

Geometric Singularities, Moduli Stabilization, and Gravitational Wave Signatures in String Compactifications

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We present a unified framework connecting Calabi–Yau geometry, singularity theory, and early-universe cosmology within heterotic and Type IIB string compactifications. Starting from the Tian–Yau threefold defined by its complete-intersection configuration matrix $P^3 \begin{bmatrix} 3 & 0 & 1 \\ 0 & 3 & 1 \end{bmatrix}$, we demonstrate how a free $\mathbb{Z}_3$ quotient reduces the Euler characteristic to $\chi = -6$, yielding precisely three chiral generations. By embedding a stable $SU(4)$ vector bundle with $c_1(V) = 0$ and $c_2(V) = 12 \leq c_2(TX) = 50$, we satisfy the Green–Schwarz anomaly cancellation condition while preserving $N = 1$ supersymmetry and enabling Wilson-line breaking of E_6 to the Standard Model gauge group.

A central result is the identification of universal singularity structures governing vacuum transitions. Generic multi-field scalar potentials correspond to non-simple singularities with Milnor number $\mu = 9$, but near critical degeneracy loci the Hessian vanishes and the system universally reduces to an A_2 cusp with $\mu = 2$ [1]. This reduction controls the dynamics of first-order phase transitions in the early universe. We derive the stochastic gravitational-wave spectrum generated near these critical points, showing that potential flattening enhances the signal amplitude as $\Omega_{\text{GW}} \propto \delta^{-3}$, where $\delta = 1 - \hat{\xi}/\hat{\xi}_c$ measures the distance to criticality. The predicted peak frequencies naturally lie in the milli-Hertz band, and benchmark points satisfying strong first-order transition criteria yield $\Omega_{\text{GW}} h^2 \sim 10^{-12} - 10^{-11}$, placing them directly within the sensitivity window of the LISA mission.

We systematically analyse the KKLT moduli stabilisation mechanism [2] incorporating leading α'^3 corrections to the Kähler potential. The correction breaks the classical no-scale structure and generates three distinct vacuum regimes separated by a critical threshold $\hat{\xi}_c$. For $\hat{\xi} < \hat{\xi}_c$, controlled AdS minima persist and can be uplifted to metastable de Sitter vacua; for $\hat{\xi} > \hat{\xi}_c$, the potential exhibits runaway behaviour characteristic of the Large Volume Scenario or decompactification. The conifold transition mechanism [3], where massless black holes resolve geometric singularities via flop transitions, provides a dynamical pathway connecting parent manifolds to the three-generation Tian–Yau/ $\mathbb{Z}_3$ vacuum. We quantify the tension between shallow dS vacua near $\hat{\xi}_c$ and the de Sitter swampland conjecture, mapping the parameter space where controlled string constructions remain consistent with quantum gravity constraints. Detailed derivations, explicit benchmark tables, and the full Hessian analysis are provided in [1]. Our results establish a direct observational bridge between compactification topology, singularity-driven cosmology, and gravitational-wave detectors.

Keywords: String compactification, Tian–Yau threefold, conifold transitions, singularity theory, Milnor number, KKLT mechanism, α'^3 corrections, gravitational waves, LISA, de Sitter swampland conjecture.

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