across a constant magnetic field. The equations of motion become statistically nonlinear, and the evolution of dispersion from a short initial ballistic regime, namely quadratic dependence on time, changes asymptotically to a fractional power law. Accordingly, the distribution of particles is not Gaussian, and the diffusion coefficient changes over time.

The feature of such a system is that the two-dimensional drift of particles occurs along equipotential lines or streamlines. The presence of such an integral of motion allows for dividing the complete ensemble of particles into separate groups named subensembles, which are concentrated near streamlines with a certain value of potential. Observation of subensembles allows a better understanding of how the transport occurs as a whole. In this work, the behavior of the moments of the particle distribution function was studied using simulation for subensembles with the same initial value of the random potential, in particular, the mean squared displacement and excess kurtosis were calculated. It is shown that in each subensemble there are particles that travel far from the initial position and that remain close to it. The distribution of the displacement of particles depending on the initial value of the potential was found, and the average displacements and velocities for the sub-ensembles were calculated. It was found that the mean square displacement of the entire ensemble of particles is formed from the partial contributions. The obtained statistical characteristics of particle motion are useful for the verification of analytical models.

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Session Classification: Poster Session

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 119

Type: Oral

Methods of Neutron Optics for Studying Physical Properties of Liquids

Tuesday, 24 September 2024 14:30 (40 minutes)

This presentation is aimed at using neutron optics methods to study the physical properties of bulk and confined liquids. To achieve this goal, the defining idea of M.M. Bogolyubov regarding the hierarchy of relaxation times and the sequential description of the dynamic evolution of condensed systems was used [1]. The following results were obtained by the methods of neutron optics [2-6], which apply the Schrödinger equation for the neutron wave function and the Fermi potential depending on the local numerical value of the density of nuclei [2]:

1. For bulk liquids, the singular behavior of the temperature derivative for the diameter of the neutron refractive index (NRI) is theoretically predicted, the main reason for which is a violation of the Polyakov conformal invariance hypothesis on the coexistence curve of a real liquid-vapor system.
2. Due to the spatial inhomogeneity of the bulk fluid near the critical state in the external gravitational field (see, for example, [7,8]), the appearance of a uniaxial ellipsoid of the NRI has been proven (by analogy with the ellipsoid of wave normals in crystal optics). The parameters of such an ellipsoid were determined for a cylindrical volume of liquid with a radius significantly larger than the correlation length of density fluctuations. On the axis of such a cylindrical sample, the uniaxial NRI ellipsoid becomes the NRI sphere.
3. Different signs of the coherent scattering length of the components of the solution of liquids predict the phenomenon of zero refraction of the neutron beam, which resembles the zero optical activity of a racemic mixture. Theoretical calculations established that for a binary solution of ethane and carbon dioxide, the phenomenon of zero refraction of the neutron beam should take place in the solution of [6].
4. It was theoretically established that the temperature dependence of the peak width of quasi-elastic scattering of slow neutrons is quantitatively confirmed by experimental results for confined supercooled water with spatial dimension $d = 2$ near its lower critical temperature $T = 2280\text{C}$ [9].
5. Using Mandelbrot's formula [10] for the fractal dimension, it was proved that the dependence of the cross section of the elastic neutron scattering, being proportional to the random mean-square fluctuation of the number density of nuclei, on linear sizes of a confined liquid volume is determined by a new critical index, which is equal to the fractal dimension. For systems that belong to the universality class of the Ising model in a magnetic field, the fractal dimension values are 1.875 and 2.482, respectively, for spatial dimensions $d = 2$ and $d = 3$ [11].
6. It has been proven that the method of quasi-elastic neutron scattering [4,6] makes it possible to create a reliable basis for new diagnostic tests of the carcinogenesis process based on the established correlation between the self-diffusion coefficient of water molecules in aqueous suspensions of plasma membranes and the sensitivity of different groups of tissues to anticancer drugs [12]. Another biomedical application of neutron optics methods is the calculation of NRI and refraction of a neutron beam in an aqueous suspension of proteins and lipids.

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Session Classification: Afternoon Session 1

Track Classification: CONDENSED MATTER PHYSICS

Contribution ID: 120

Type: **Oral**

Elastic form factors of light alpha-cluster nuclei

Thursday, 26 September 2024 14:50 (20 minutes)

Within the α -particle model, the structure of ^{12}C , ^{16}O , and ^{20}Ne nuclei is studied. With the use of the variational method with Gaussian basis, the wave functions are found for three-, four-, and five-particle systems consisting from α -particles. The charge density distributions and elastic form factors of ^{12}C , ^{16}O , and ^{20}Ne nuclei are calculated within the Helm approximation.

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Session Classification: Afternoon Session 3

Track Classification: HIGH ENERGY PHYSICS AND NUCLEAR MATTER

Contribution ID: 121

Type: **Oral**

Properties of multi-qubit states representing directed graphs and their studies with quantum programming

Tuesday, 24 September 2024 11:40 (20 minutes)

We analyze multi-qubit states that can be represented using directed graphs $G(V,E)$. We focus on the geometric properties of these states, namely on curvature and torsion [1]. It has been found that the curvature of quantum states is determined by the sum of the weighted degrees of nodes in graphs where the weights in $G(V,E)$ are raised to the second and fourth powers [2]. Additionally, curvature depends on the sum of the products of the weights of edges that form squares within the graph $G(V,E)$. The torsion, on the other hand, is connected to the sum of the products of the weights of edges that create triangles in the graph $G(V,E)$. We have computed these geometric properties on IBM's quantum computer in the case of a quantum graph state corresponding to a chain [2].

We have also examined quantum states that represent directed networks. We calculated the entanglement of these states both analytically and by programming on AerSimulator. We identified relationships between the geometric measure of entanglement and the weights of incoming and outgoing arcs, the outdegree, and indegree of the vertex corresponding to the qubit in the graph [3].

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Session Classification: Morning session 1

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 122

Type: **Poster**

Graph Structural Complexity

Tuesday, 24 September 2024 16:20 (5 minutes)

Introduced the quantitative measure of the structural complexity of the graph (complex network, etc.) based on a procedure similar to the renormalization process, considering the difference between actual and averaged graph structures on different scales. The proposed concept of the graph structural complexity corresponds to qualitative comprehension of the complexity. The proposed measure can be obtained for the weighted graphs also.

The structural complexities for various graph types were found – the deterministic infinite and finite size graphs, artificial graphs of different natures including percolation structures, and the time series of cardiac rhythms mapped to complex networks using the parametric visibility graph algorithm. The latter reaches a maximum near the formation of a giant component in the graph or at the percolation threshold for 2D and 3D square lattices when a giant cluster having a fractal structure has emerged. Therefore, the graph structural complexity allows us to detect and study the processes similar to a second-order phase transition in complex networks.

A new node centrality index, characterizing the structural complexity of a certain node within the graph structure is introduced also, it can serve as a good auxiliary or generalization to the local clustering coefficient. Such an index provides another new ranking manner for the graph nodes. Being an easily computable measure, the graph structural complexity might help to reveal different features of complex systems and processes of the real world.

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Session Classification: Poster Session

Track Classification: STATISTICAL PHYSICS AND KINETIC THEORY

Contribution ID: 123

Type: **not specified**

Conference opening

Tuesday, 24 September 2024 10:00 (20 minutes)

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Session Classification: Morning session 1