

MAGIC

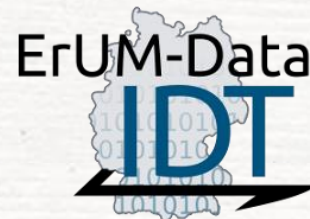
Matter, **A**strophysics, **G**ravitationalwaves & **I**on **C**ollisions

A. Motornenko, M.O. Kuttan, E. Most, J. Papenfort, L. Weih, L. Rezzolla, ITP

M. Hanauske**, *St. Schramm*[†], J. Steinheimer, H. Stoecker*, FIAS

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*GSI Darmstadt, CCNU, Wuhan; HU, Huzhou; USTC, Hefei



Matter, Gravity and Neutron Stars

1915 **A. Einstein**, born in Ulm, published GR:

Gravity governs the motion of masses and light by curving spacetime.

1915 **Karl Schwarzschild**,

born 1873 in Frankfurt am Main,

found the static point source solution of the theory of GR: BHs !

1916 K.S.' last article: "Neutron Star" solution of GR: NS !

SchwarzSchild died in WW I just after publishing these articles..

SchwarzSchild's solutions of GR: **black holes & neutron stars**

Add Einstein's **Gravitational Waves** - we see a whole new Universe!



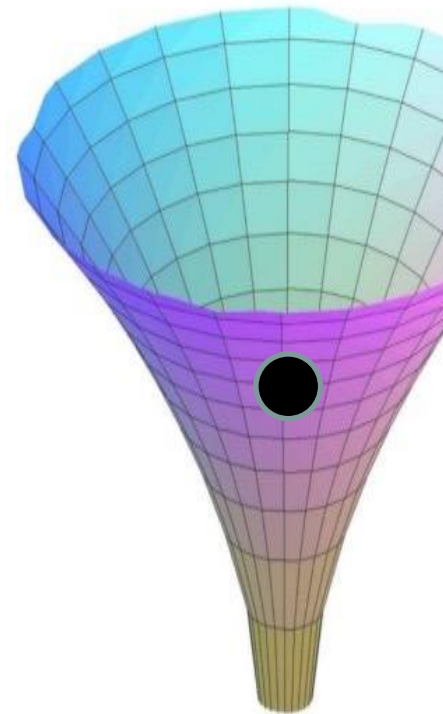
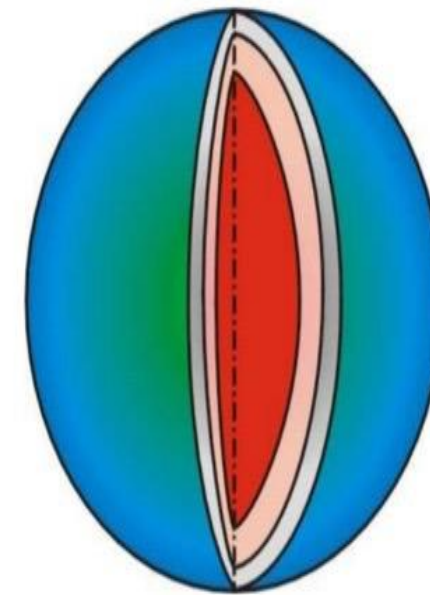
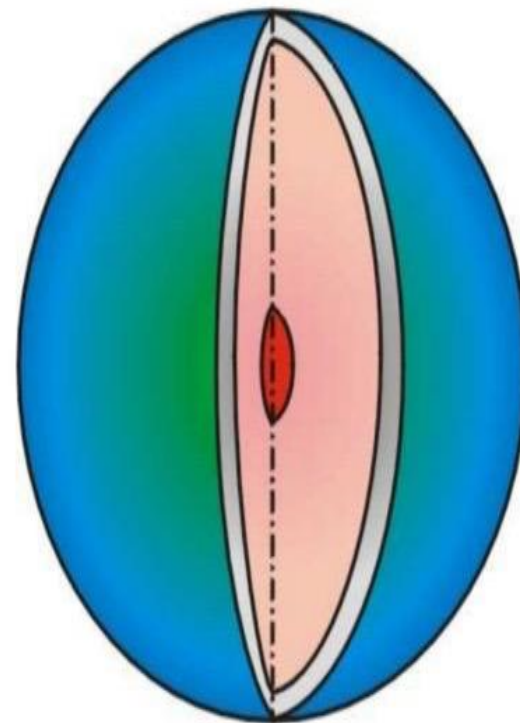
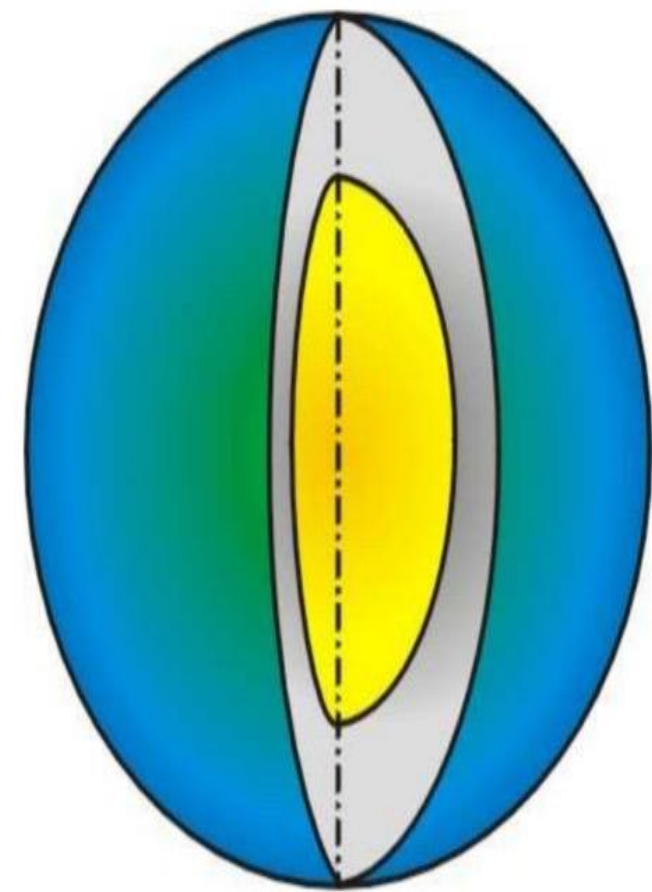
Neutron Star, Quark Star, Black hole ?

Neutron Stars

Hybrid Stars

Quark Stars

Black Holes



$$\rho_c = \rho_0$$

$$\approx 2 \rho_0$$

$$\approx 5 \rho_0$$

... ∞

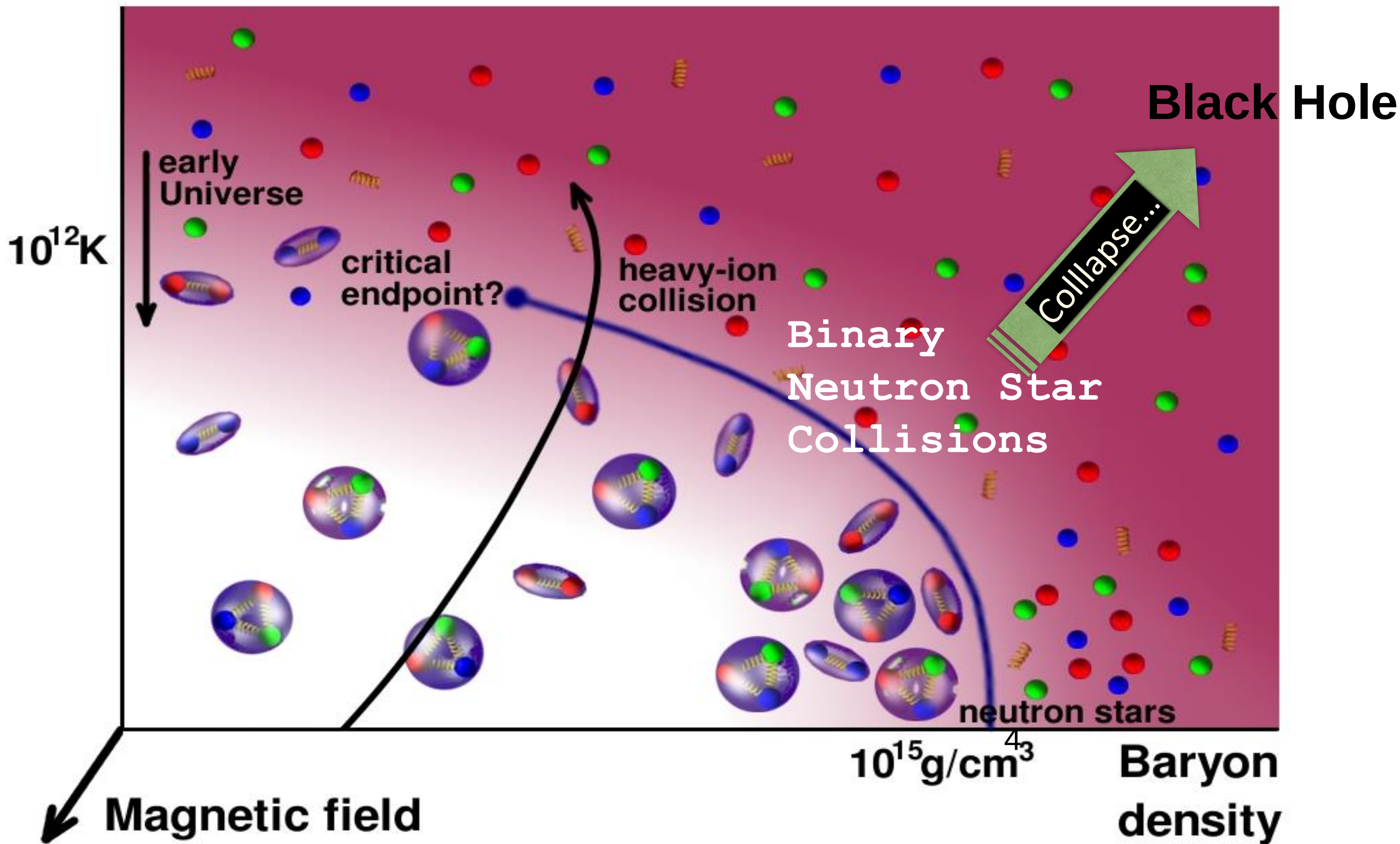
central density ρ_c in the star

$$(\rho_0 := 0.15/\text{fm}^3)$$

Dense Matter, Strange Matter, Quark Matter, Quark Stars?

FAIR: Relativistic collisions of Heavy Ions vs. BNS-NSC

Temperature



Chiral $SU(3)_f$ parity-doublet Polyakov-loop quark-hadron model

- **Chiral** — chiral symmetry restoration among parity partners and in the quark sector, chiral field is a proxy interaction between quarks and hadrons
- **$SU(3)$** — 3-flavor (**u**, **d**, **s**) chiral Lagrangian: respective baryon octet interacts through mesonic fields. Realization of **σ - ω** model.

P. Papazoglou et al., nucl-th/9706024

- **parity-doublet** — parity doubling among the baryon octet

C. E. Detar and T. Kunihiro, Phys.Rev. D39 (1989)

T. Hatsuda and M. Prakash, Phys.Lett. B224 (1989)

G. Aarts et al., 1703.09246 and 1812.07393

- **quark-hadron** — realization of the deconfinement, PNJL-like

K. Fukushima, hep-ph/0310121

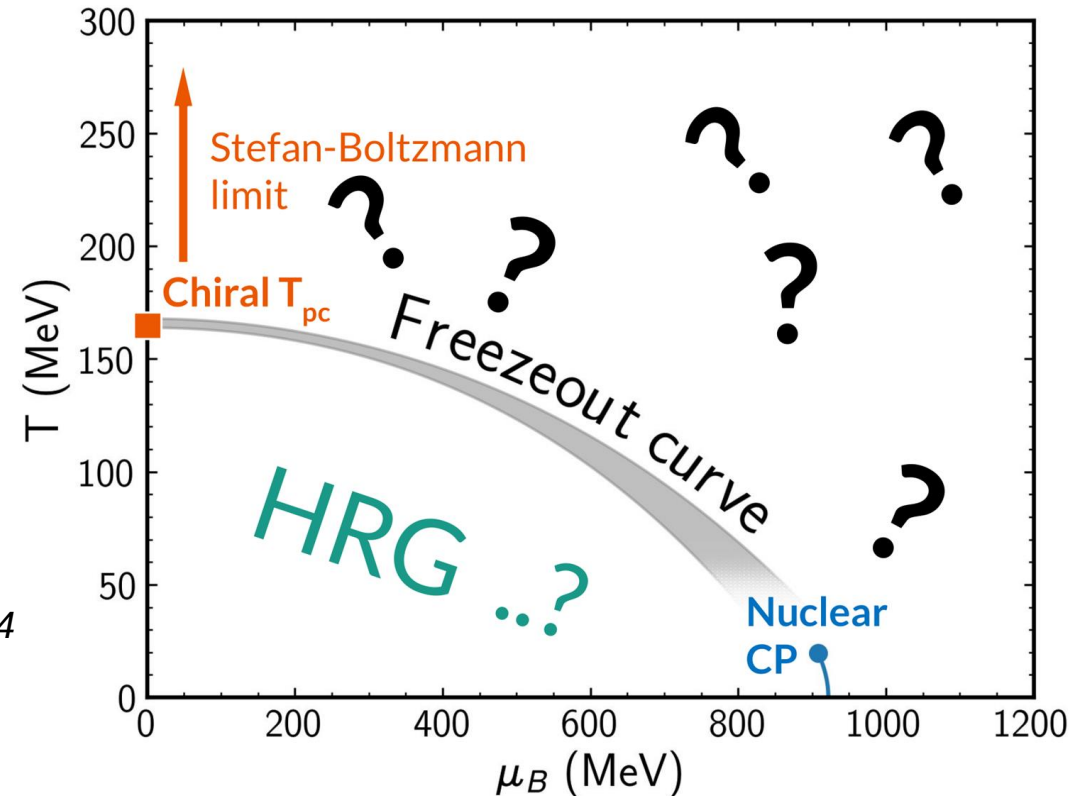
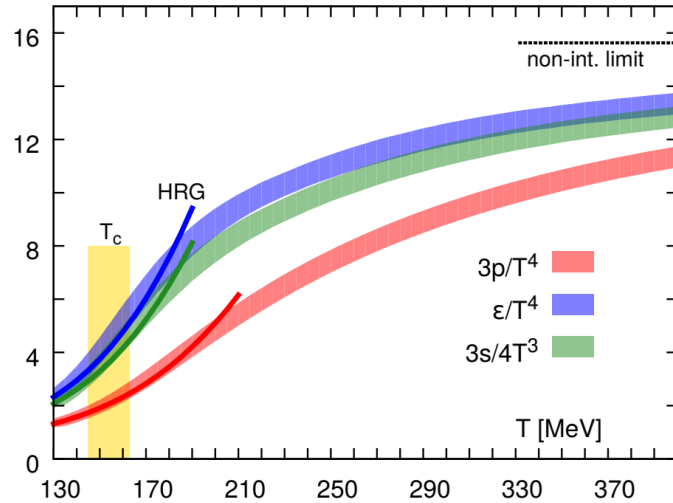
C. Ratti, M.A. Thaler, W. Weise, hep-ph/0506234

J. Steinheimer, S. Schramm, H. Stoecker, 1009.5239

A **single framework** for QCD thermodynamics, **simultaneously** satisfies constraints from **lattice QCD** and known **nuclear matter properties**, as well as **neutron star** observations.

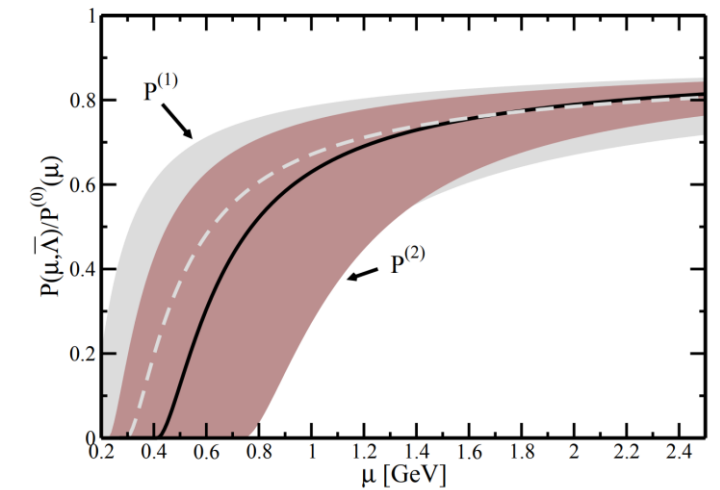
QCD phenomenology for the EoS

Stefan-Boltzmann limit $\mu_B=0$ HotQCD, 1407.6387

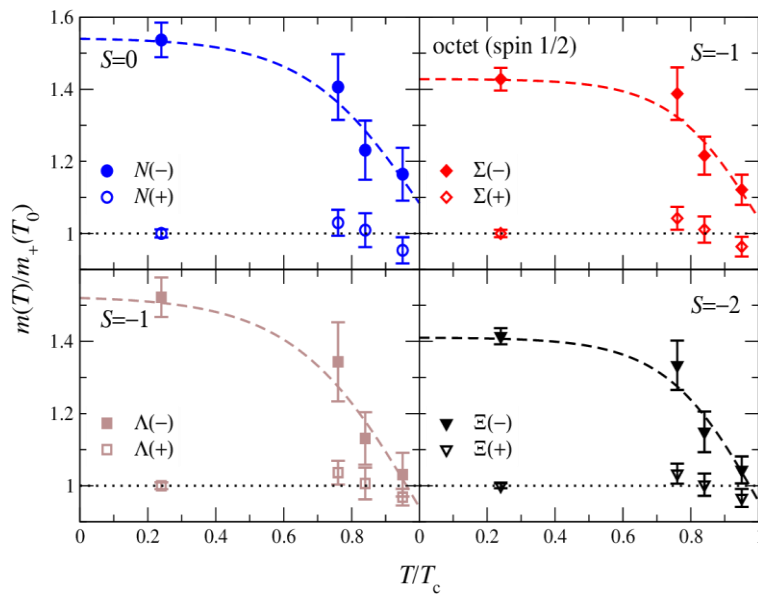


Stefan-Boltzmann limit $T=0$

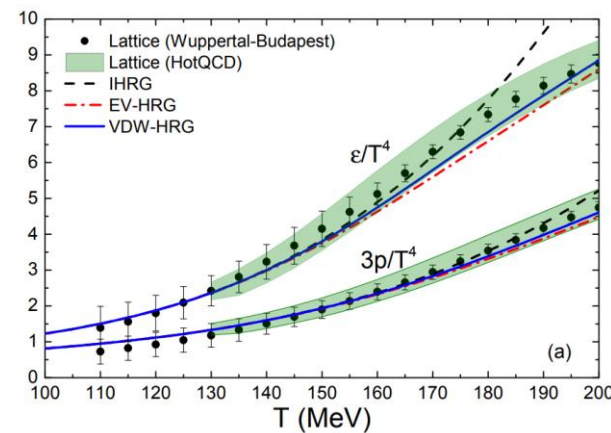
A. Kurkela, P. Romatschke,
A. Vuorinen, 0912.1856



Parity doubling G. Aarts et al., 1710.08294



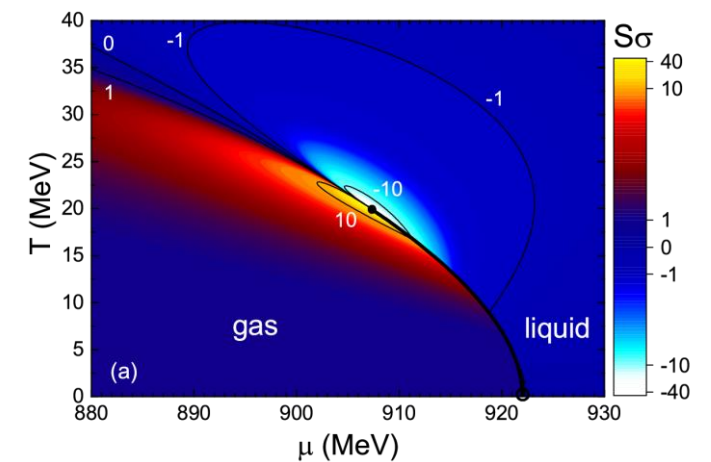
Hadron Resonance Gas



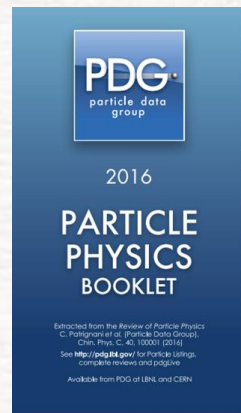
Vovchenko,
Gorenstein,
Stoecker,
1609.03975

Nuclear matter properties

J. Pochodzalla et al., Phys.Rev.Lett. 75 (1995),
V. Vovchenko et al., 1506.05763



Hadronic part: QCD matter at low densities



$$\rho_i = \frac{\rho_i^{\text{id}}(T, \mu_i^* - v_i p)}{1 + \sum_j v_j \rho_j^{\text{id}}(T, \mu_j^* - v_j p)}$$
$$\varepsilon_i = \frac{\varepsilon_i^{\text{id}}(T, \mu_i^* - v_i p)}{1 + \sum_j v_j \rho_j^{\text{id}}(T, \mu_j^* - v_j p)}$$

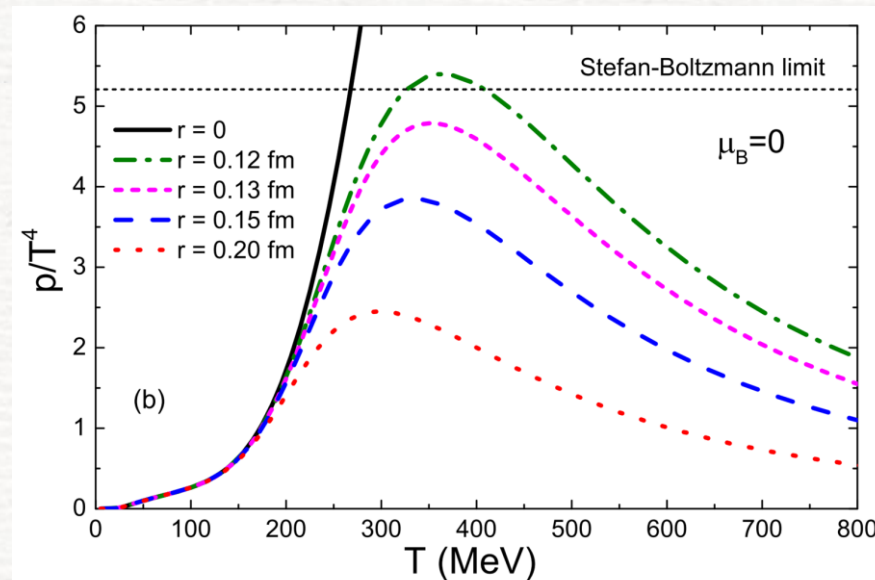
PDG list of known hadrons is included with Excluded Volume interactions.

EV suppress hadrons at high energy densities.

EV of baryons: 1 fm^3

EV of mesons: $1/8 \text{ fm}^3$

EV triggers the switch between hadron and quark degrees of freedom: **hadron** pressure is **suppressed** as function of T and μ_B — quarks are dominant at high densities.



V. Vovchenko, D. Anchishkin, M. Gorenstein, 1412.5478

SU(3)_f octet and parity doubling: nuclear matter and lattice

We include all states of the **SU(3)_f** baryon octet:

$$\begin{pmatrix} \frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & \Sigma^+ & p \\ \Sigma^- & -\frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & n \\ \Xi^- & \Xi^0 & -2\frac{\Lambda}{\sqrt{6}} \end{pmatrix}$$

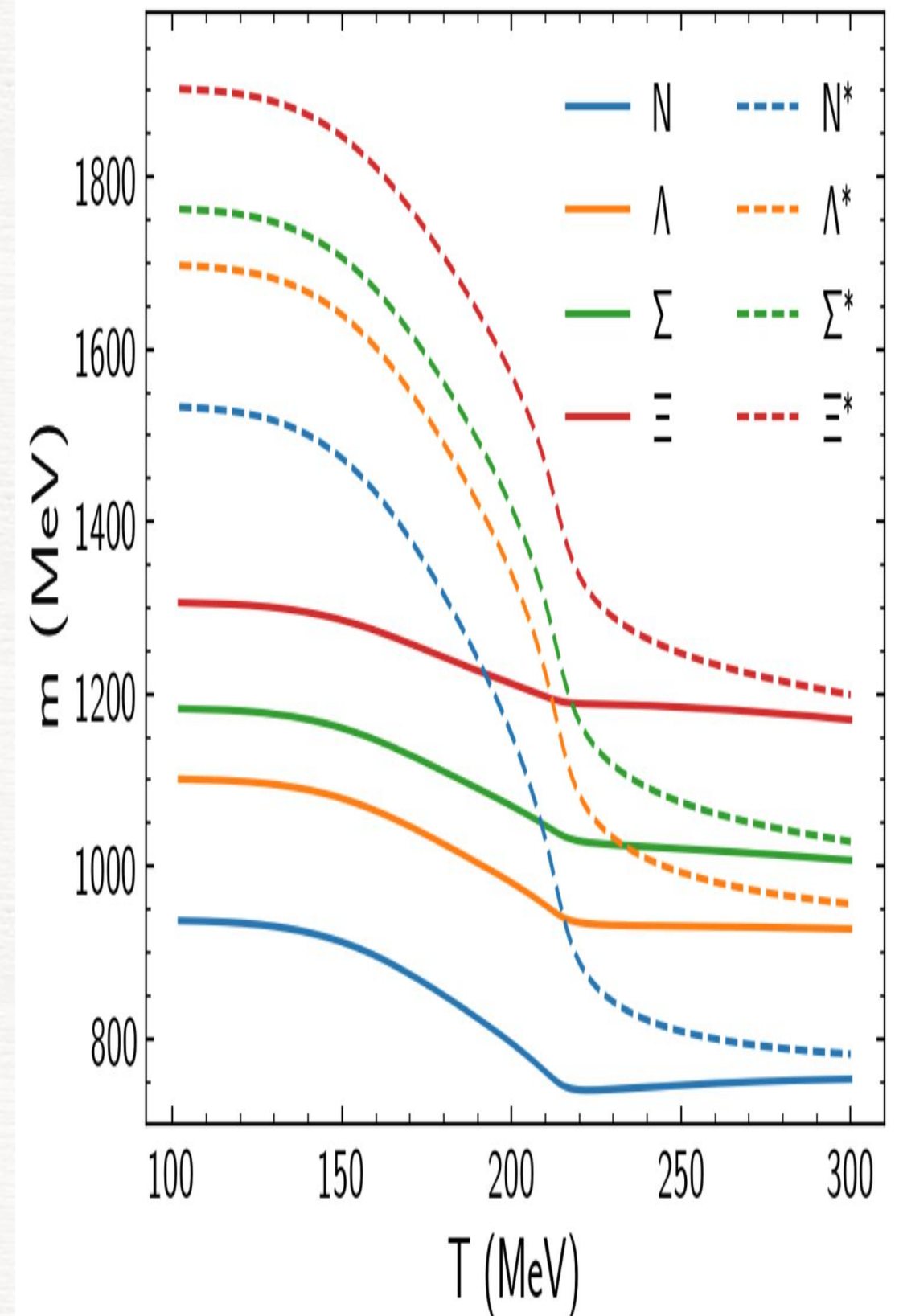
together with their **parity partners** (G. Aarts et al., 1710.08294), i.e. states with the same quantum numbers but **opposite parity**. Those interact within SU(3)_f σ model:

$$\begin{aligned} \mathcal{L}_B = & \sum_i (\bar{B}_i i \not{\partial} B_i) + \sum_i (\bar{B}_i m_i^* B_i) \\ & + \sum_i (\bar{B}_i \gamma_\mu (g_{\omega i} \omega^\mu + g_{\rho i} \rho^\mu + g_{\phi i} \phi^\mu) B_i) \end{aligned}$$

with effective masses generated by chiral fields **σ** and **ζ** :

$$m_{i\pm}^* = \sqrt{[(g_{\sigma i}^{(1)} \sigma + g_{\zeta i}^{(1)} \zeta)^2 + (m_0 + n_s m_s)^2]} \pm g_{\sigma i}^{(2)} \sigma \pm g_{\zeta i}^{(2)} \zeta$$

‘+’ stands for positive and ‘-’ for negative parity states



Including Quarks: PNJL-like approach

Quarks are included within **PNJL** inspired approach (*Fukushima, hep-ph/0310121*):

$$\Omega_q = -VT \sum_{i \in Q} \frac{d_i}{(2\pi)^3} \int d^3k \frac{1}{N_c} \left[\ln \left(1 + 3\Phi e^{-(E_i^* - \mu_i^*)/T} + 3\bar{\Phi} e^{-2(E_i^* - \mu_i^*)/T} + e^{-3(E_i^* - \mu_i^*)/T} \right) \right. \\ \left. + \ln \left(1 + 3\bar{\Phi} e^{-(E_i^* + \mu_i^*)/T} + 3\Phi e^{-2(E_i^* + \mu_i^*)/T} + e^{-3(E_i^* + \mu_i^*)/T} \right) \right]$$

Polyakov loop Φ — is deconfinement order parameter:

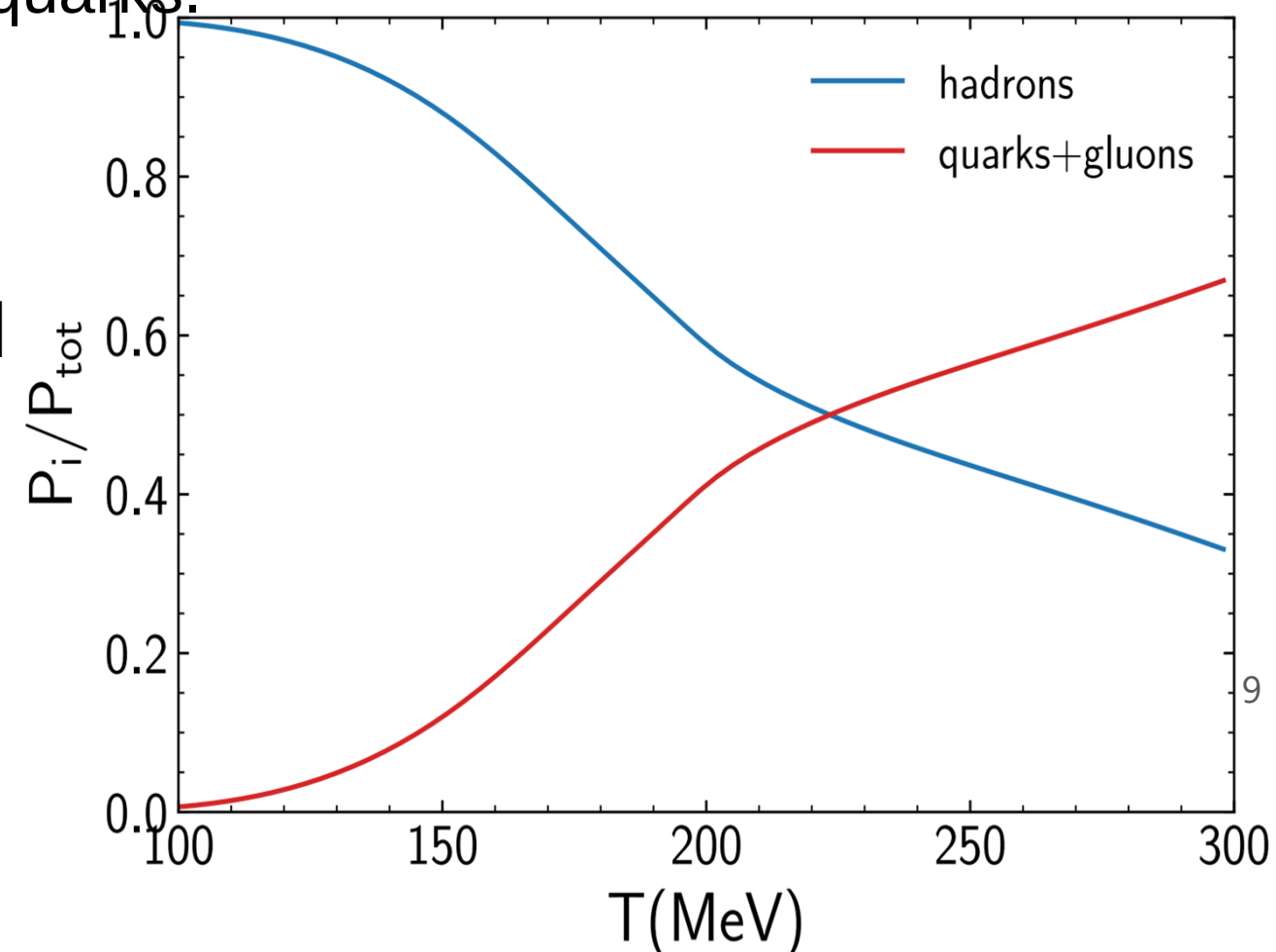
$\Phi=0$ — no quarks, $\Phi=1$ — free quarks.

Φ is controlled by the **potential $U(\Phi)$** :

$$U = -\frac{1}{2}(a_0 T^4 + a_1 T_0 T^3 + a_2 T_0^2 T^2)\Phi\Phi^* \\ + b_3 T_0^4 \log[1 - 6\Phi\Phi^* + 4(\Phi^3 + \Phi^{*3}) - 3(\Phi\Phi^*)^2]$$

Fukushima, hep-ph/0310121

Roessner, Ratti, Weise, hep-ph/0609281

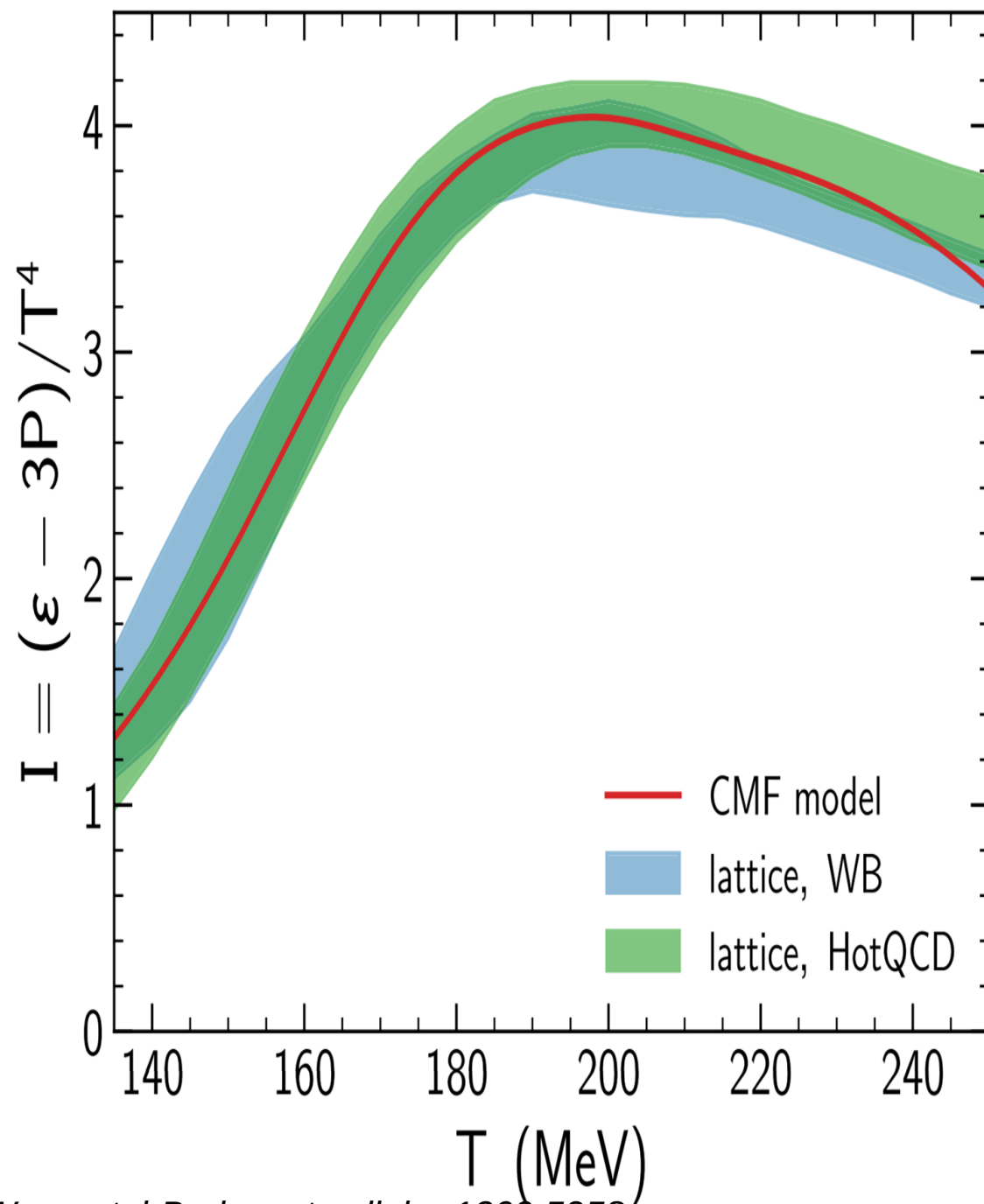


Chiral Mean Field description of QCD matter

- **Chiral SU(3) parity-doublet quark-hadron mean-field model** — **unified phenomenological approach** to model QCD thermodynamics at wide range of scales;
- $\mu_B=0$ lattice QCD data is used to constrain parameters of model's quark sector;
- **Nuclear liquid-vapor** phase transition gives strong signals in fluctuations even at $\mu_B=0$;
- Chiral symmetry restoration and transition to quark-dominated phase are at very **high μ_B and/or T** ;
- Model produces neutron stars in **agreement** with modern constraints;
- Model's EoS can be used as an input for both finite T and $T=0$ **neutron star physics**
- ... as well as for hydro simulations of heavy ions collisions.

Stefan Schramm: “That is most of what is known about QCD phenomenology”

The CMF model and lattice data



Wuppertal-Budapest collab., 1309.5258
HotQCD collab., 1407.6387

The Interaction measure I effectively measures rate of increase/decrease of degrees of freedom ($N_{\text{dof}} \sim p/T^4$) function of temperature (*Fukushima, 0804.3318*):

$$I = \frac{\varepsilon - 3p}{T^4} = T \frac{\partial}{\partial T} \left(\frac{p}{T} \frac{1}{T^3} \right)$$

I is an illustrative quantity for quark appearance.

We reproduce I by fitting coefficients of Polyakov loop potential $U(\Phi)$ and quark couplings $g_{q\sigma}$ and $g_{q\zeta}$ to the chiral fields.

$$m_q^* = -g_{q\sigma}\sigma + \delta m_q + m_{0q},$$

$$m_s^* = -g_{s\zeta}\zeta + \delta m_s + m_{0q}$$

$$U = -\frac{1}{2}(a_0 T^4 + a_1 T_0 T^3 + a_2 T_0^2 T^2)\Phi\Phi^* + b_3 T_0^4 \log[1 - 6\Phi\Phi^* + 4(\Phi^3 + \Phi^{*3}) - 3(\Phi\Phi^*)^2]$$

The CMF model and lattice data, hadron sizes

$$v_B = 1 \text{ fm}^3, v_M = 1/8 \text{ fm}^3, v_{MS} = 1/8 \text{ fm}^3$$

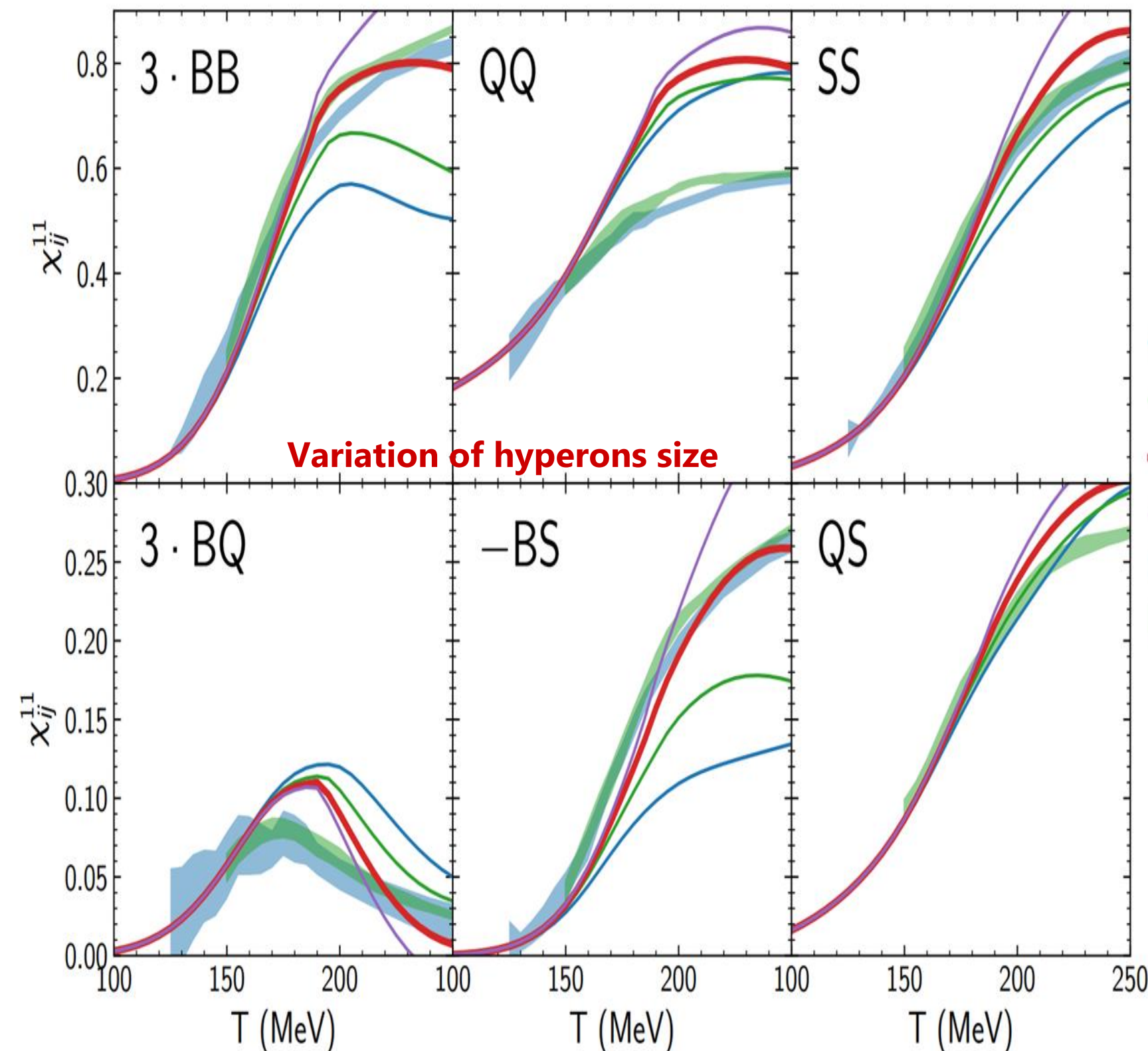
**Motornenko *et al.*,
2009.10848**

The lattice data on second order
**susceptibilities are sensitive to
hadron sizes at $T > T_{pc}$**

$$\chi_{ij}^{11} = \frac{\partial P / T^4}{\partial \mu_i \partial \mu_j}$$

We followed ideas of
Alba *et al.* 1606.06542
and Vovchenko *et al.*
1707.09215 of **flavor-
dependent EV**
interactions, but in
quark-hadron model.

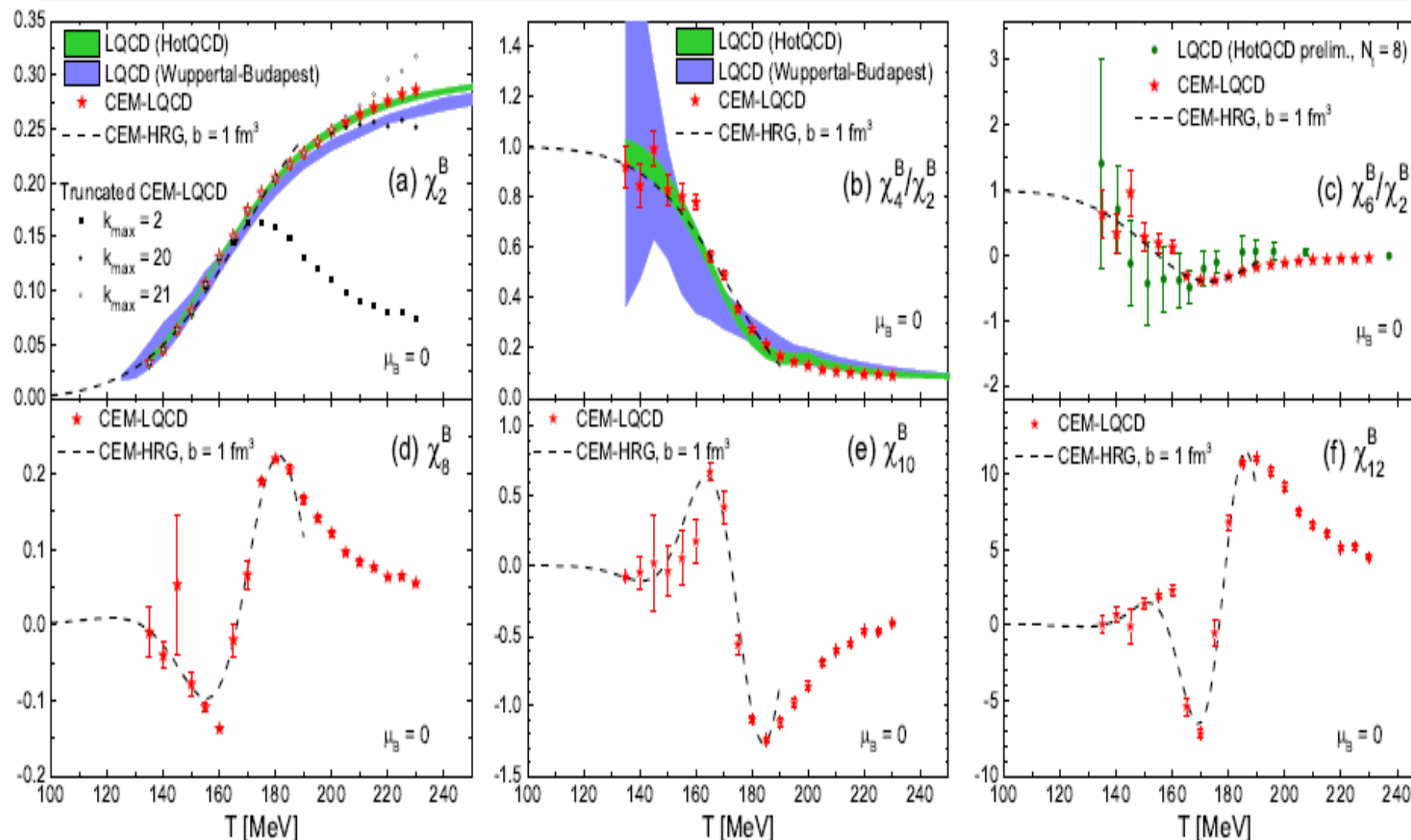
**Smaller EV sizes of hyperons
and mesons as compared to
non-strange baryons help to
describe the lattice data.**



Expansions in imaginary chemical potential

Using only the Fourier coefficients b_k from imaginary μ_B simulations as input:

- One can write the density of QCD as a cluster expansion:
- $\frac{\rho_B}{T^3} = \frac{\partial(p/T^4)}{\partial(\mu_B/T)} = \sum_{k=1}^{\infty} b_k(T) \sinh\left(\frac{k \mu_B}{T}\right)$
- Assuming the proper SB limit and using only the first two coefficients one can exactly predict finite μ_B thermodynamics
- $b_k(T) = \alpha_k \frac{[b_2(T)]^{k-1}}{[b_1(T)]^{k-2}}$. Use these to calculate χ^n .



Results on the applicability

Radius of convergence: $\mu_B/T < \pi$

V. Vovchenko, JS, O. Philipsen and H. Stoecker, Phys. Rev. D **97**, no.11, 114030 (2018)

Beyond the lattice data

The lattice QCD calculations allow to go beyond the $\mu_B = 0$ by using Taylor expansion which involves conserved charge

susceptibilities χ : (Allton *et al.* [hep-lat/0204010](#))

$$P = P_0 + T^4 \sum_{i,j,k} \frac{1}{i!j!k!} \chi_{B,Q,S}^{i,j,k} \left(\frac{\mu_B}{T}\right)^i \left(\frac{\mu_Q}{T}\right)^j \left(\frac{\mu_S}{T}\right)^k$$

$$\chi_{B,Q,S}^{i,j,k} = \frac{\partial^i \partial^j \partial^k P(T, \mu_B, \mu_Q, \mu_S) / T^4}{\partial (\mu_B/T)^i \partial (\mu_Q/T)^j \partial (\mu_S/T)^k}$$

Radius of convergence — distance to the closest singularity of P/T^4 in the **complex μ_B/T plane**, could be QCD critical point.

One singularity is known at

$$\mu_B/T = i\pi$$

Roberge-Weiss transition

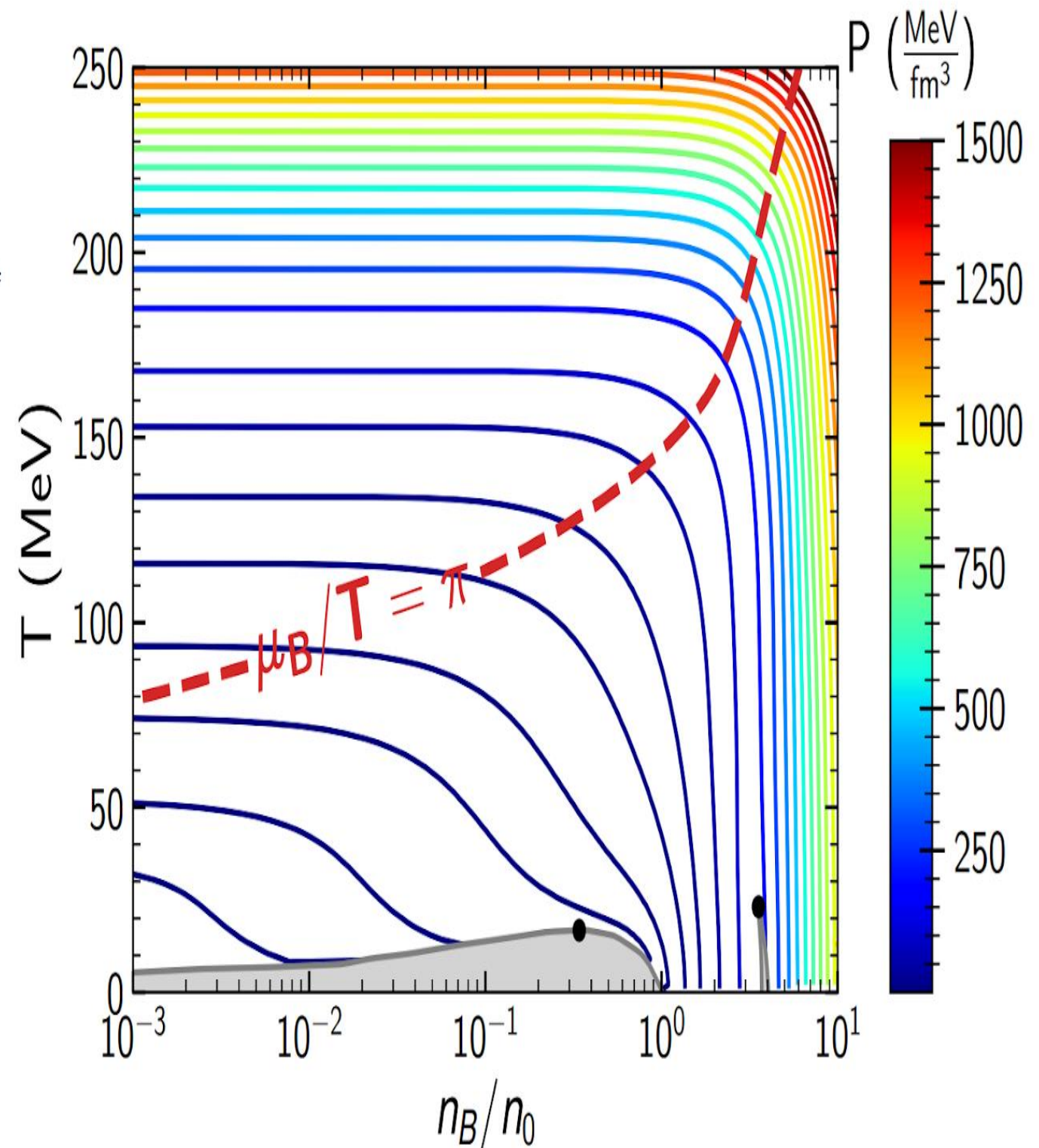
(Roberge, Weiss, *Nucl.Phys.B* 275 (1986) 734-745)

However, estimates suggest $R_{\mu_B/T} \approx 2-3$

(Bazavov *et al.* [1701.04325](#),

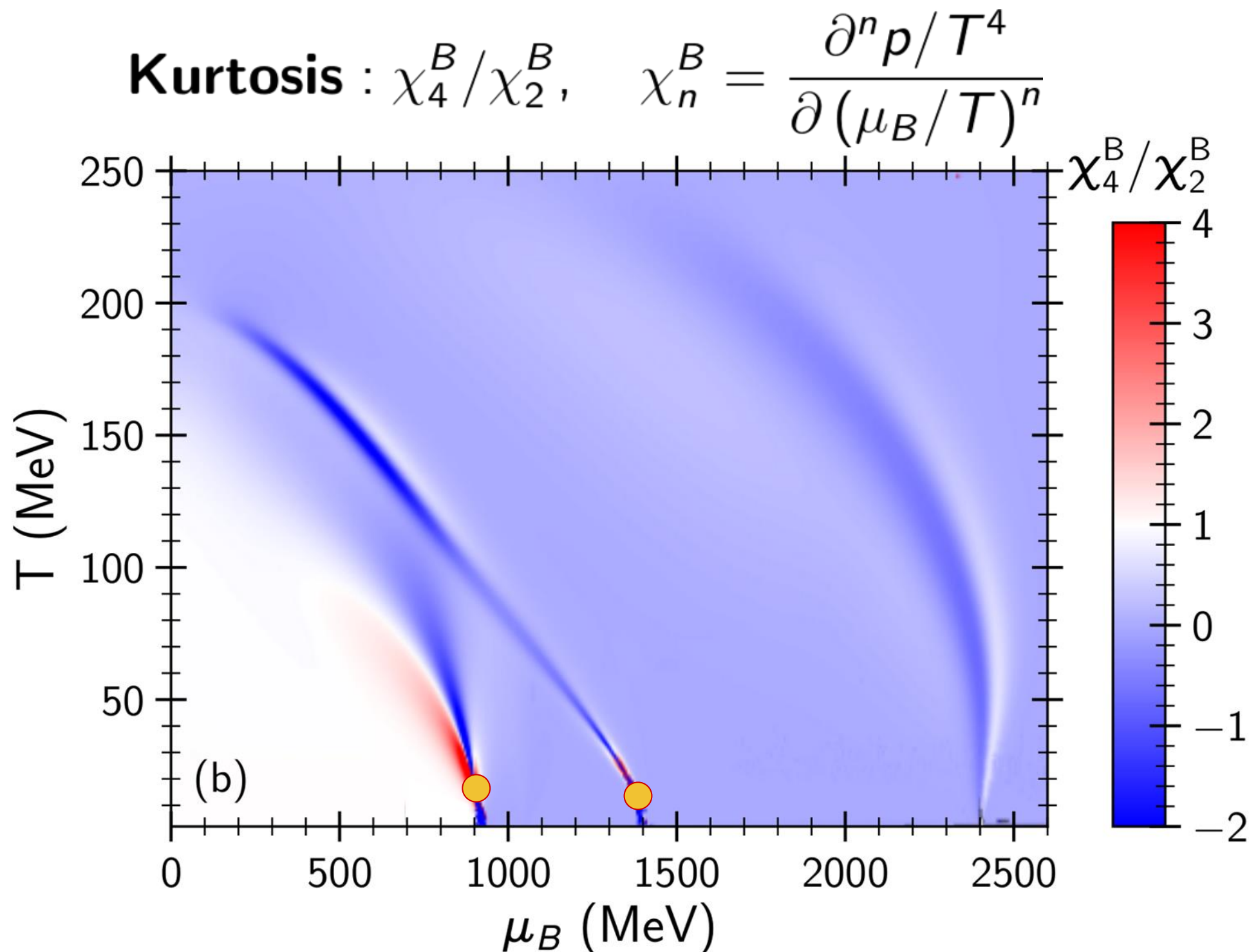
Vovchenko *et al.* [1711.01261](#),

Giordano *et al.* [1911.00043](#))



Lines of constant pressure. The grey shaded regions: mixed phases by nuclear liquid-vapor and chiral phase transitions. Black dots — critical endpoints.

The CMF phase diagram

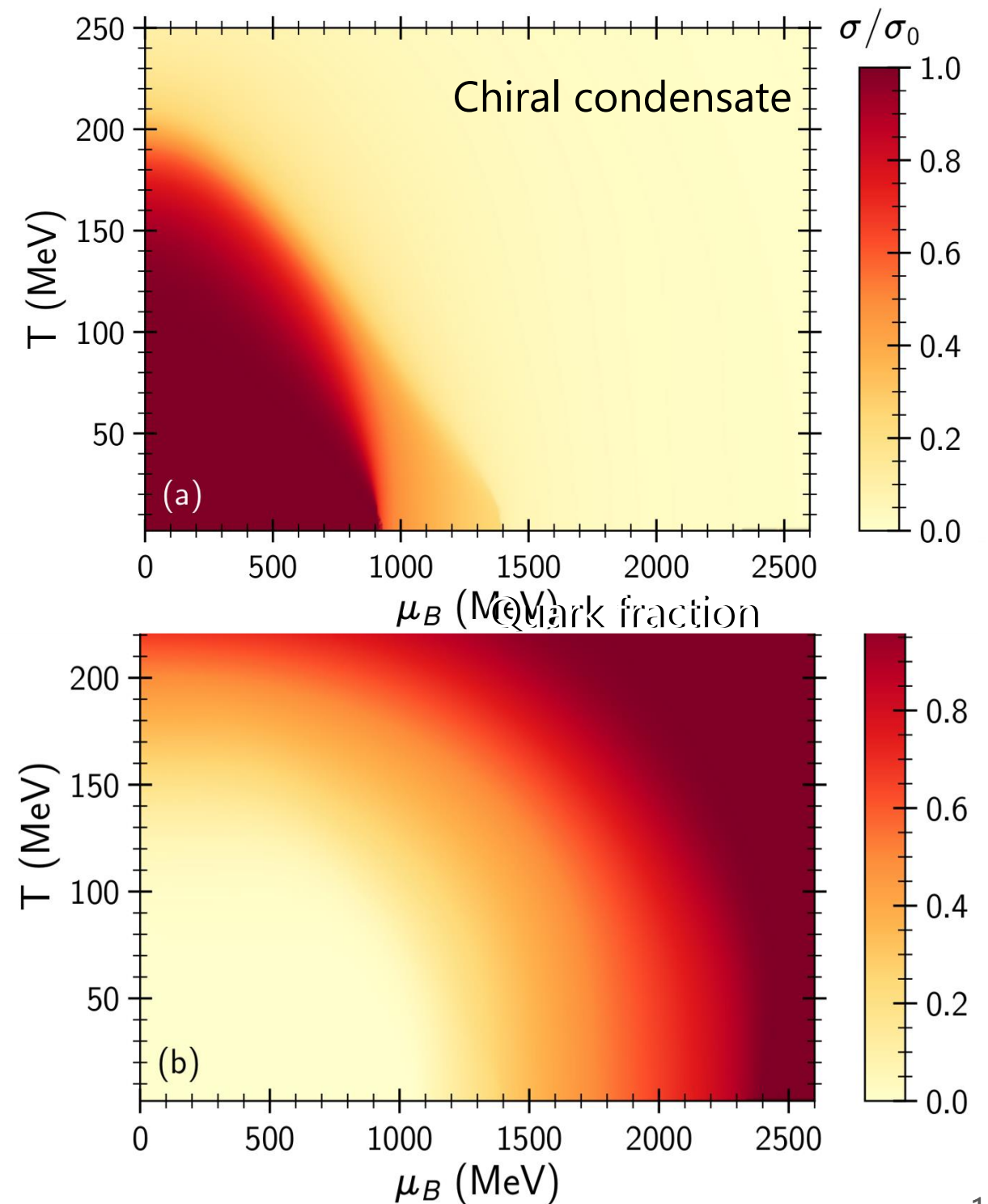
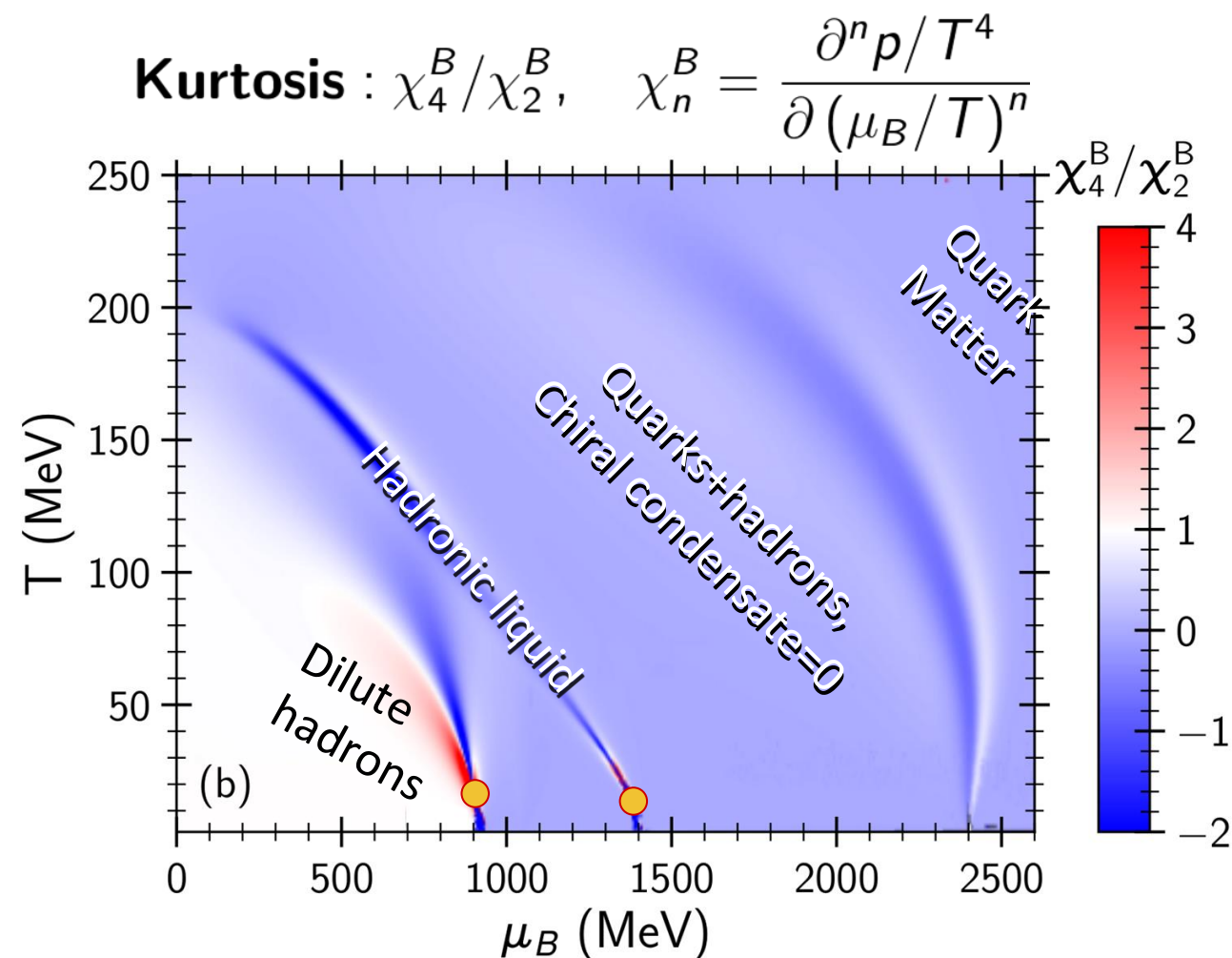


- Remnants of the well established nuclear liquid-vapor transition visible at $\mu_B=0$
- Chiral transition does not change the baseline in kurtosis
- Third transition is always a crossover, transition from quark-hadron mixture
- to **quark matter**

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3 transitions: hadron gas → hadronic liquid → chiral symmetry restoration → quark matter
2 critical points: nuclear CP $T_{CP} \approx 17$ MeV, chiral CP $T_{CP} \approx 17$ MeV

The CMF phase diagram



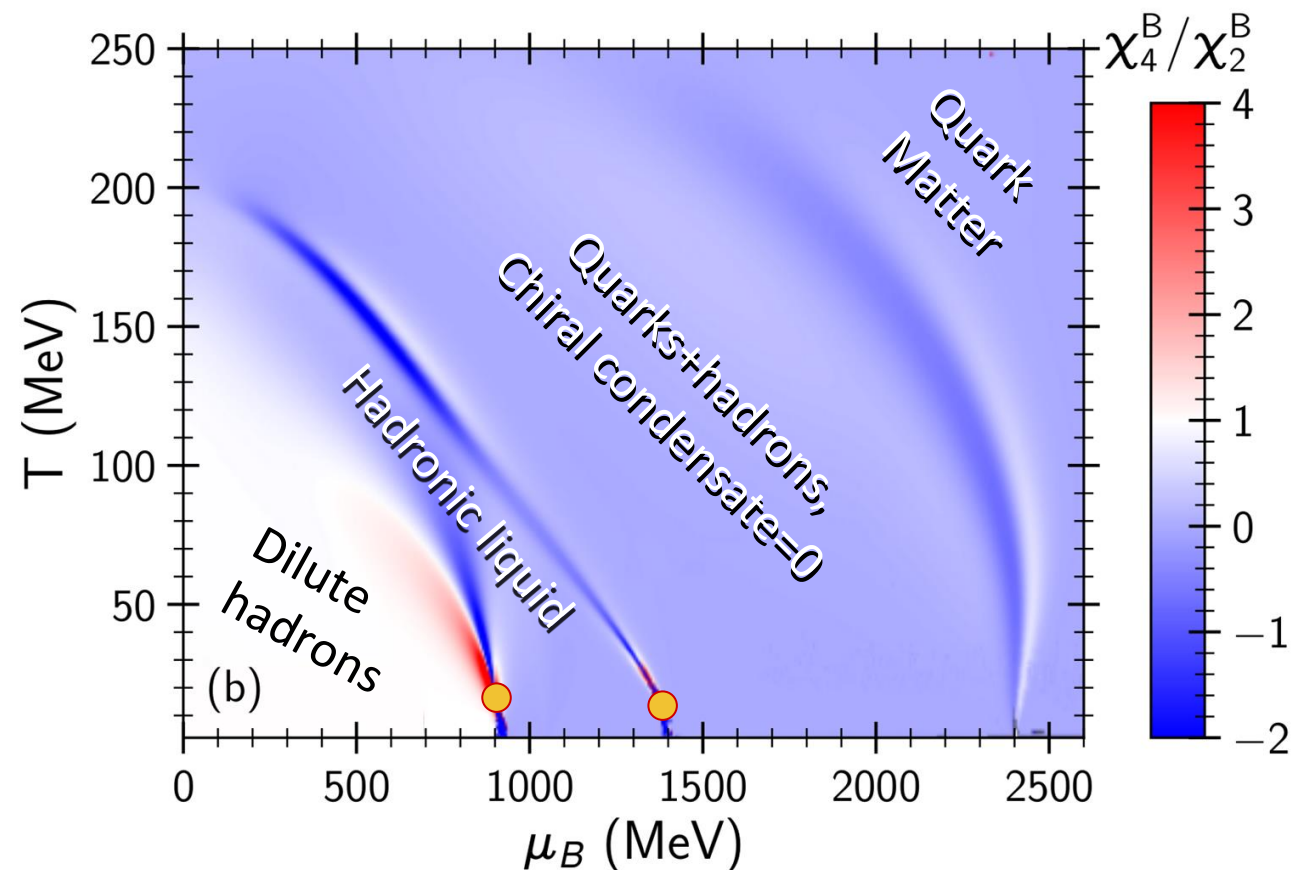
Three transitions:

hadron gas → hadronic liquid → chiral symmetry restoration → quark matter

Two critical points: nuclear CP $T_{CP} \approx 17$ MeV, chiral CP $T_{CP} \approx 17$ MeV

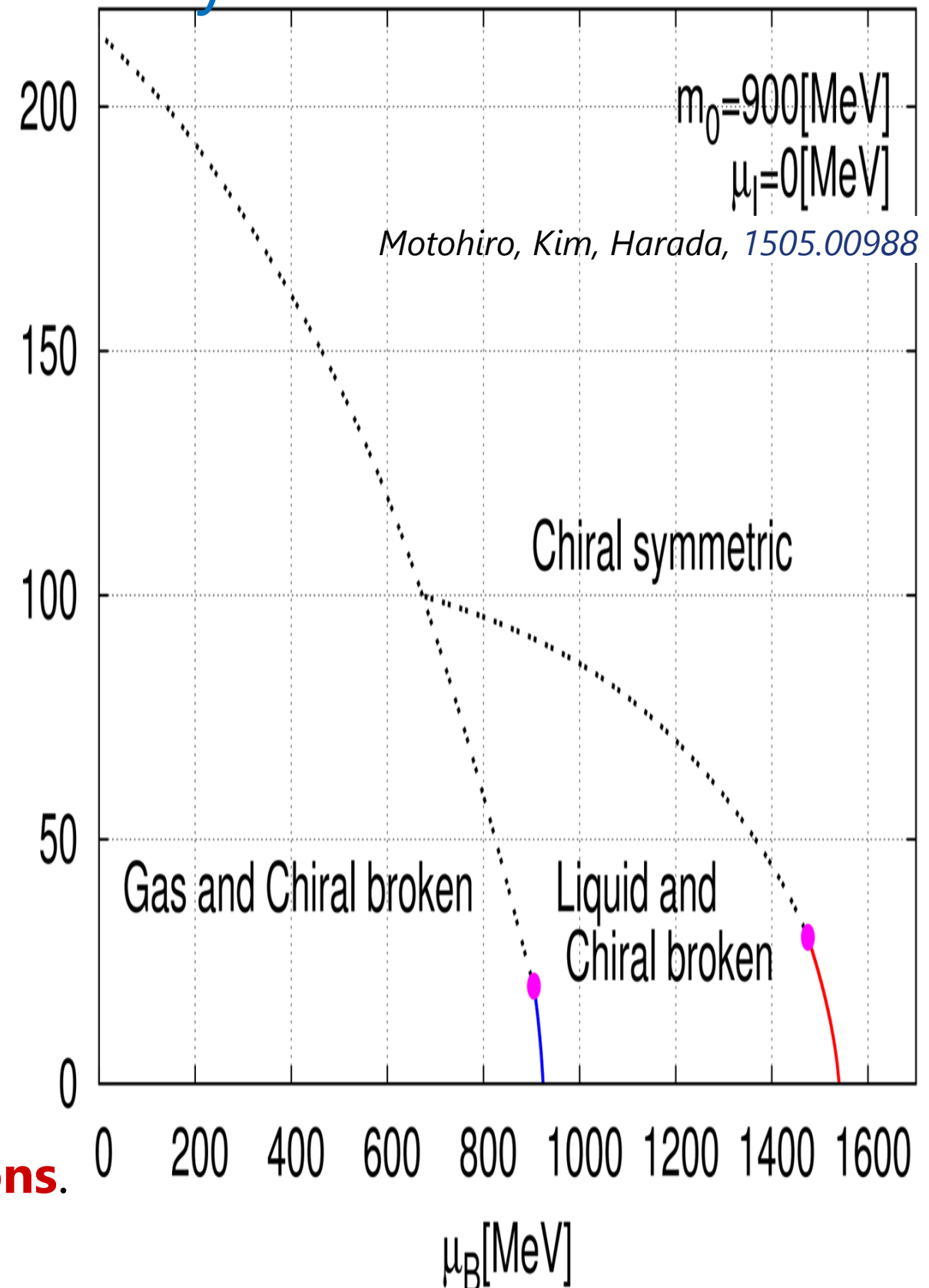
based on [1905.00866](#), A. Motornenko

The CMF phase diagram



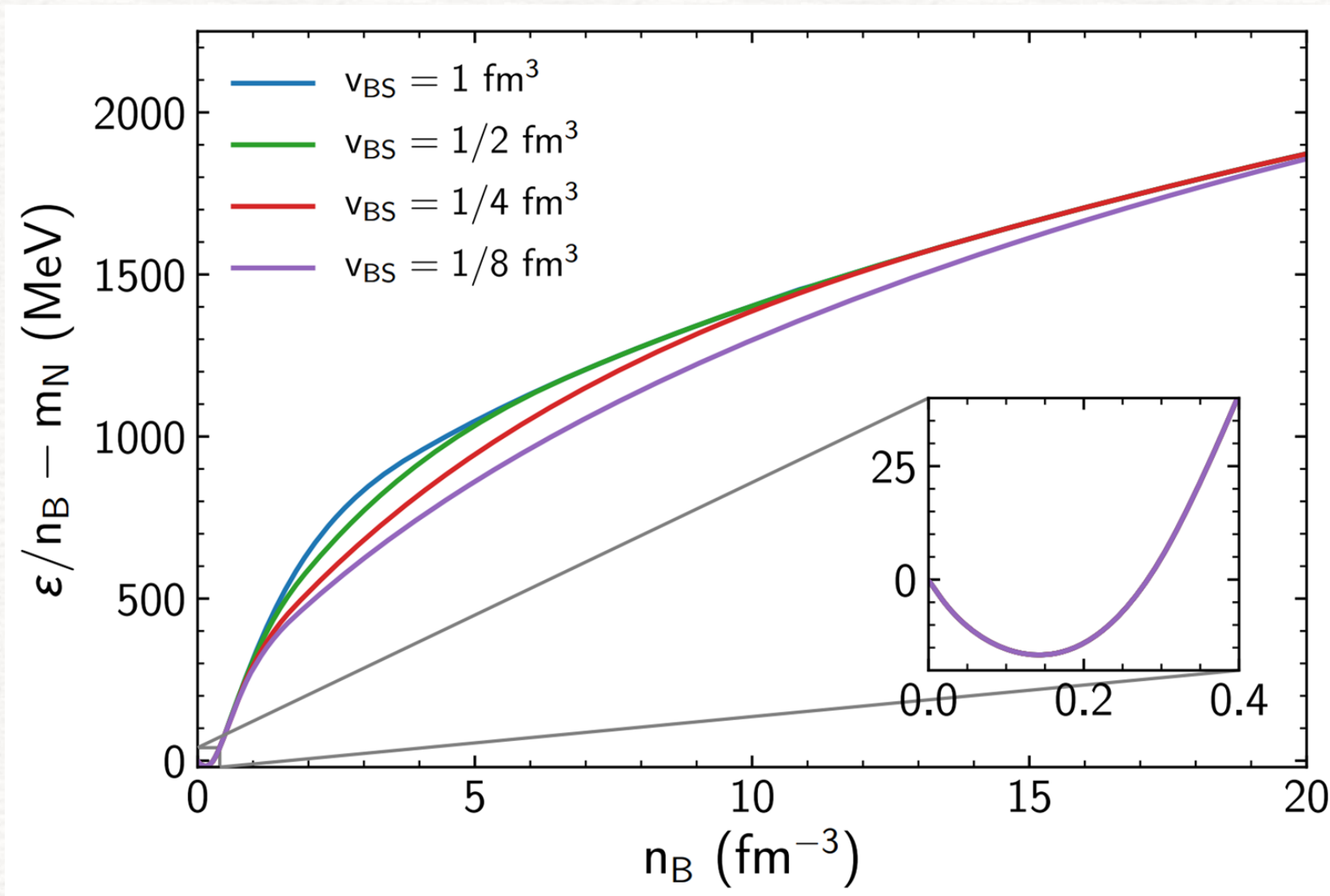
The phase transitions are only driven by **hadrons**.
Deconfinement is always smooth.

Parity doublet model with only hadron d.o.f



Properties of cold matter

$T=0$ isospin symmetric matter.



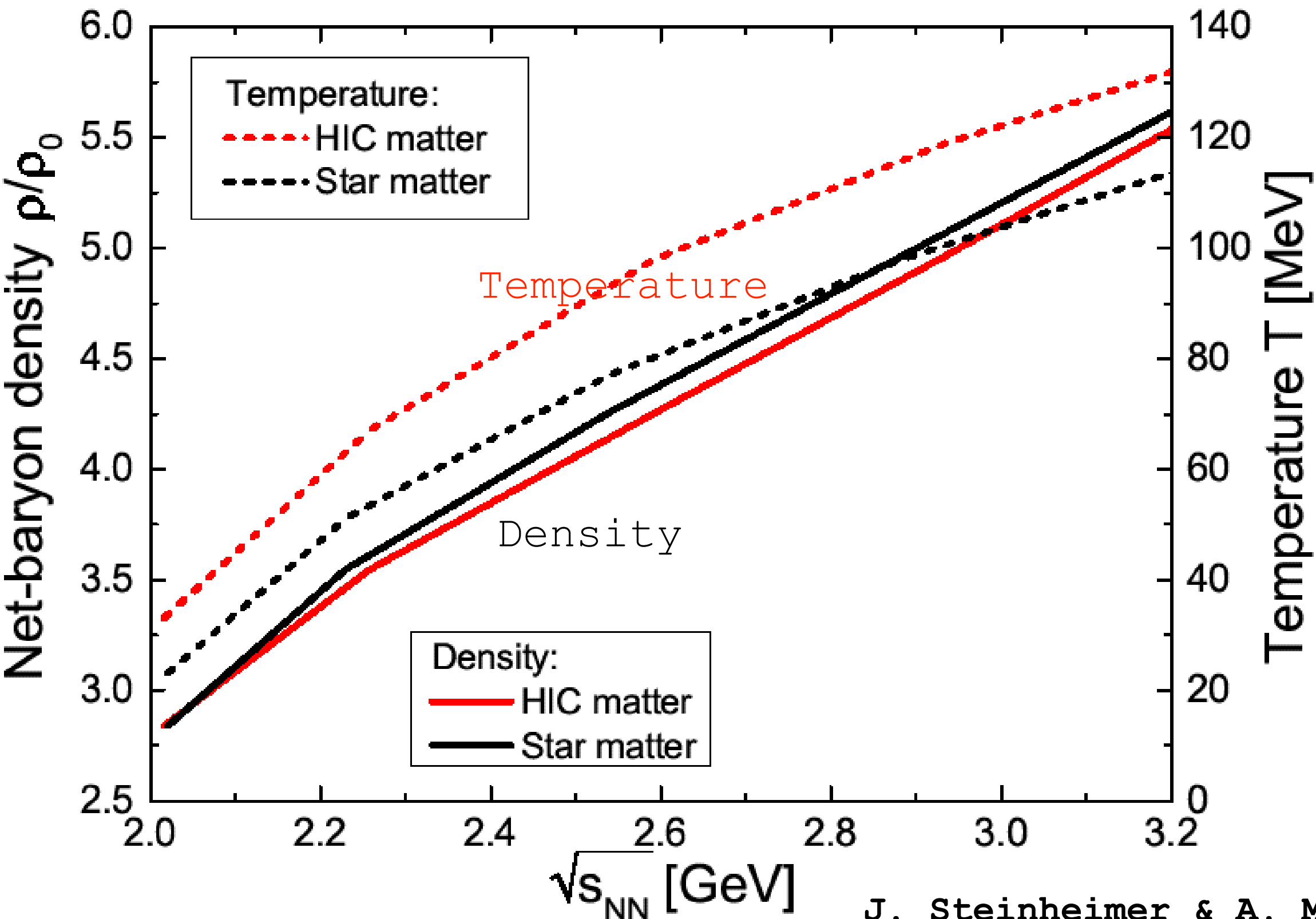
Nuclear ground state is not affected — good.

Then at higher densities hyperons start to populate CMF matter — the EOS softens. Then at extreme densities quarks kick in, hadrons are suppressed.

The appearance of hyperons do produce additional (meta) stable state. Probably additional attraction is needed.

Neutron Star merger vs. heavy ion collisions: Baryon Densities and Temperatures

+ initialize by Relativistic Rankine Hugoniot Taub Adiatat with Relativistic CMF- EoS



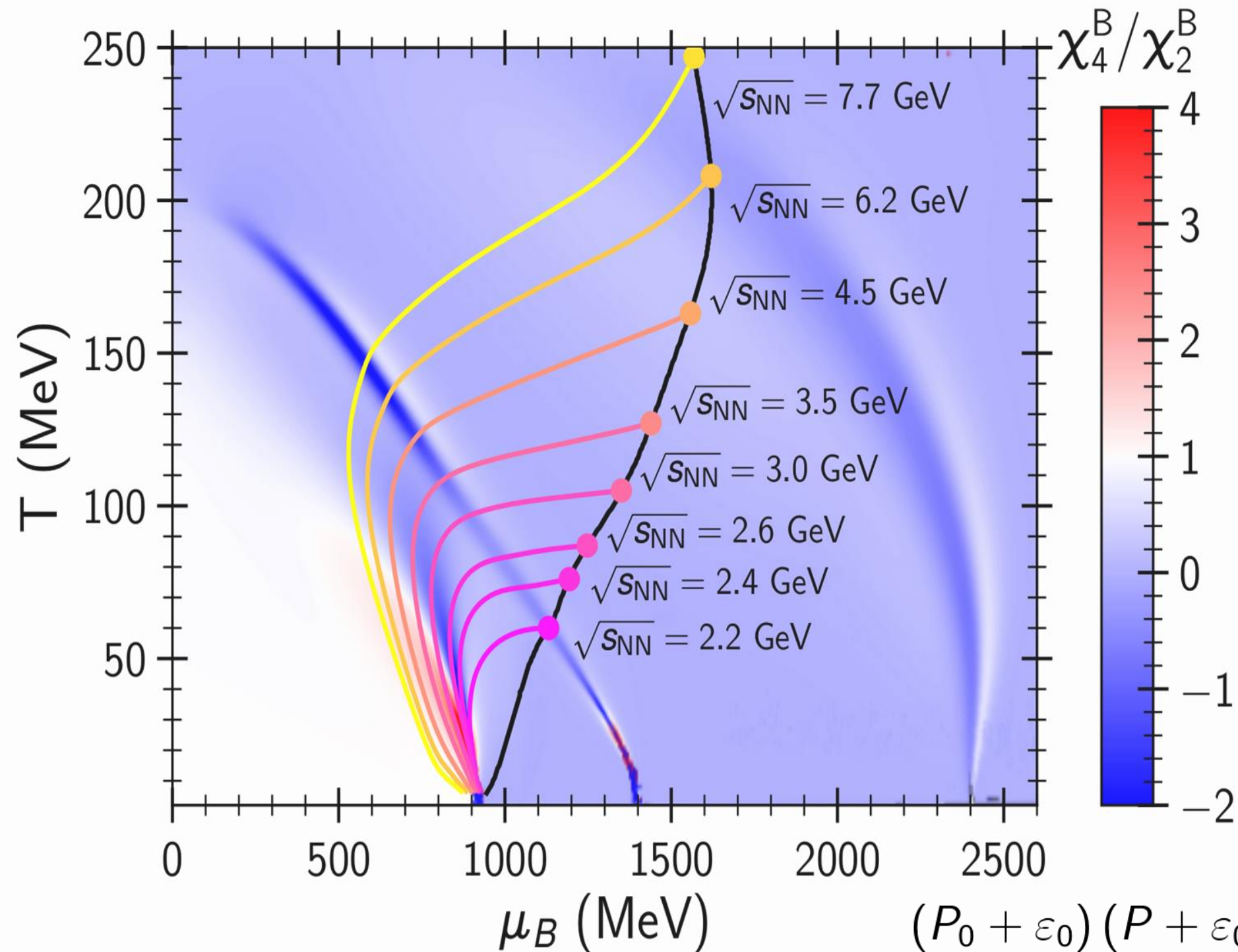
Compare central heavy ion collisions with head-on neutron star collisions:

Rankine Hugoniot Taub Adiabate

conserve baryon number and energy momentum current densities across shock front yields stationon.1+1D, hydrodynamical equation for n , p vs E :

$$E^2 - E_0^2 = (p - p_0)(E/n - E_0/n_0)$$

Probing the phase diagram by heavy ions



Hydrodynamical evolution of the **hot central region in heavy ion collision** can be calculated as isentropic expansion ($S/A = \text{const}$, no dissipations).

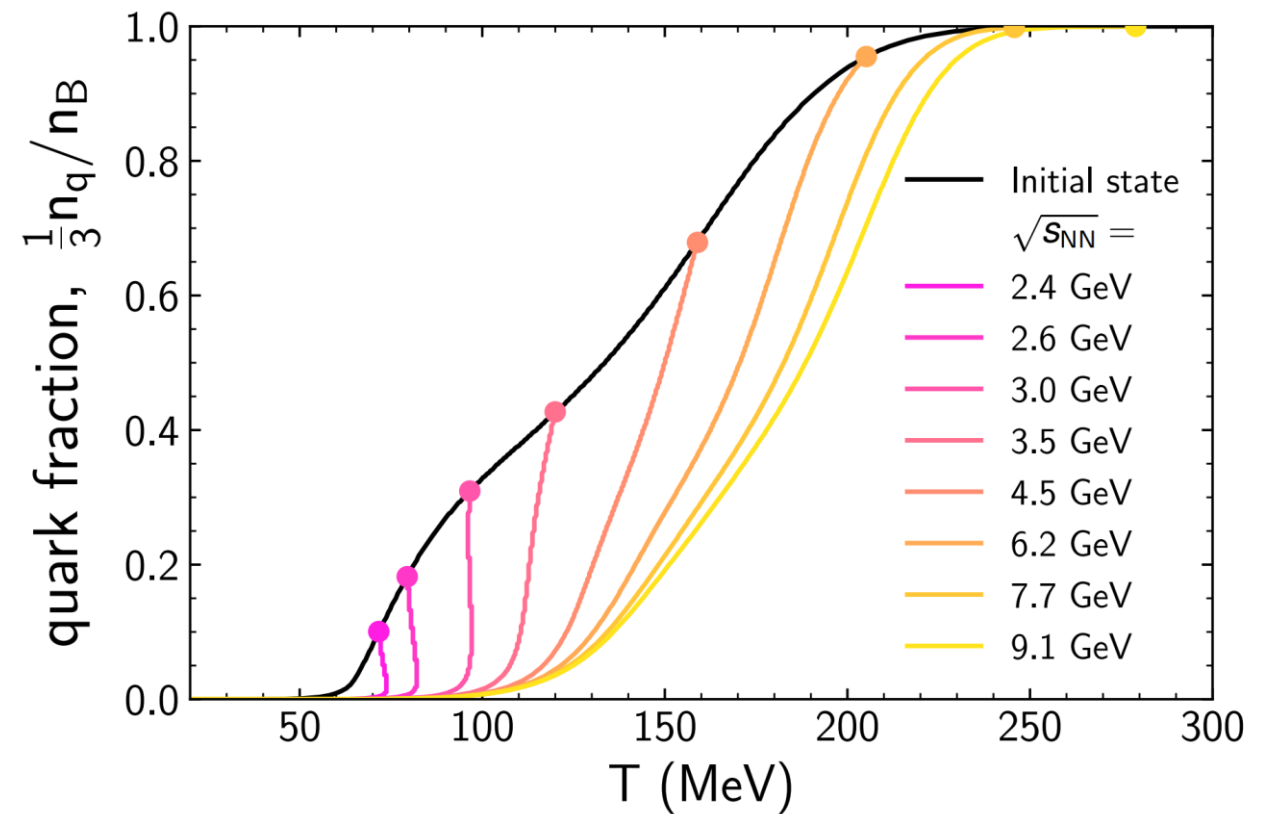
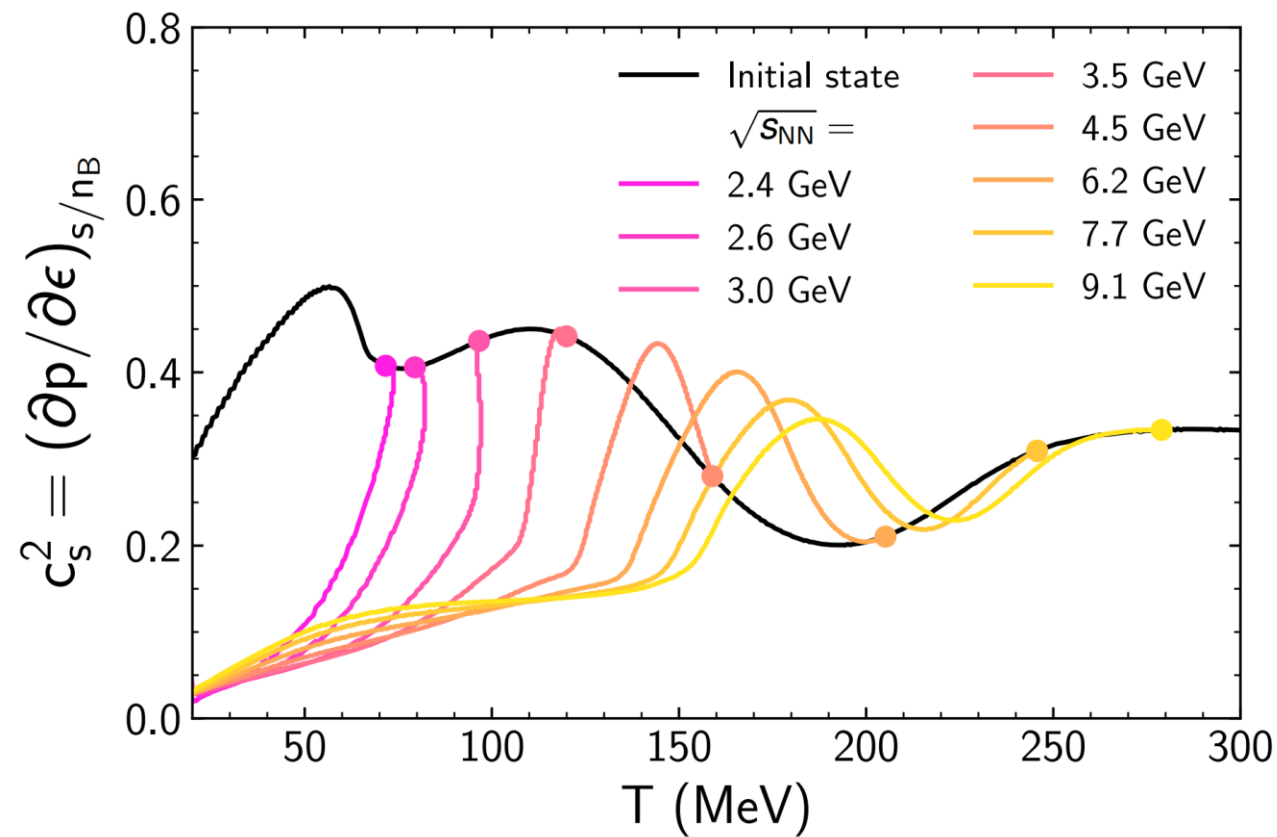
Initial entropy per baryon S/A is estimated by the relativistic Rankine-Hugoniot-Taub adiabatic (shock wave solution) *A. H. Taub, Phys. Rev. 74, 328 (1948)*

$$(P_0 + \varepsilon_0) (P + \varepsilon_0) n^2 = (P_0 + \varepsilon) (P + \varepsilon) n_0^2$$

with the initial condition

$$P_0 = 0, \quad \varepsilon_0/n_0 - m_N = -16 \text{ MeV} \quad \text{and} \quad n_0 = 0.16 \text{ fm}^{-3}$$

Probing phase diagram by heavy ions collisions



speed of sound c_s^2 (left) and **quark fraction (right)** along the **isentropes** as functions of temperature T .

Colored lines = different collision energies (initial S/A), black solid line correspond to the initial state speed of sound and quark fraction respectively.

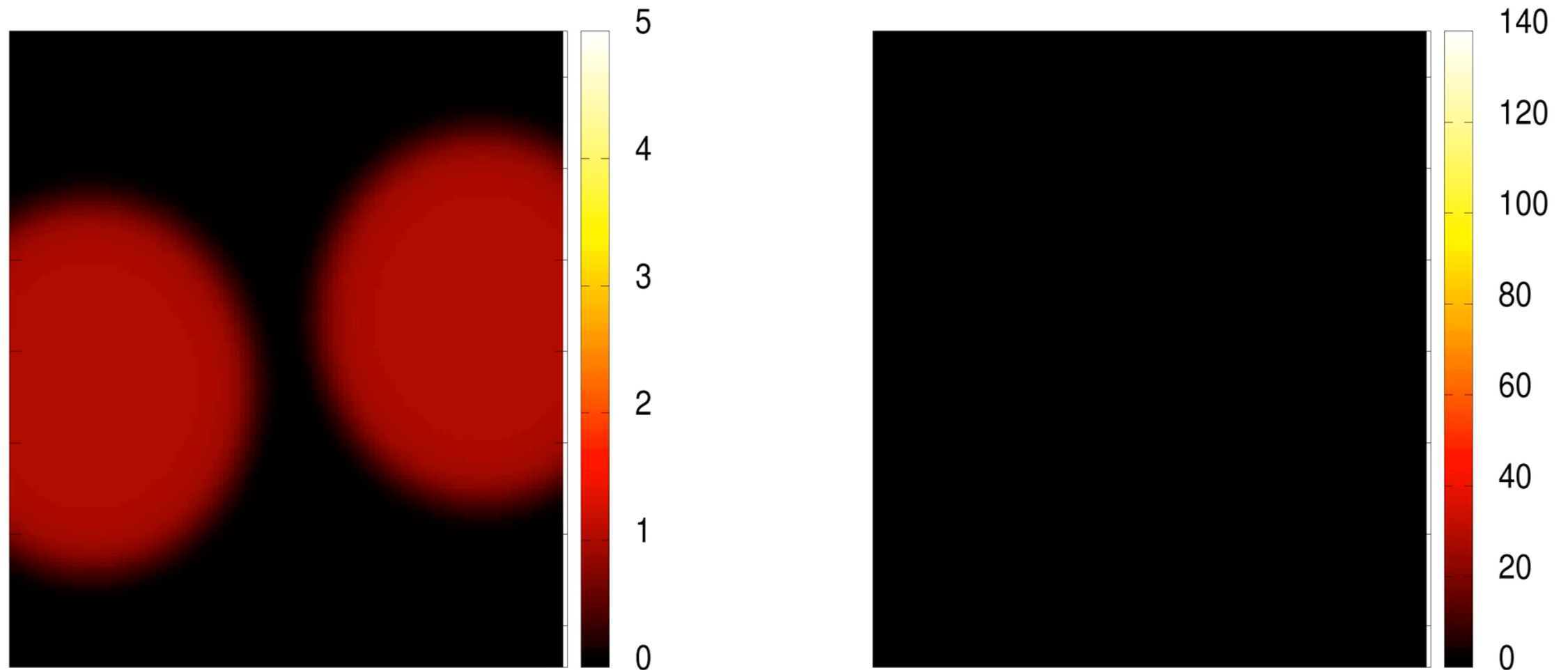
Scenario for higher energy $\sqrt{s_{NN}} > 7$ GeV:

1. start at the quark phase
2. softest point of deconfinement
3. baryons rapidly appear providing repulsion and increase of c_s^2
4. transition to dilute hadronic phase and lowering of c_s^2

Relativistic 4D Hydrodynamics for Heavy Ion Collisions@FAIR

Gold+Gold collisions at GSI: Helmholtz Zentrum für Schwerionenforschung.

At the FAIR facility: with high intensity beam



Density in units of nuclear ground state density

Temperature in MeV

time= 0.08 fm/c

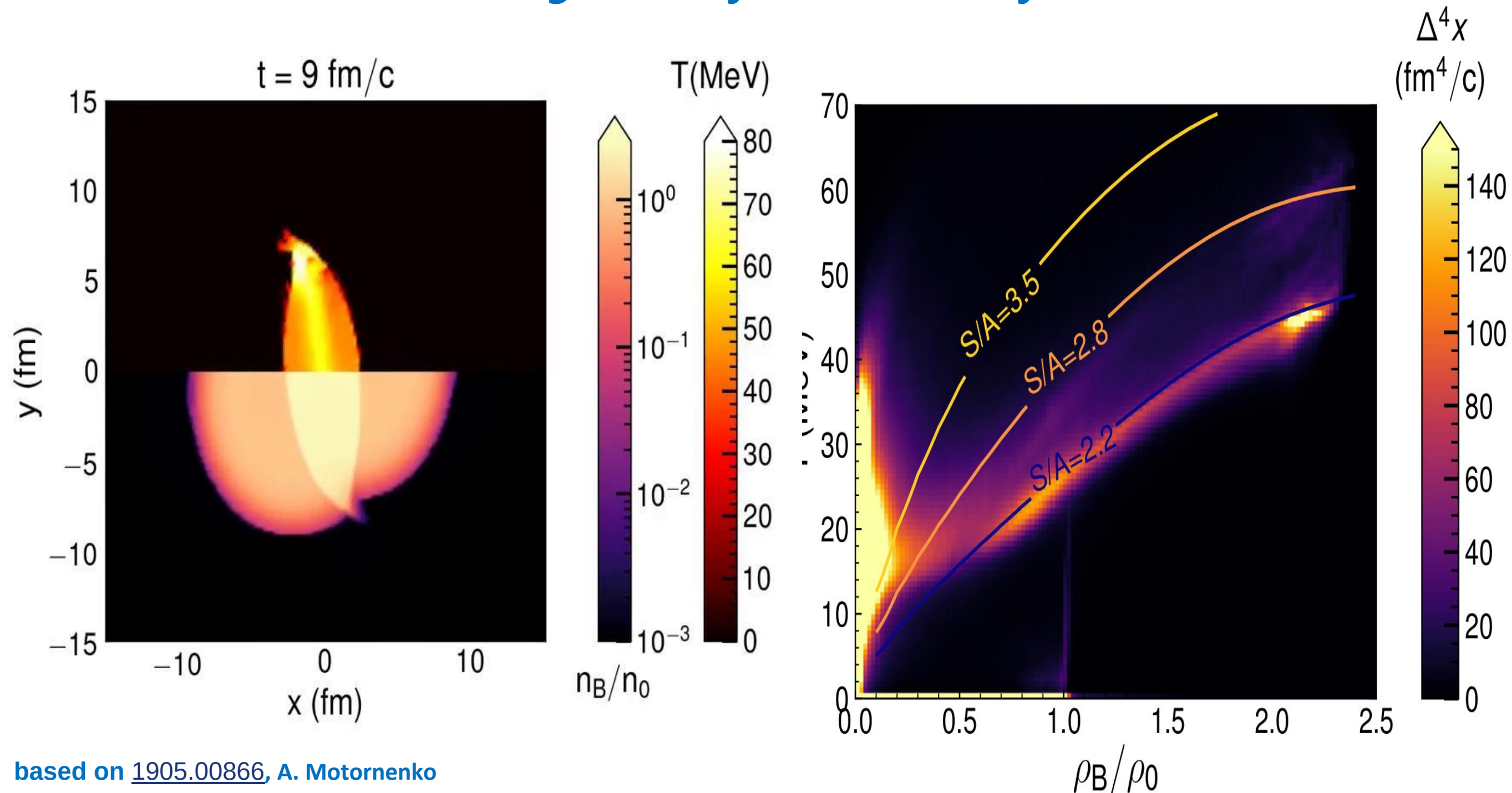
Jan Steinheimer , FIAS Frankfurt

Special Relativistic 3+1Dim Hydrodynamics for HIC '80-/'90-ies :

G.Graebner, D.Rischke, et al., ITP, Goethe University

Probing the QCD- phase diagram by heavy ions

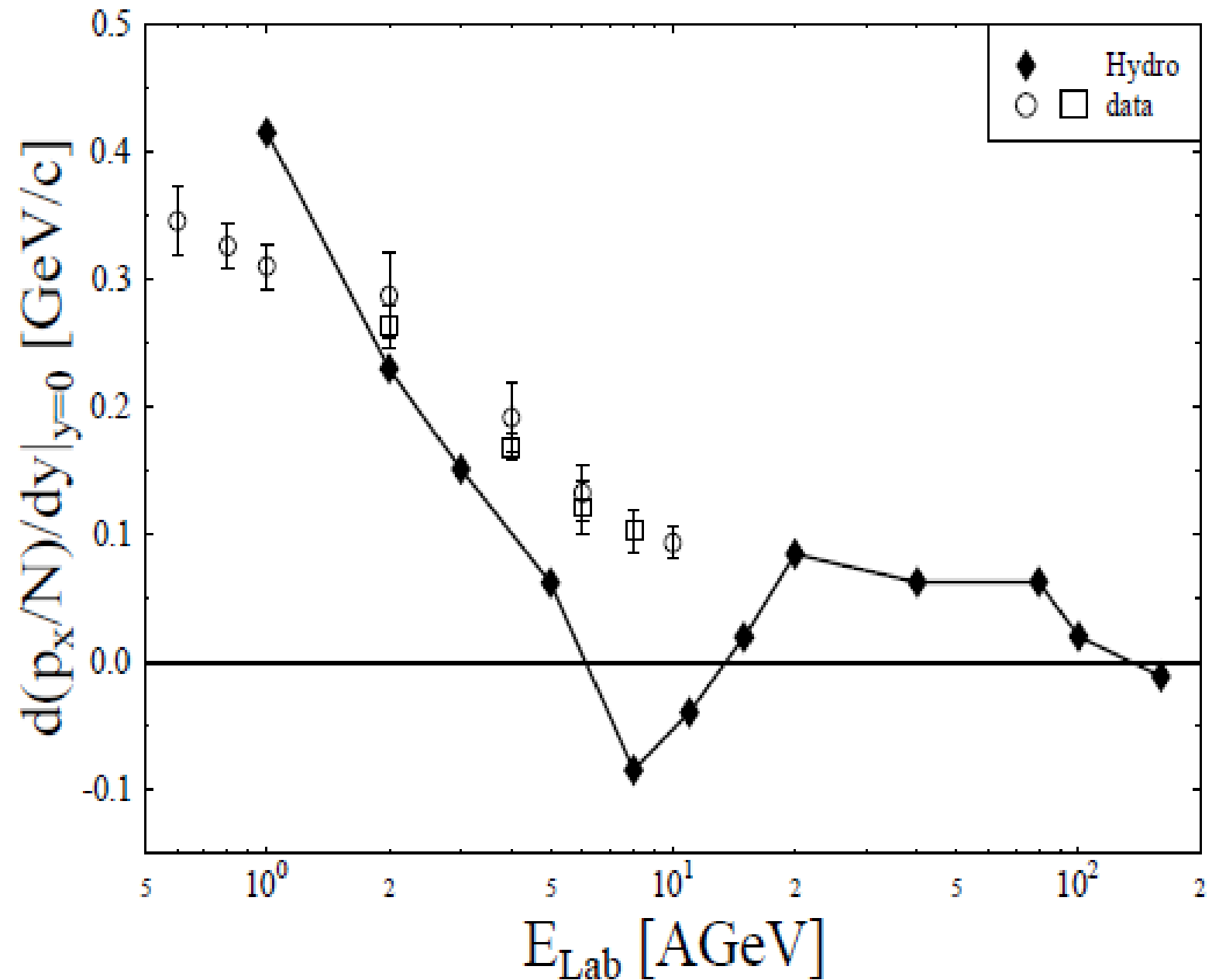
Full 3+1Dim relativistic hydrodynamic simulation of heavy ion collision at GSI - HADES energies, $E_{\text{lab}}=600$ AMeV
With CMF - a realistic high density EOS for Heavy Ion collisions



Some results

What is directed flow?

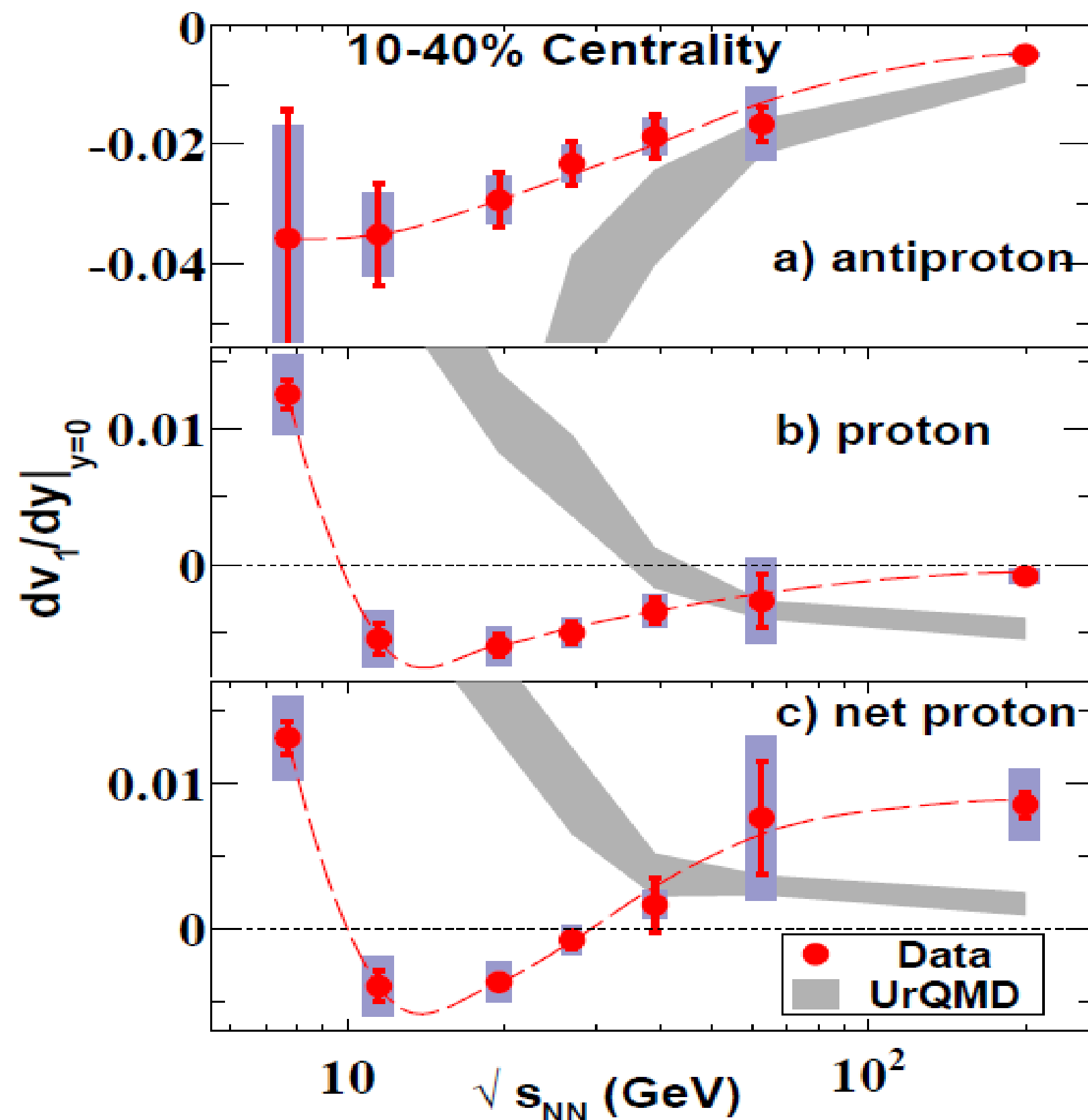
One is interested in the slope of $v_1 = \langle p_x/p_T \rangle (y)$ w.r.t the rapidity.



K. Paech, M. Reiter, A. Dumitru, H. Stoecker and W. Greiner, Nucl. Phys. A 681, 41 (2001)

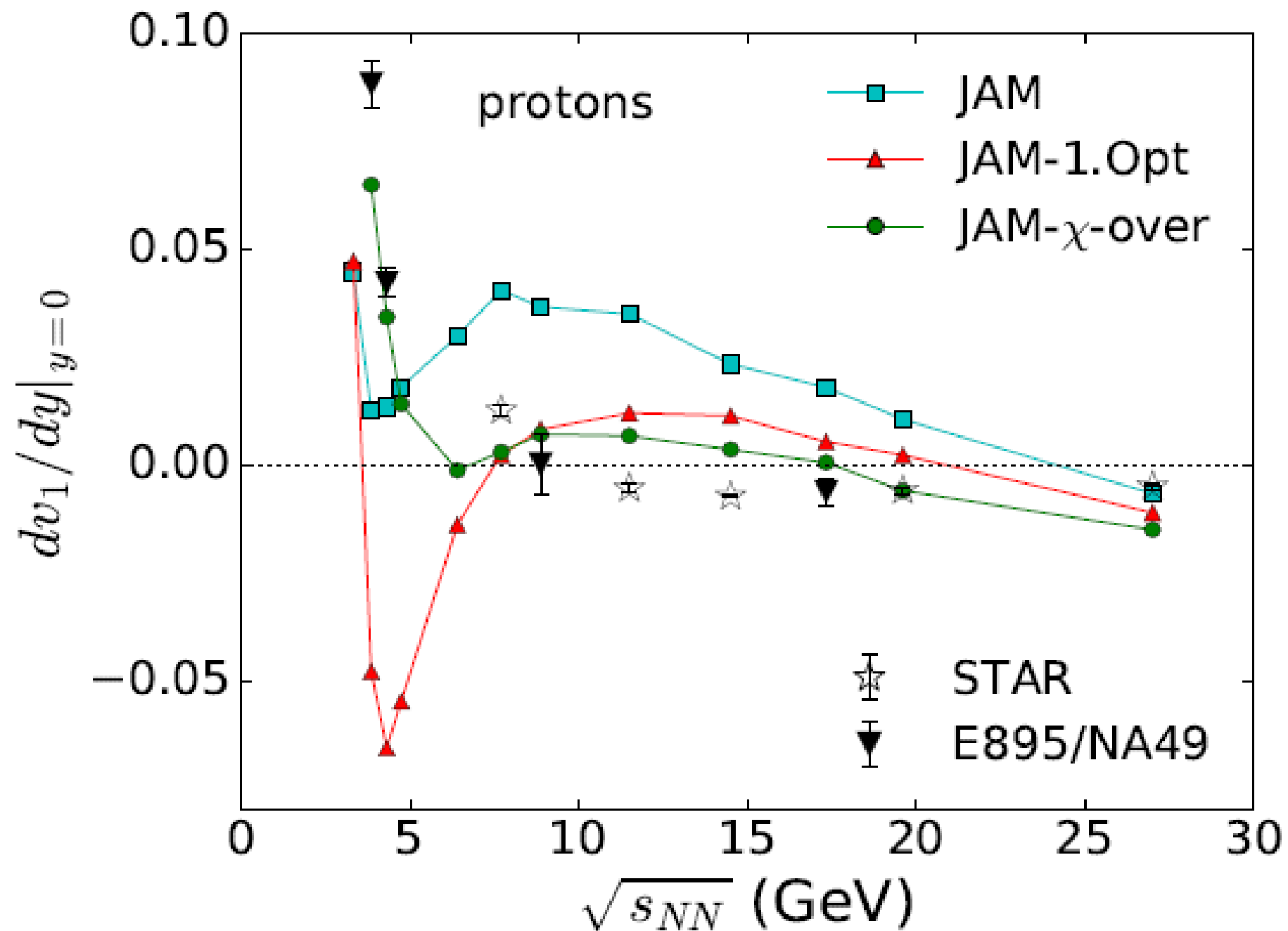
a strong effect from the softening of the EoS is observed

- Resent STAR measurements show a negative slope of net proton v_1 .



Microscopic Transport with EoS

If a fully microscopic transport simulation with EoS (JAM) is used the effect persists.



Y. Nara, H. Niemi, JS and H. Stöcker, Phys. Lett. B 769, 543-548 (2017)

Death-Star- Machines - FAIR HIAF NICA STAR NeutronStar matter in the Lab - Heavy Ion Collisions Charm and Beauty of International Collaboration



Observers



Austria Czech



China

Finland



France



Germany



India



Italy



Poland



Slovenia



Spain



Sweden



Romania



Rosatom



UK

ungary

11.11.2019

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**"THE MOST HORRIFYING MOTION
PICTURE I HAVE EVER SEEN."
- REX REED**

**A FILM BY
TOBE HOOPER**

THE FAIR CHAIN SAW MASSACRE

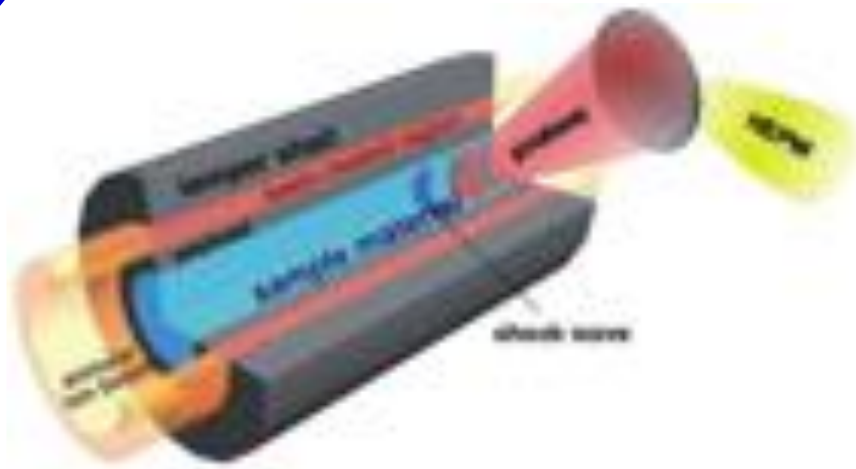




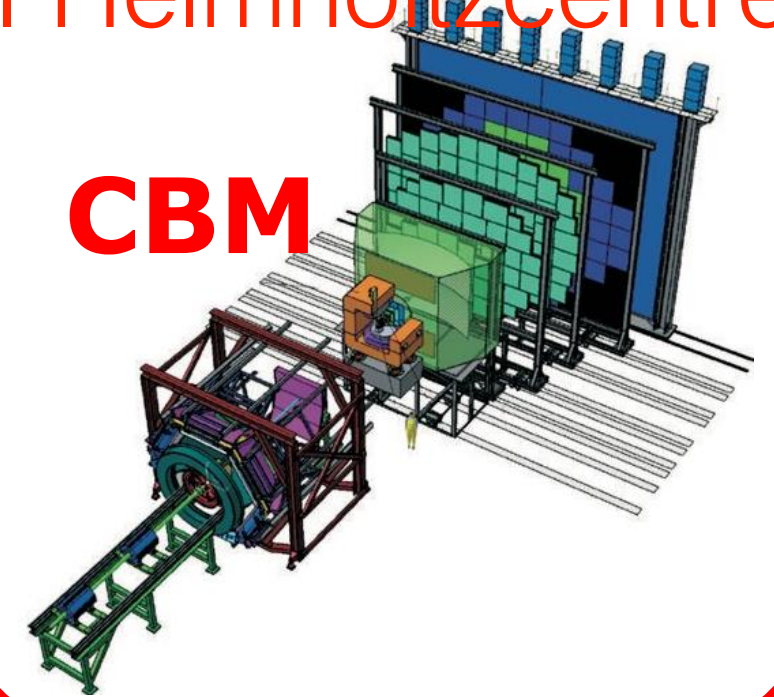


Neutron Star matter in CBM @FAiR-GSI Helmholtzcentre

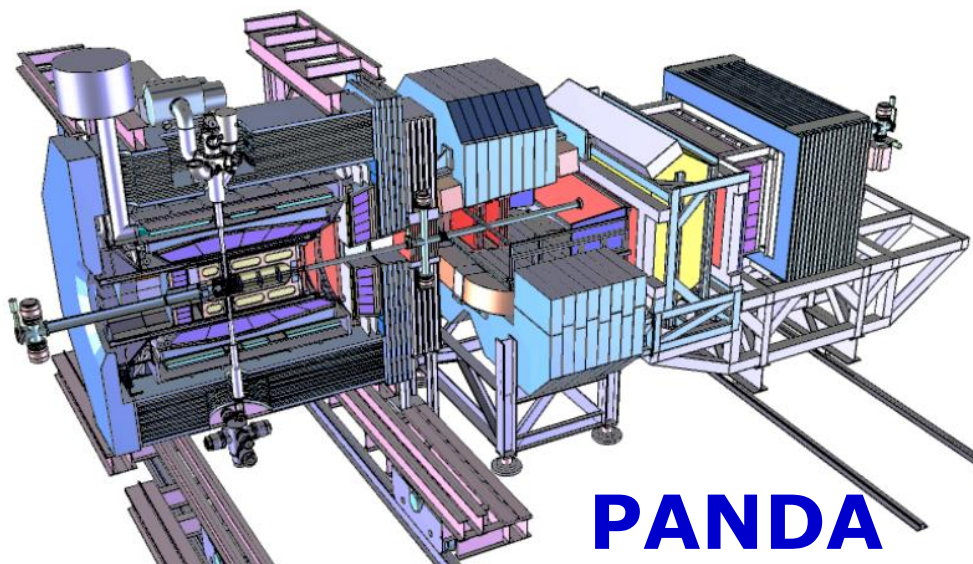
FAIR Experiments



APPA

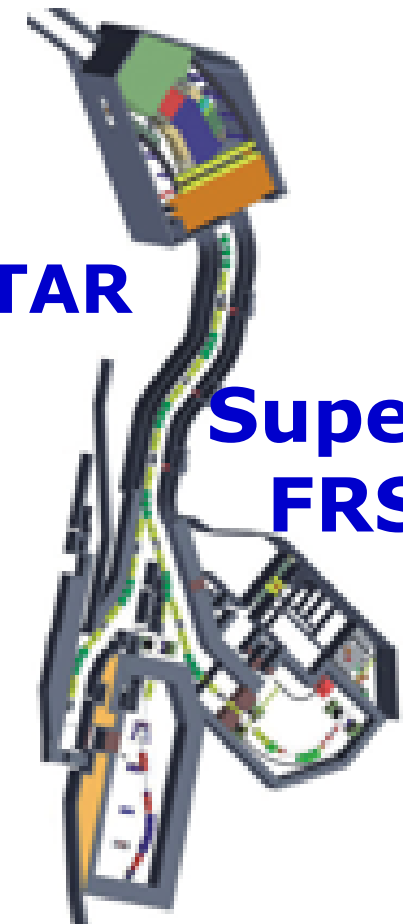


CBM



PANDA

NuSTAR



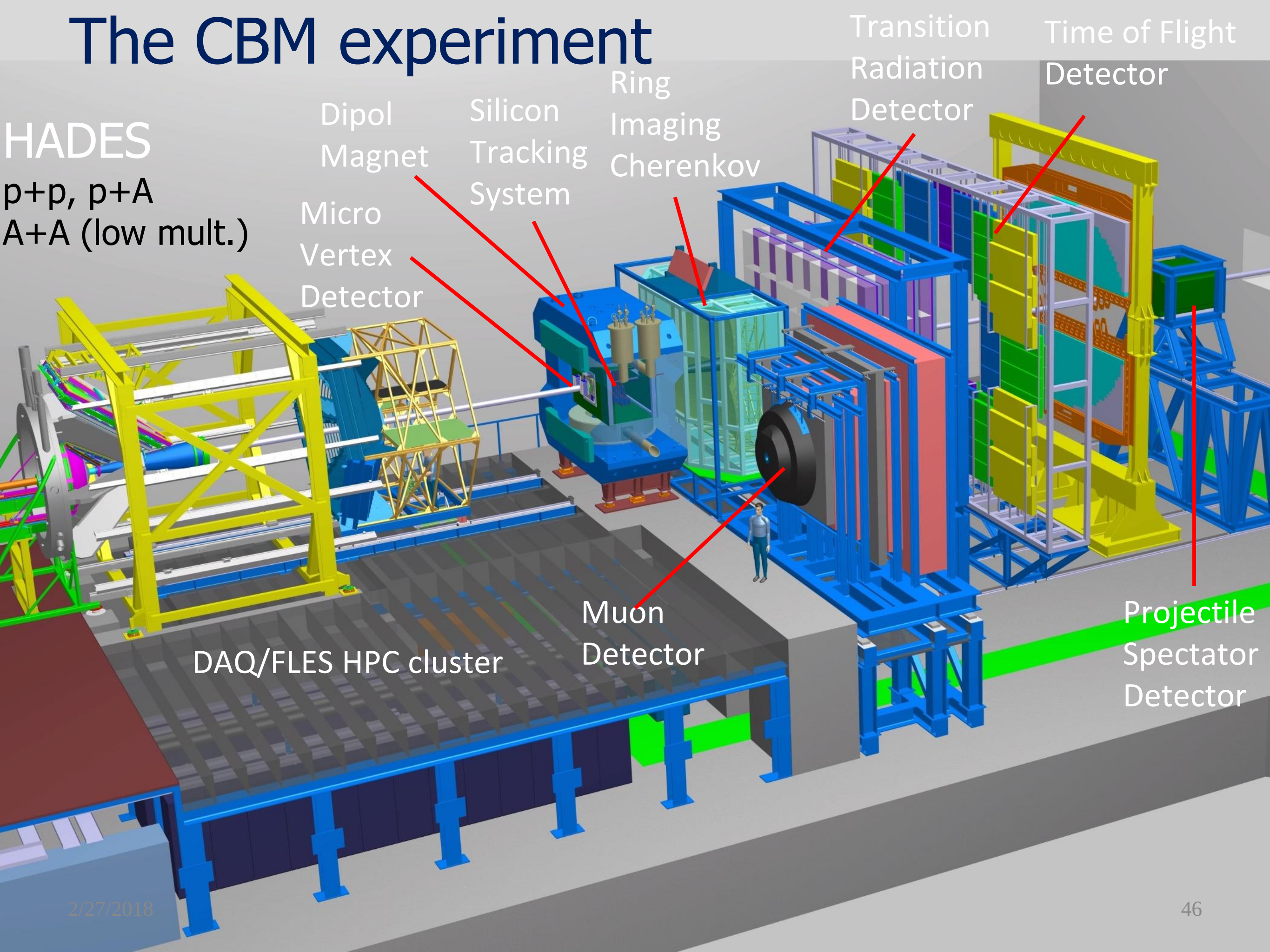
Super-FRS

The CBM experiment

HADES

p+p, p+A

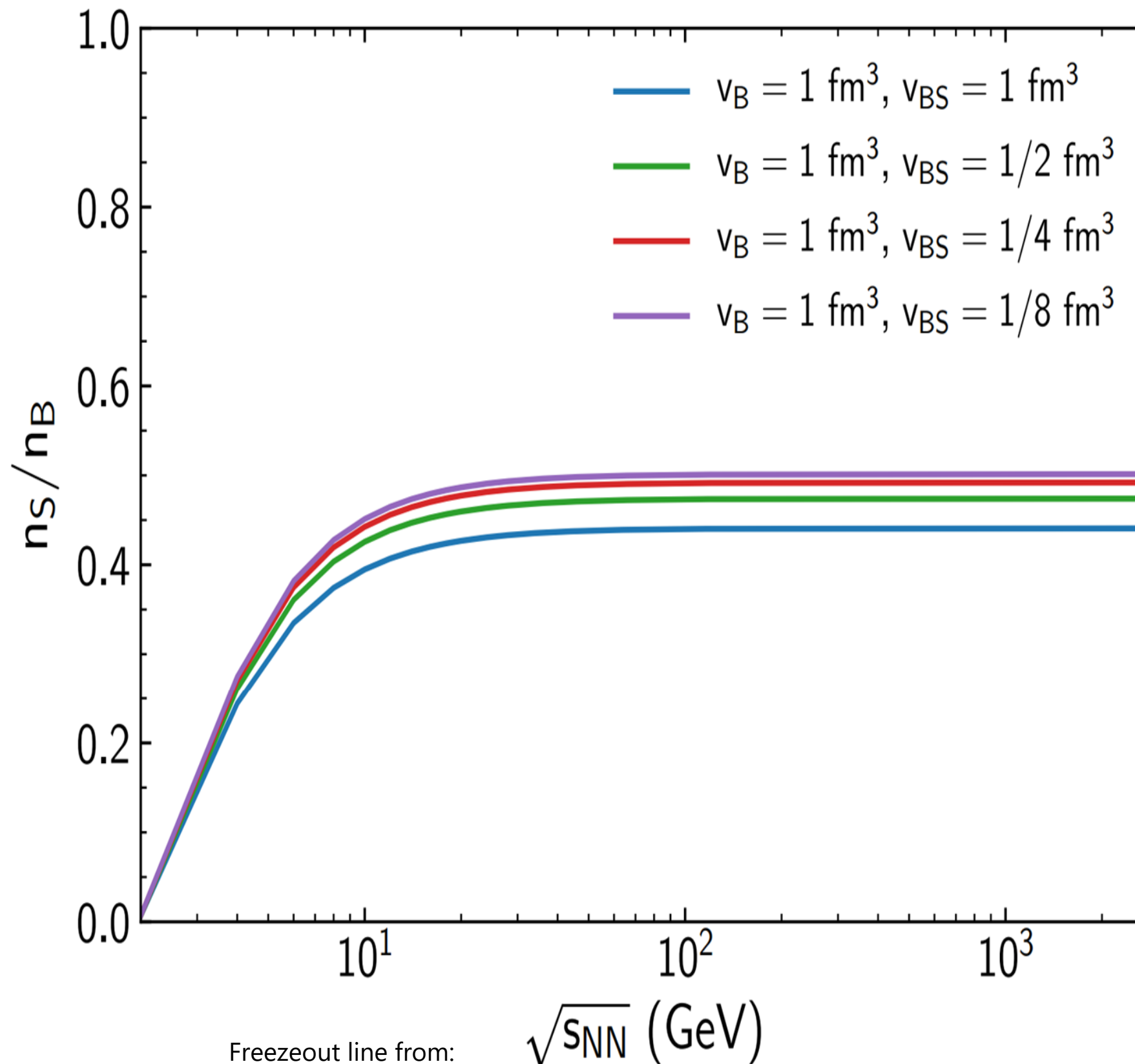
A+A (low mult.)



CBM Cave under construction



Strangeness at the freezeout



Freezeout line from:
V. Vovchenko, V. Begun, and M. Gorenstein,
Phys. Rev. C 93, 064906 (2016)

At the freezeout curve densities at temperatures are too small to feel EV effects.

Strangeness fraction at the freezeout is only changed slightly. Other effects to may suppress it even more: strangeness suppression factor, conservation laws

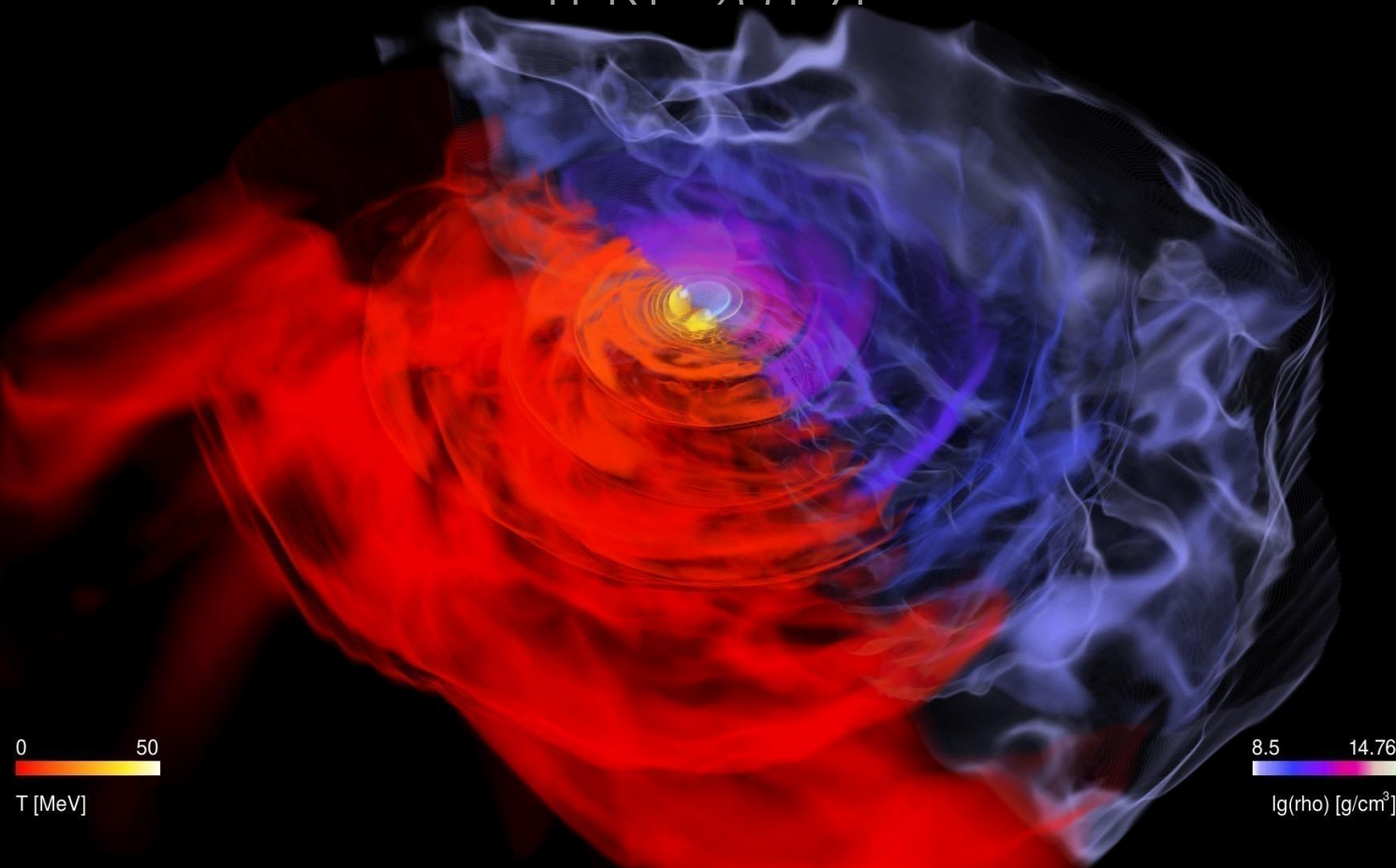
Hot Nuclear Matter EoS in Binary NS Mergers

- **Quark Matter Phase Transition**
- **Signatures in Gravitational Waves**

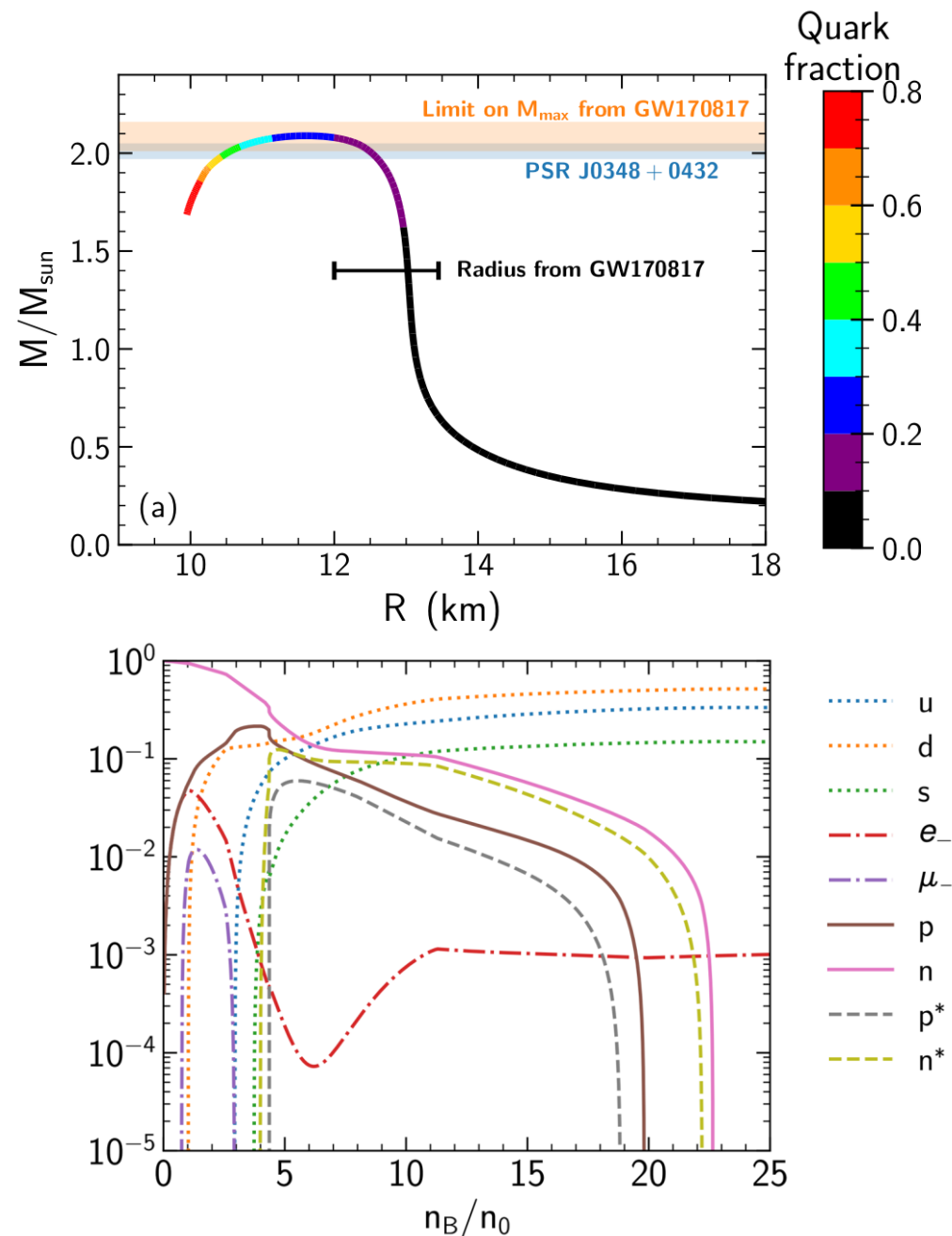
Most, Weih, Papenfort, Dexheimer, Hanauske,
Motornenko, Steinheimer, **Schramm**, Stoecker, Rezzolla

see also Bauswein, Bastian, Blaschke, Chatziioannou, Clark, Fischer, Oertel

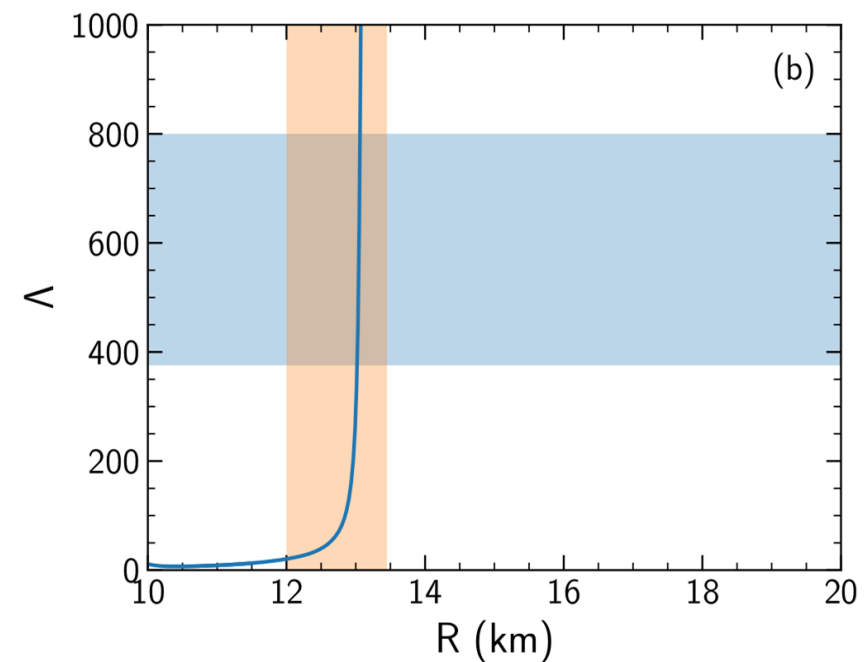
(PRI 2019)



Neutron stars: another benchmark for the QCD EoS

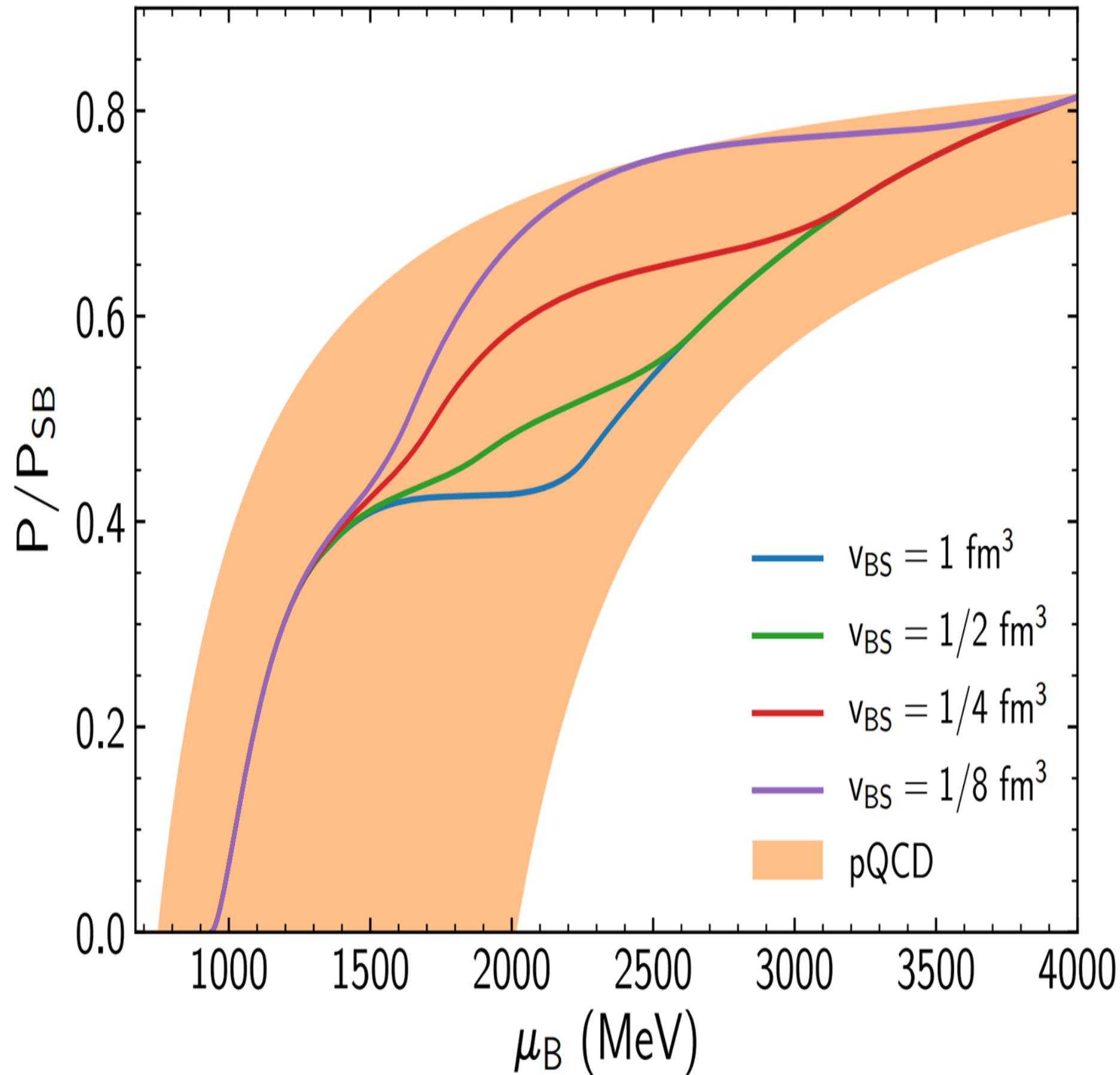


- The EoS is stiff enough to provide $2M_{\text{sun}}$ NS
- When quarks are dominant — NS are unstable
- No PT due to the deconfinement
- quark fraction $< 30\%$ for stable stars
- Agreement with the analysis of GW170817 (Most, Weih, Rezzolla, Schaffner-Bielich, 1803.00549)
- Maximal mass of NS is in agreement with constraints from universal relations (Rezzolla, Most, Weih, 1711.00314)



- Lattice QCD data suggests that hyperons are less repulsive than non-strange baryons.
- Non-strange baryon excluded volume: $v_B=1 \text{ fm}^3$,
- strange baryon: $v_{BS}=1/4 \text{ fm}^3$
- Better description of baryon and strangeness correlators is achieved
- Correlators which involve electric charge are still off the lattice data:
 - Meson EV parameter may be tuned as well
 - However, already by tuning only hyperon EV we prove that we may tune CMF model to any kind of lattice data
- Comparison with PQCD results at $T=0$ favor $v_{BS} \geq 1/4 \text{ fm}^3$
- New parameterizations do not produce exotic types of matter

Comparison with pQCD data for cold quark matter



CMF gives reasonable description for $v_{BS} = 1/4 \text{ fm}^3$.

For smaller values — too many degrees of freedom appear, overshooting of PQCD results.

Then at high μ_B hadrons are suppressed and SB limit is slowly approached.

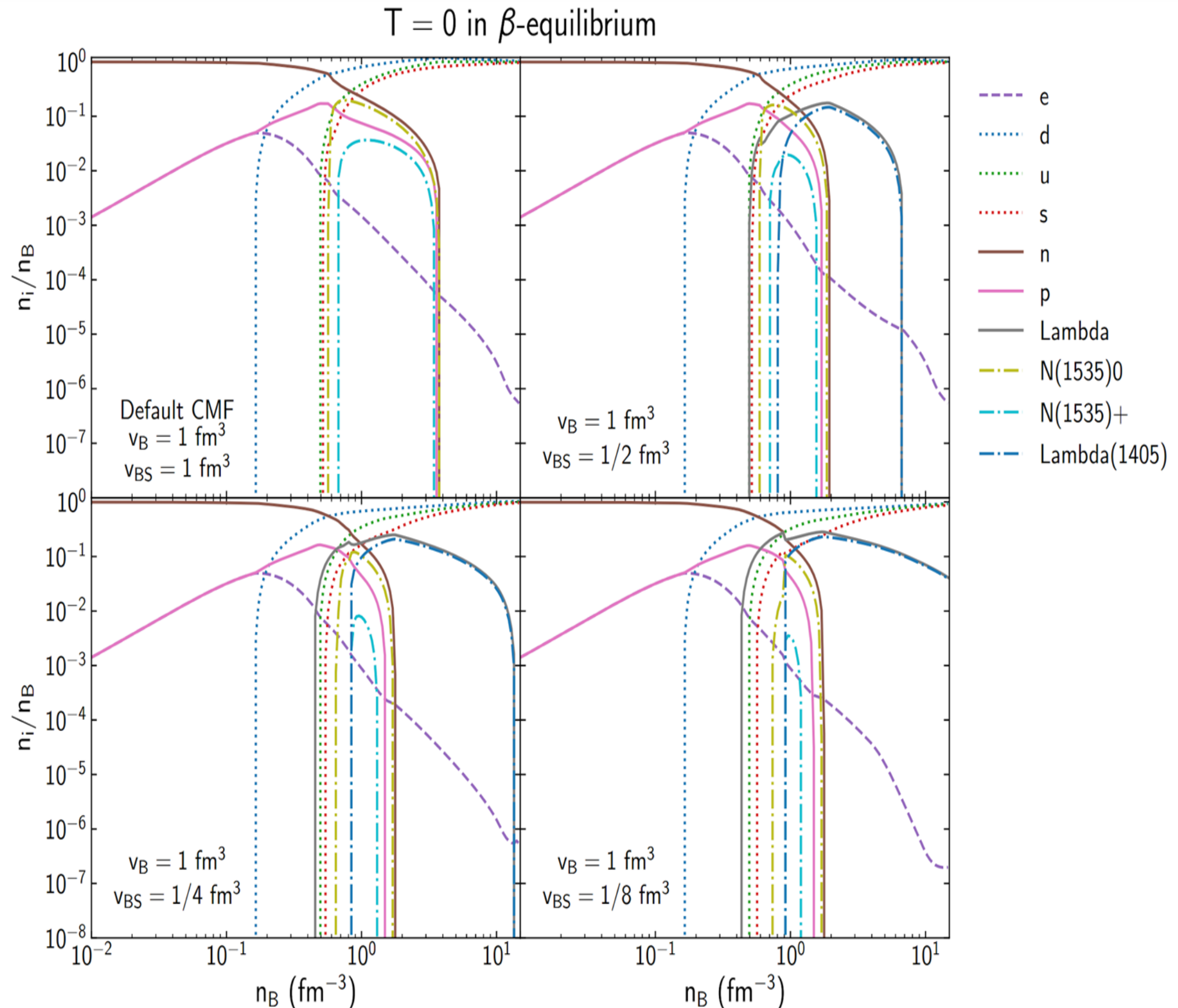
Properties of the cold matter: β -equilibrium

In the default CMF hyperons didn't appear at all for neutron stars.

Now they do !

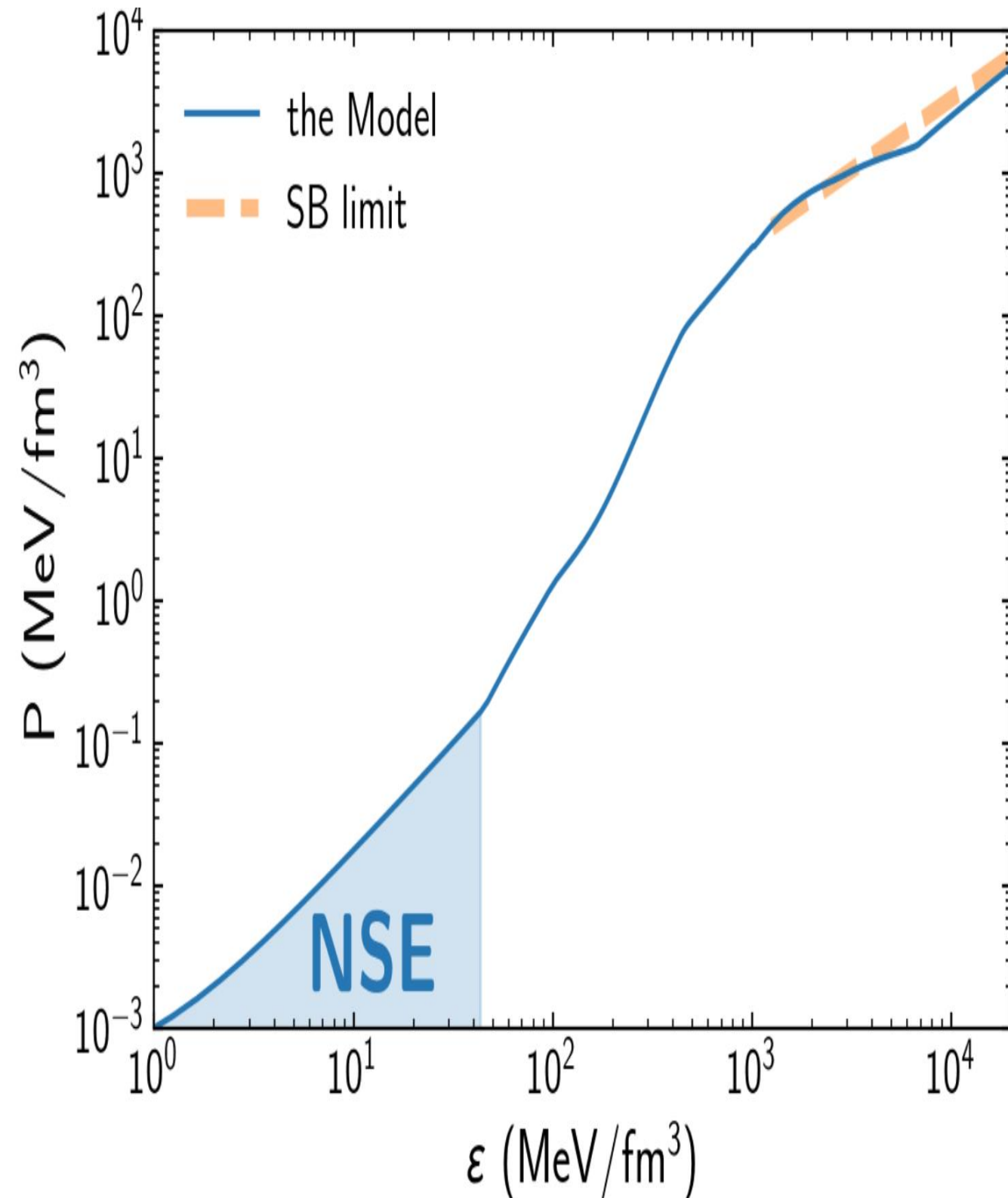
For small enough EV values hyperons survive up to very high densities.

For $v_{BS}=1/4 \text{ fm}^3$ (value from the LQCD analysis) hyperons are suppressed at $n_B=0.7 \text{ fm}^{-3}$



Application to neutron stars

- The model approaches **Stefan-Boltzmann**
- limit at high energy densities.



The model can be easily employed for the description of **neutron star matter** at **T=0 in beta-equilibrium** without any changes to the parameters. The EoS then can be used as an **input to model neutron stars** by solving Tolman–Oppenheimer–Volkoff equation:

$$\frac{dP}{dr} = -\frac{Gm}{r^2} \rho \left(1 + \frac{P}{\rho c^2} \right) \left(1 + \frac{4\pi r^3 P}{mc^2} \right) \left(1 - \frac{2Gm}{rc^2} \right)^{-1}$$

Additional input is needed to model star's crust — Nuclear Statistical Equilibrium (*Baym, Pethick, Sutherland, 1971, Astrophys. J. , 170, 299.*)



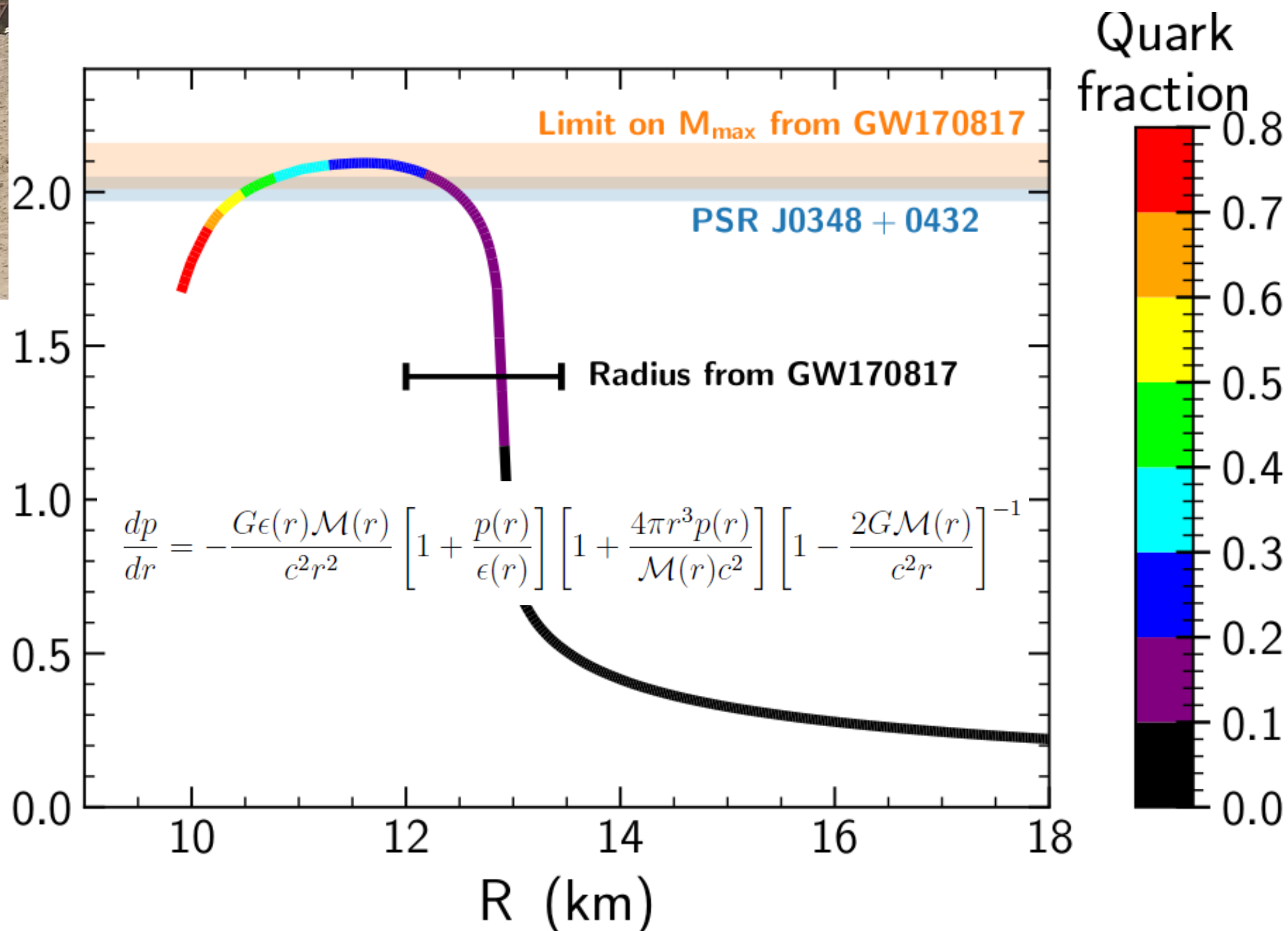
Neutron Star Masses-Radius

Anton Motornenko

Features:

Maximum NS-mass observed = $2.0 \times M_{\text{solar}}$ & **< $2.1 \times M_{\text{solar}}$** - limit of GW170817
Radii $\sim 12\text{-}13\text{km}$ observed

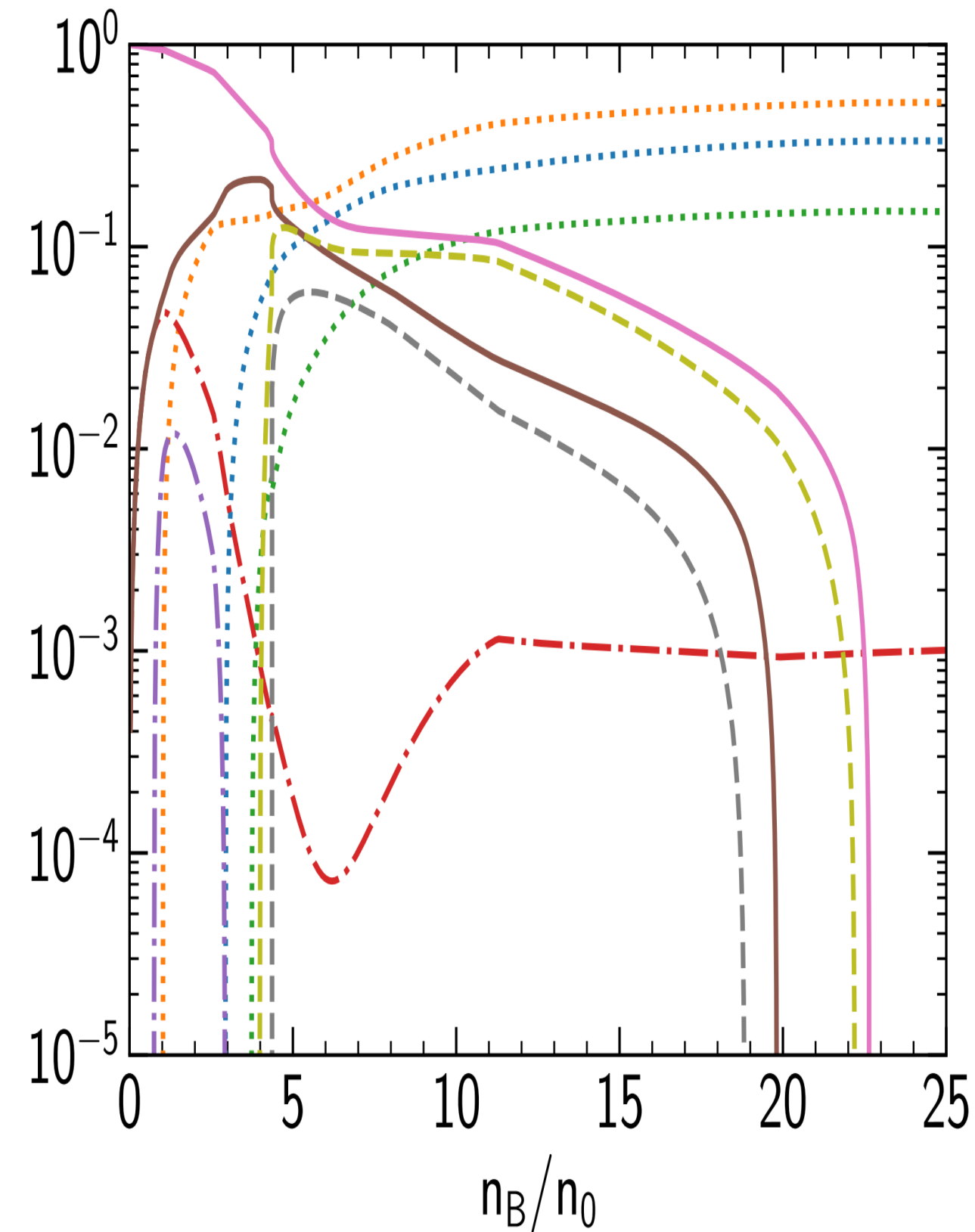
hybrid star's rel.EoS at high μ_B must **agree with lattice QCD data** at low μ_B



Anton **Motornenko**, Vovchenko, Steinheimer, **Stefan Schramm**, Stoecker
1809.02000, NPA (2019), QM'19 Wuhan

H. Stöcker, February 2020

Equation of state at $T=0$: neutron stars



Equation of state for

neutron stars:

• **$T=0$**

• Electric charge is **zero**

• **Leptons** are included

• No nuclear ground state

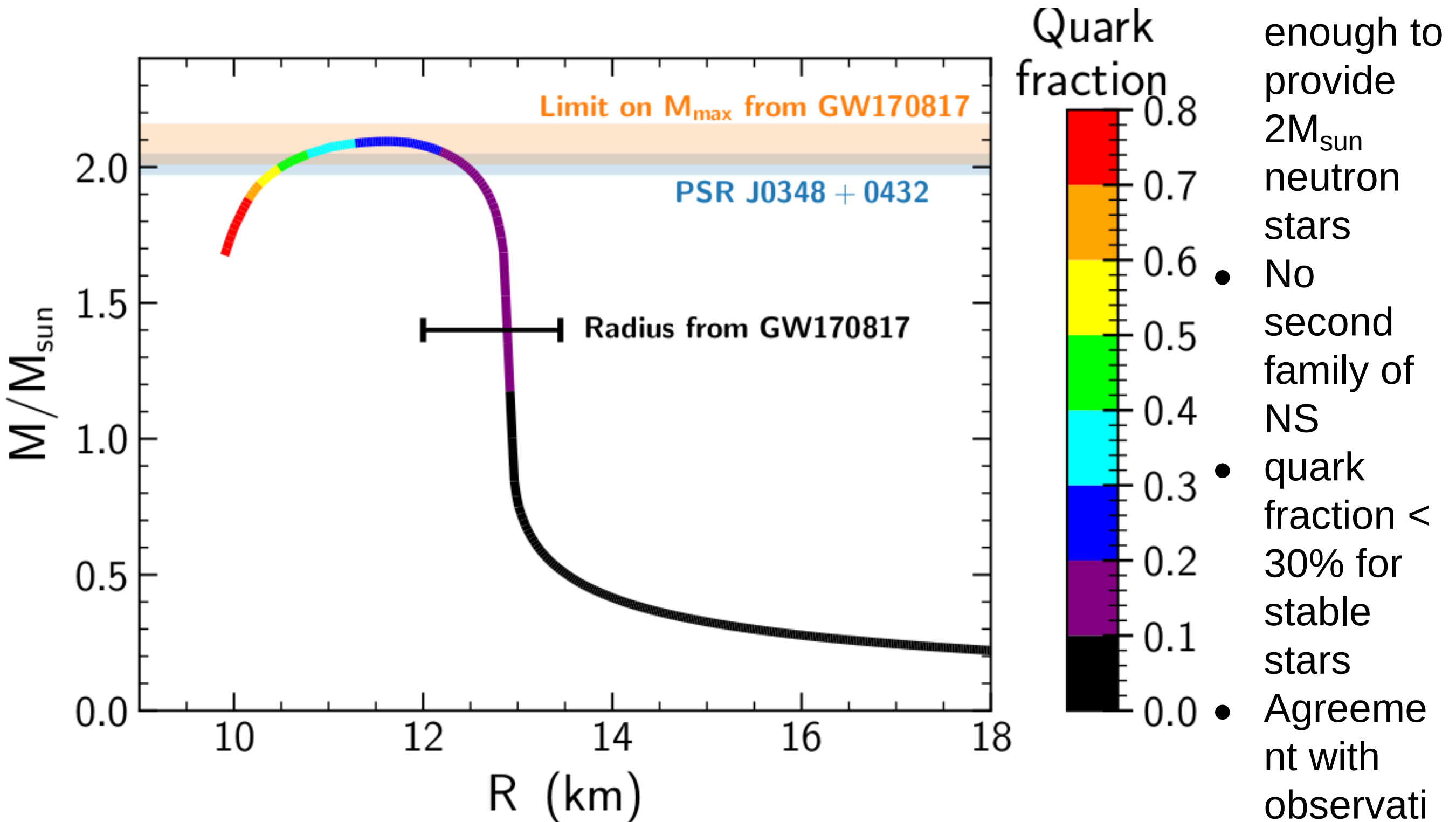
• Chiral transition is at $n \approx 4n_0$

• Quark matter is at $n \approx 23n_0$

• **Hyperons** at $T=0$ are suppressed by hard-core repulsion (nevertheless are present at $T \neq 0$)

• **Strange quarks** are included

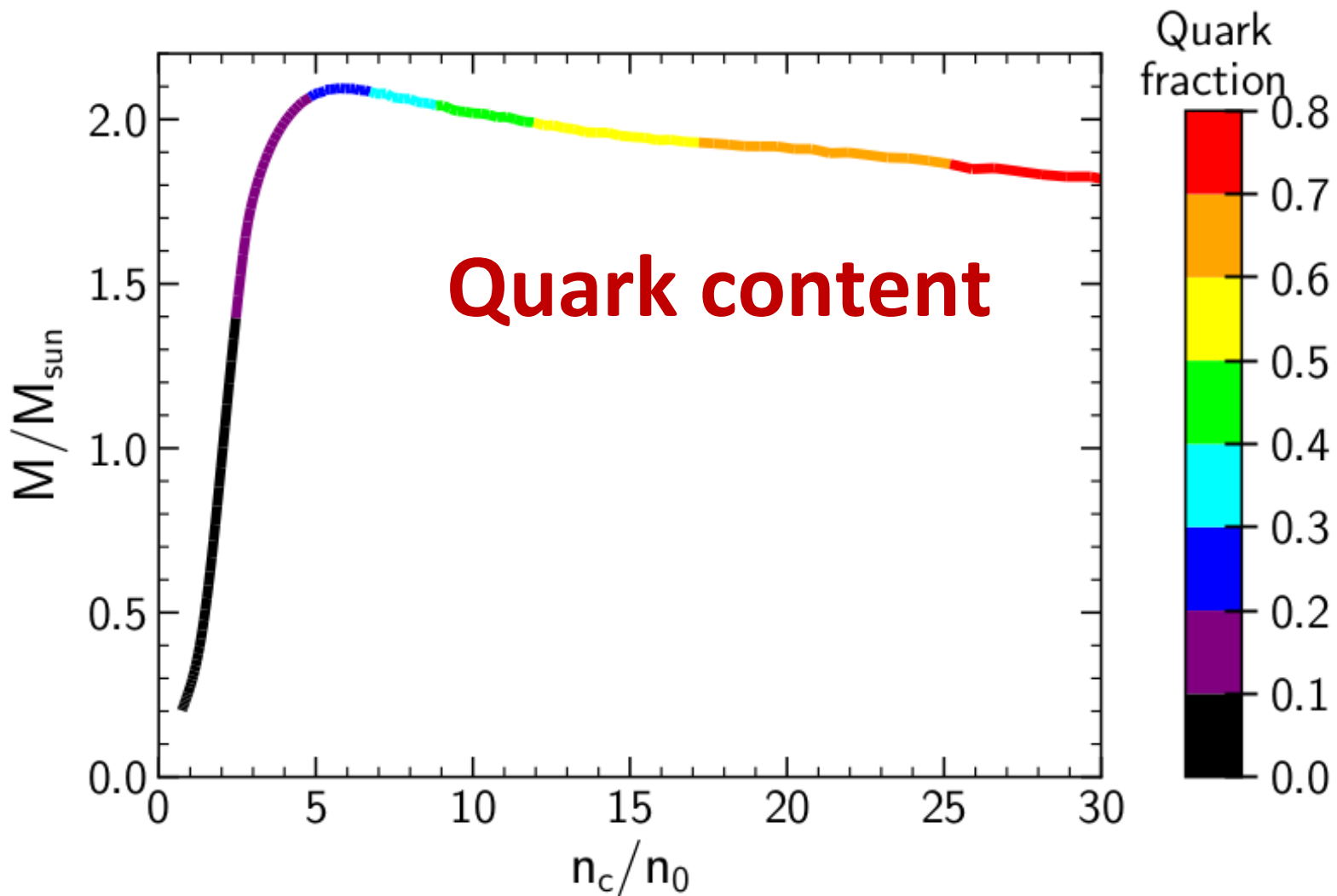
Mass-radius relations



Maximal mass is in agreement with recent constraints on maximal mass of neutron star from GW170817:

$$2.01^{+0.04}_{-0.04} \leq M_{\text{TOV}}/M_{\odot} \lesssim 2.16^{+0.17}_{-0.15}$$

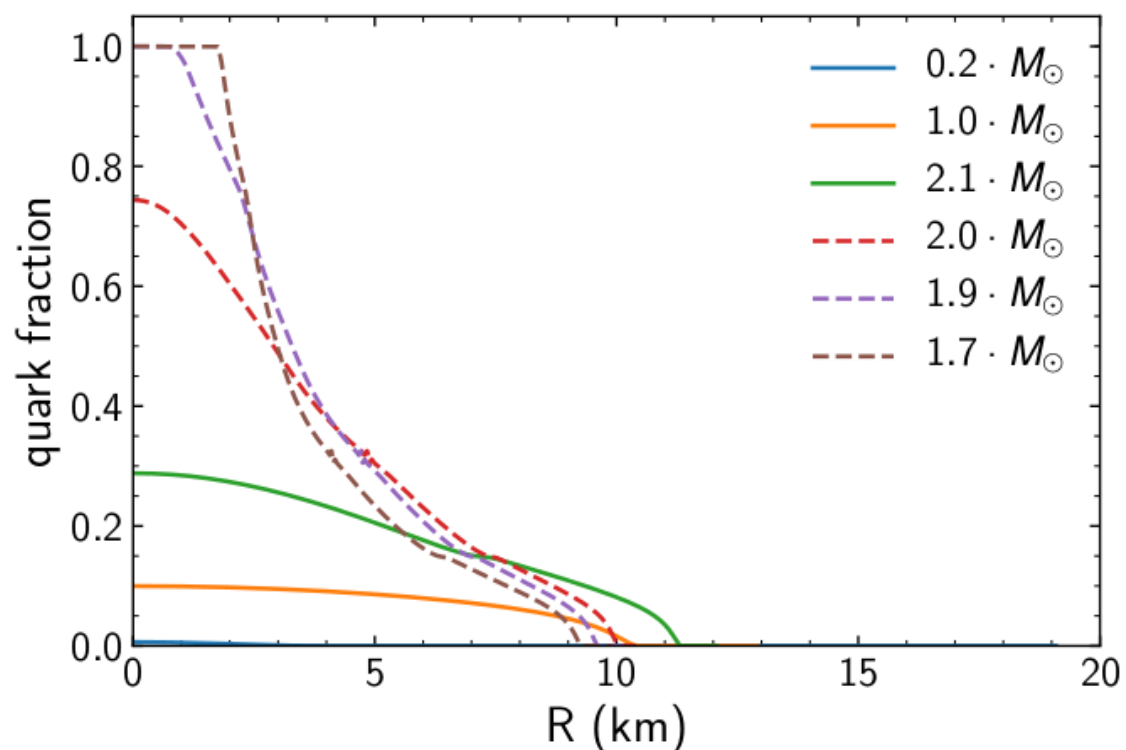
- EoS is stiff enough to provide $2M_{\text{sun}}$ neutron stars
- No second family of NS
- quark fraction $< 30\%$ for stable stars
- Agreement with observations



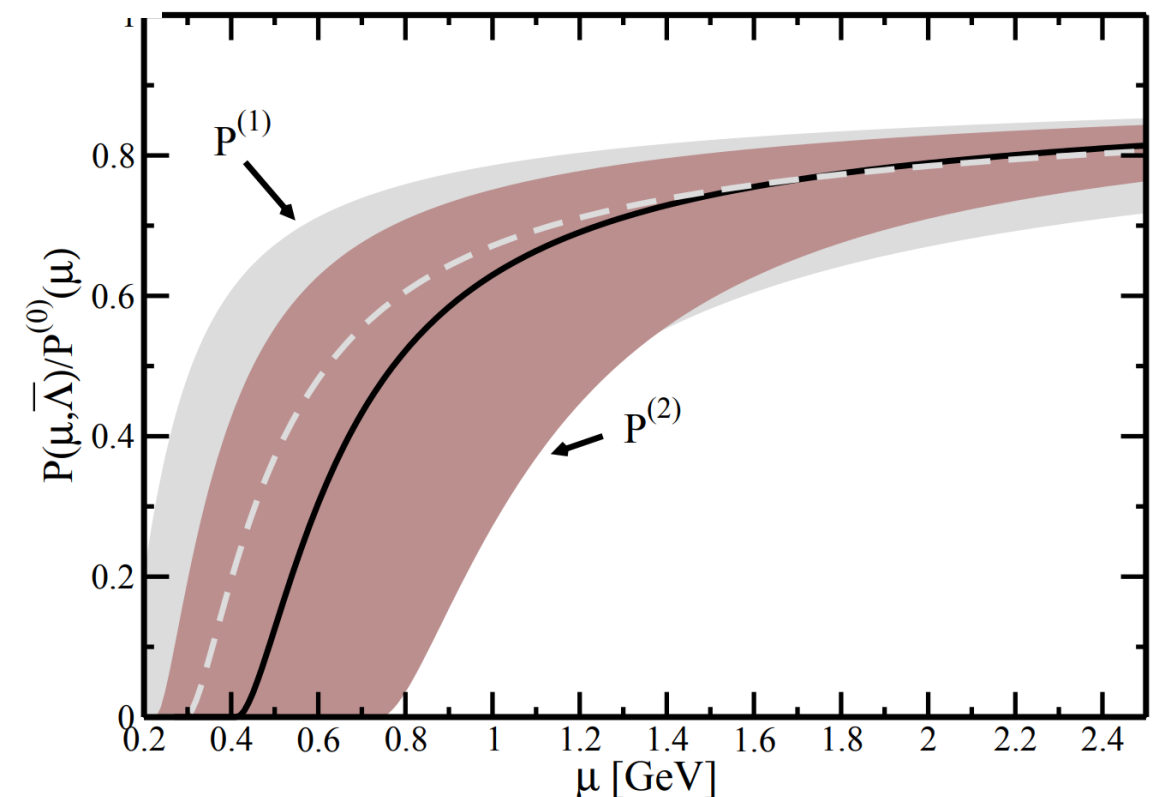
Quarks appear smoothly
— no separation between phases.

Strange quark fraction is <13%, produced by weak decays.

Quarks give significant contribution to stars with central density $n_c > 6n_0$, where pQCD calculations for EoS are available:

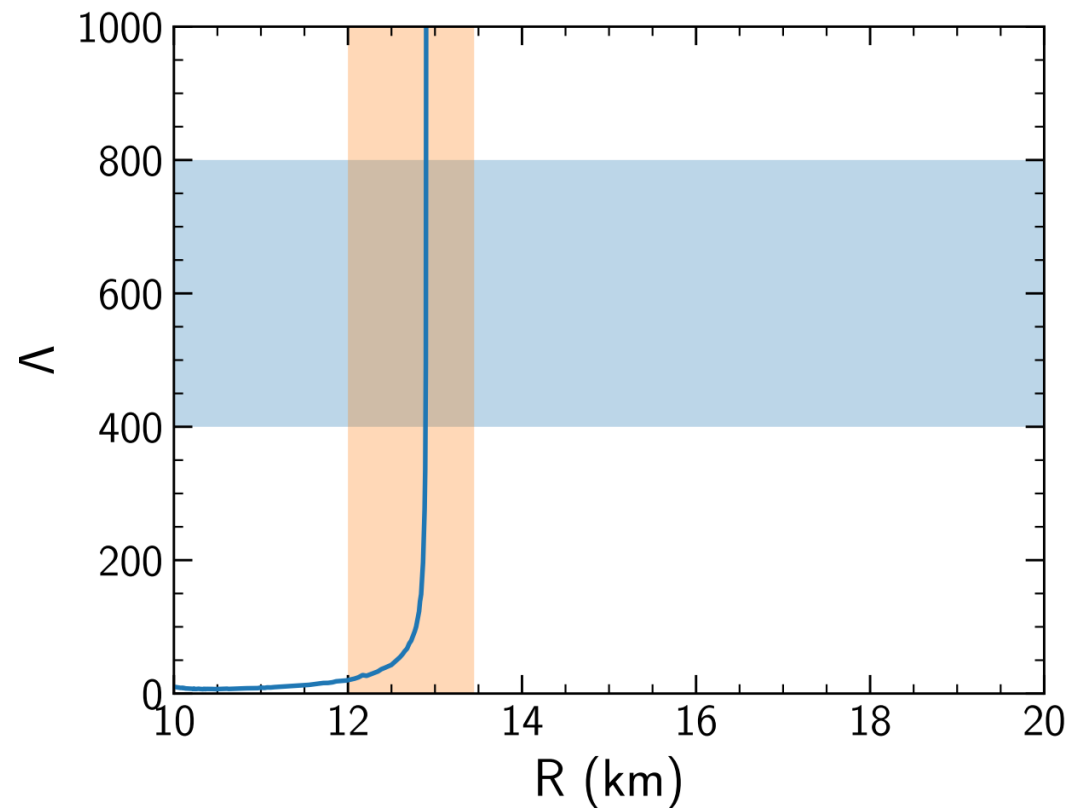


Local quark fraction (dashed — unstable stars):



A. Kurkela, P. Romatschke, A. Vuorinen, 0912.1856

Neutron star tidal deformabilities



Tidal deformability — measures stars' induced quadrupole moment Q_{ij} as a response to the external tidal field $\mathcal{E}_{ij}$:

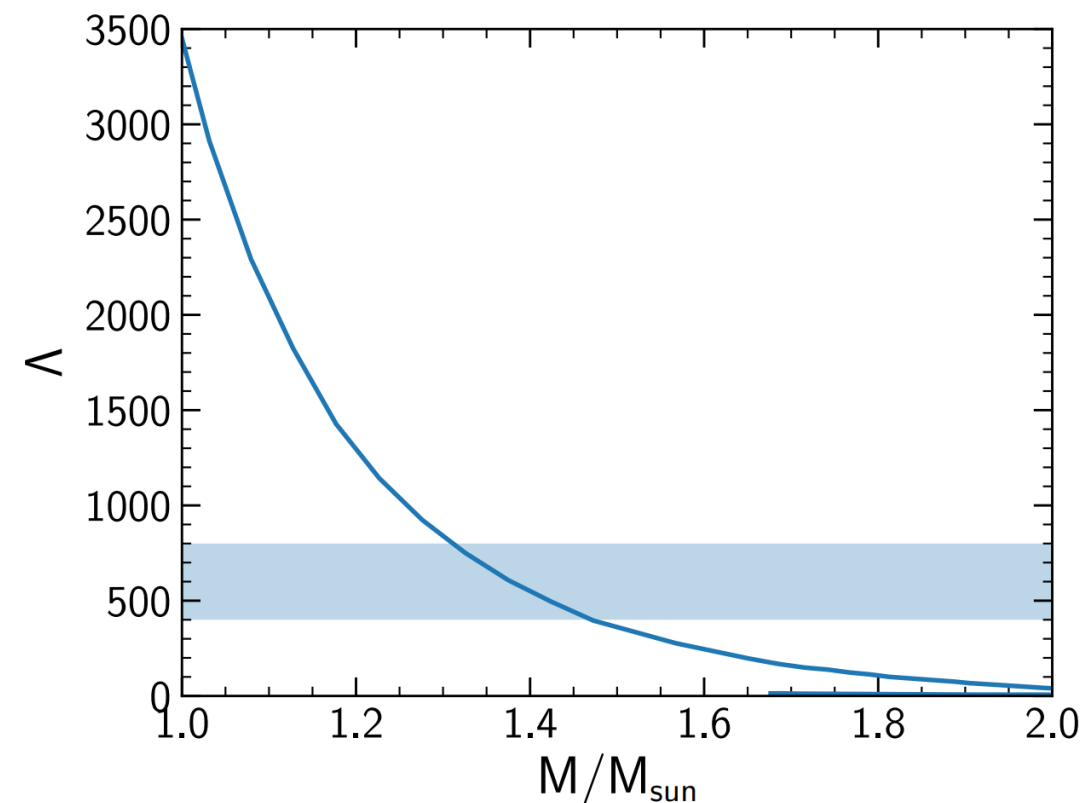
$$Q_{ij} = -\lambda \mathcal{E}_{ij}$$

important EoS-dependent quantity for inspiral phase of binary neutron star system. Related to second Love number k_2 :

$$\lambda = \frac{2}{3} k_2 R^5$$

One presents the dimensionless tidal deformability Λ (mostly dependent on compactness M/R):

$$\Lambda = \frac{\lambda}{M^5} = \frac{2}{3} k_2 \left(\frac{R}{M} \right)^5$$



Bands — recent constraints for radius and tidal deformability of $1.4M_{\text{sun}}$ star.

Most, Weih, Rezzolla, Schaffner-Bielich., 1803.00549

Line — results on Λ using EoS obtained from the model.

Gravitational Waves discovered

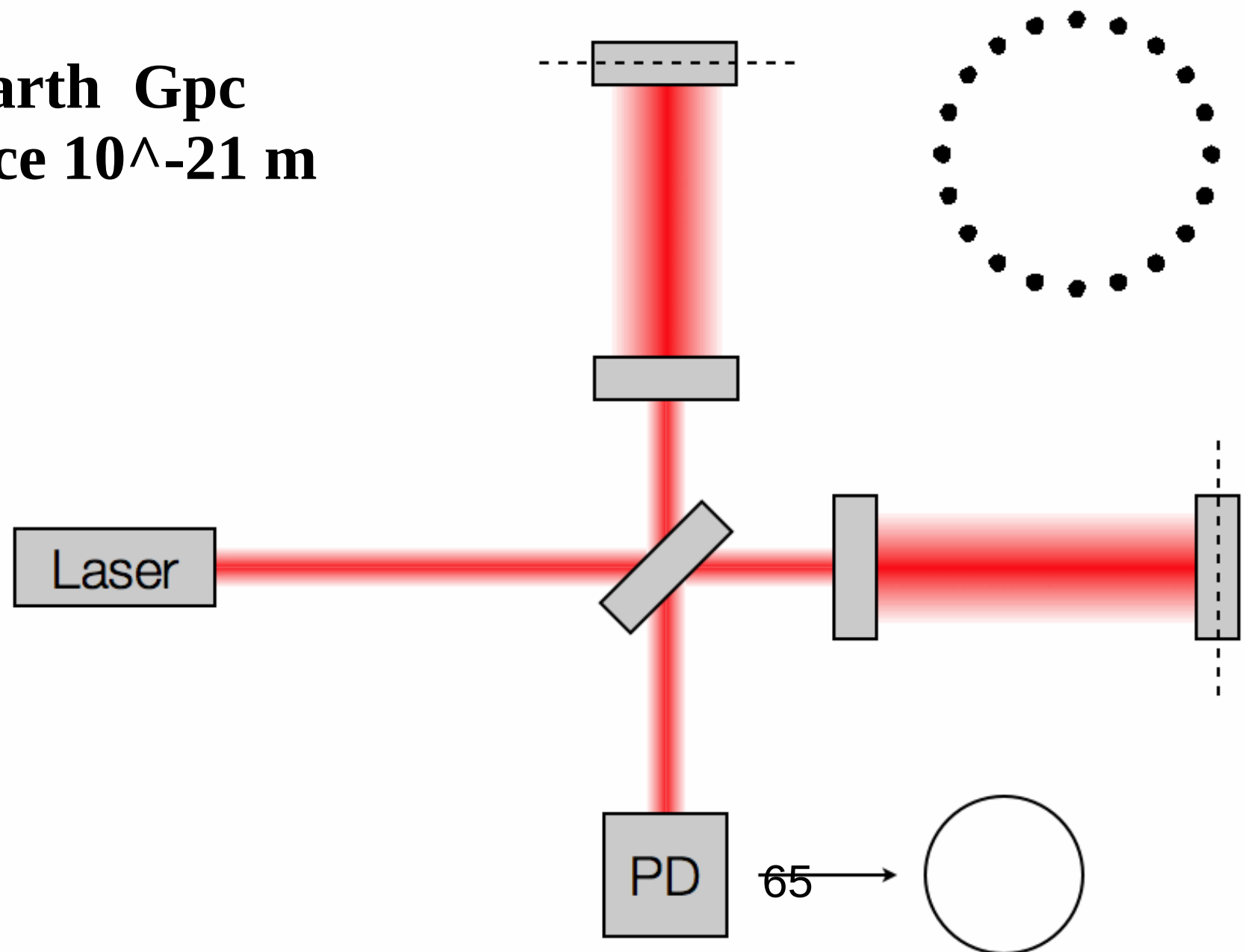
Collision of 2 Neutron Stars

GW170817

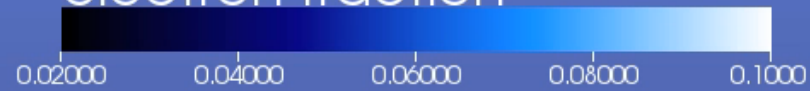
Masses of BHs: 1.4 & 1.4 Solar Masses

Distance to Earth Gpc

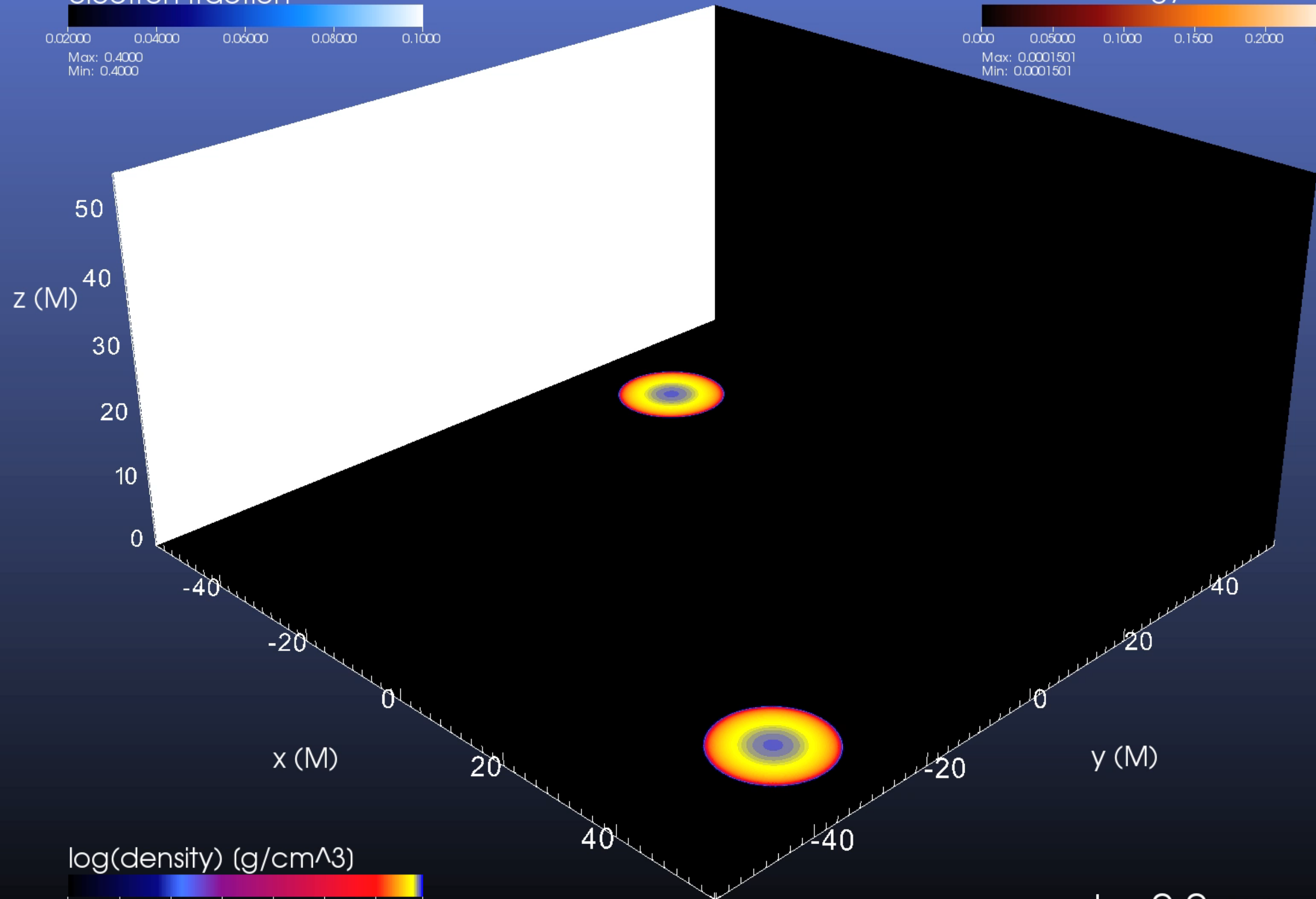
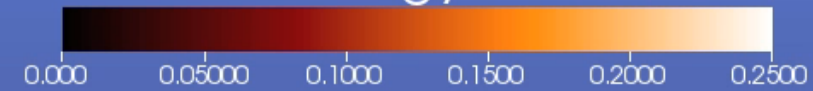
Length Difference 10^{-21} m



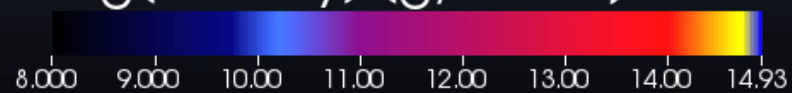
electron fraction



internal energy



log(density) (g/cm³)



$t = 0.0$ ms

The ideal fluid equations - but should include bulk- & shear viscosity & thermoconductivity - cf. A. Muronga & J. Noronha

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R = 8\pi T_{\mu\nu}, \quad (\text{field equations})$$

$$\nabla_{\mu}T^{\mu\nu} = 0, \quad (\text{cons. energy/momentum})$$

$$\nabla_{\mu}(\rho u^{\mu}) = 0, \quad (\text{cons. rest mass})$$

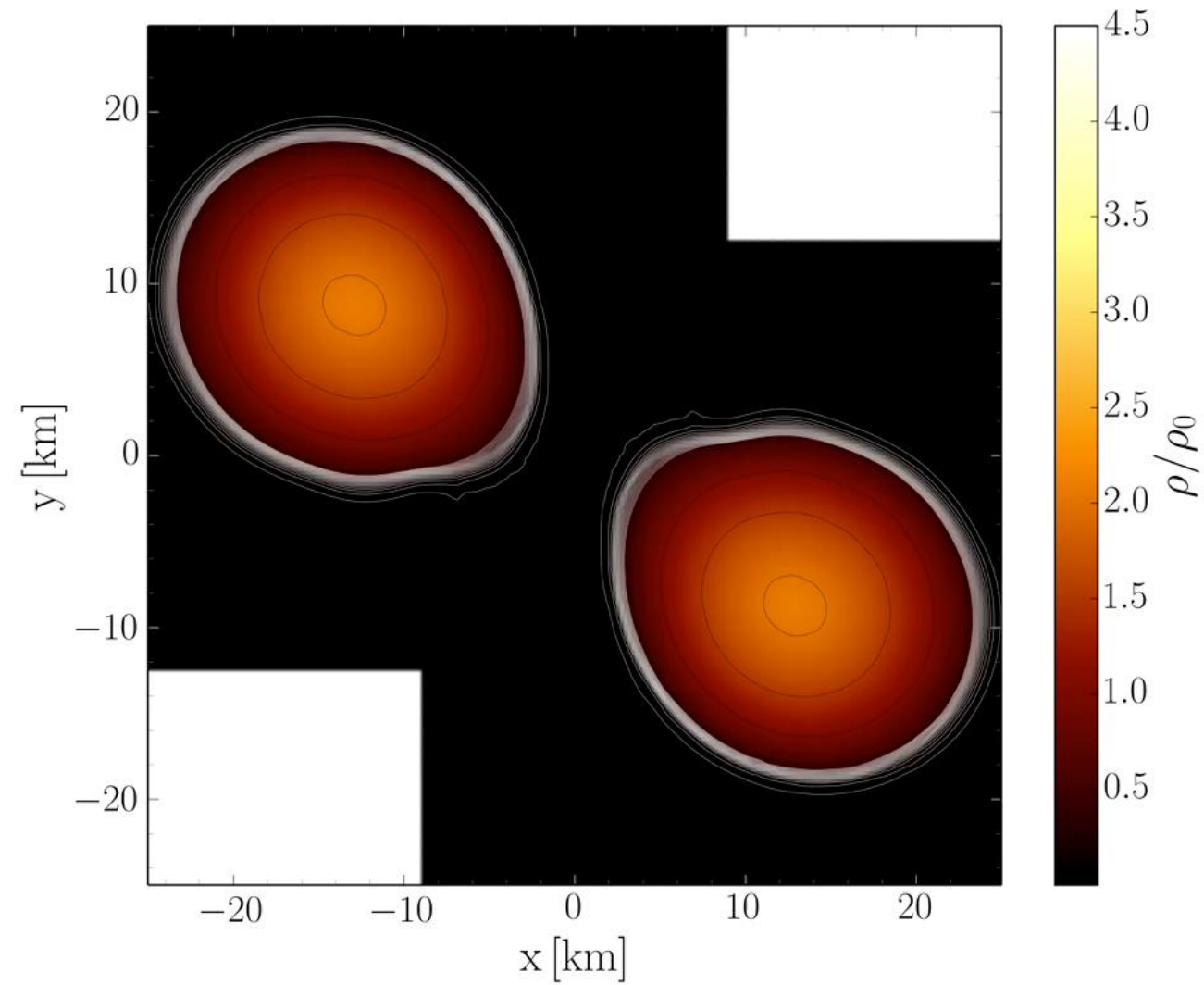
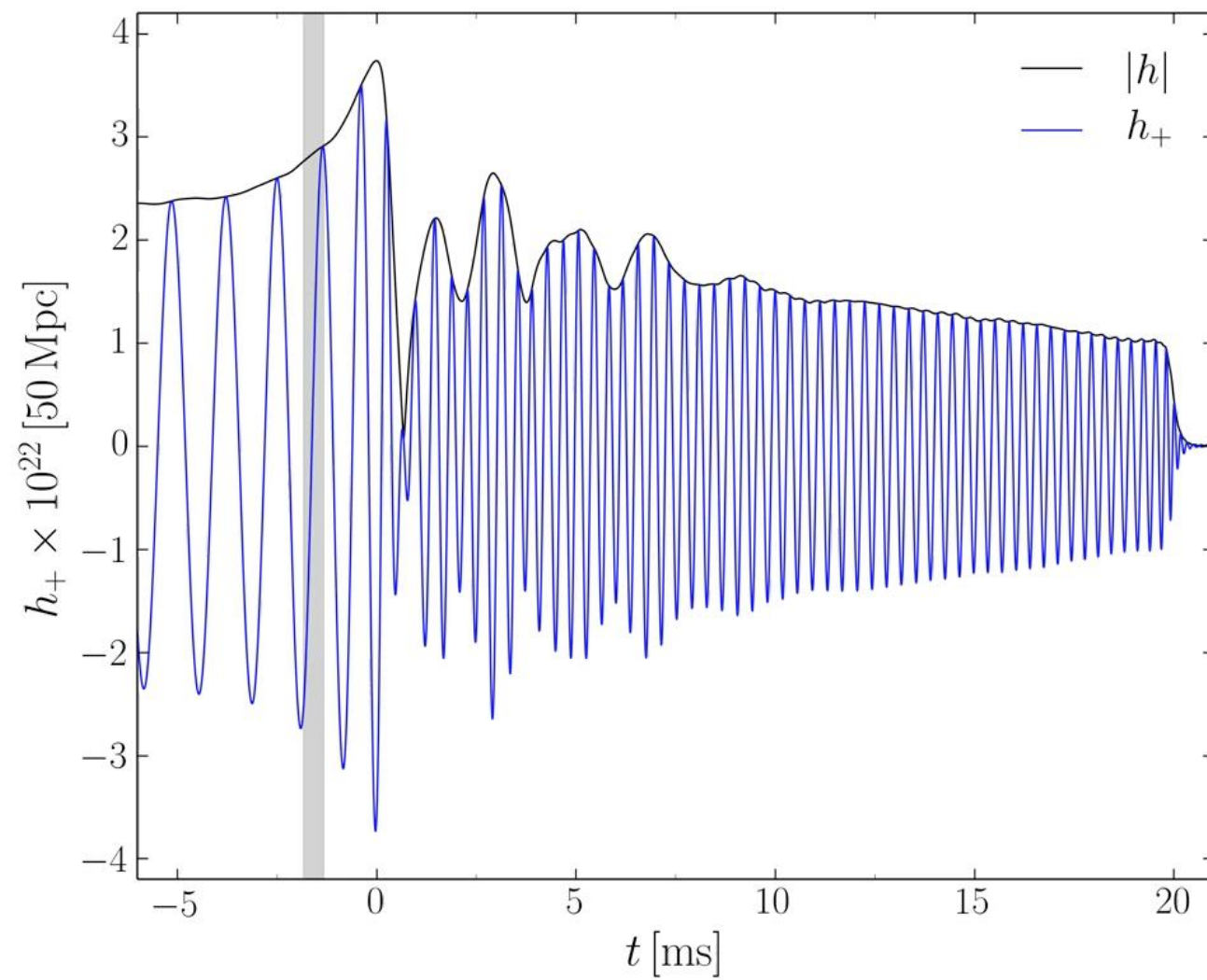
$$\nabla_{\nu}F^{\mu\nu} = I^{\mu}, \quad \nabla_{\nu}^{*}F^{\mu\nu} = 0, \quad (\text{Maxwell equations})$$

$$T_{\mu\nu} = T_{\mu\nu}^{\text{fluid}} + T_{\mu\nu}^{\text{EM}} + \dots \quad (\text{energy - momentum tensor})$$

$$p = p(\rho, \epsilon, Y_e, \dots), \quad (\text{equation of state})$$

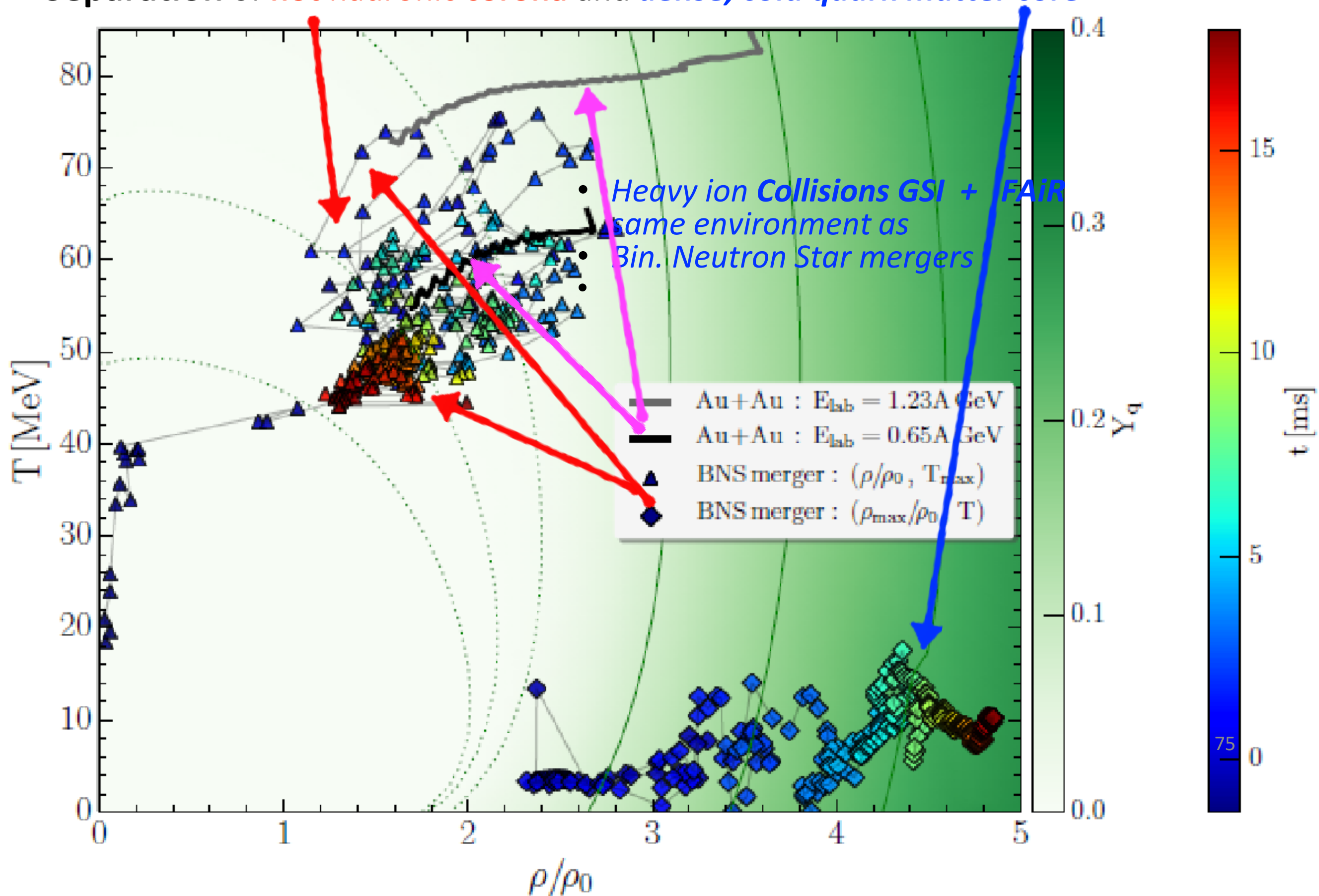
These equations do not possess analytic solutions in strong-field regimes: numerical approaches inevitable

Disco-Fox, Merengue and Tango- Phase

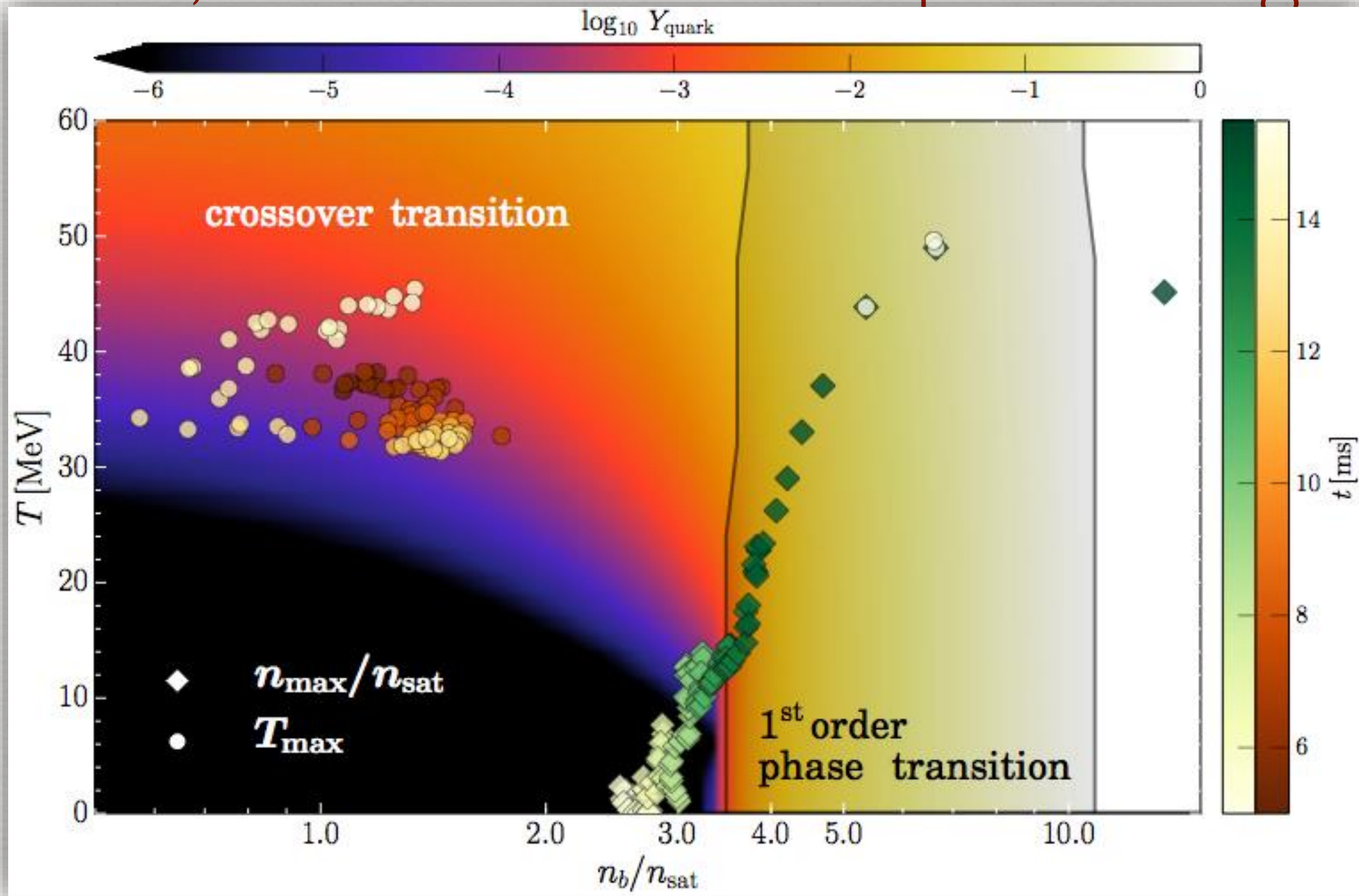


Where it's hot and dense in neutron star mergers

- Separation of **hot hadronic corona** and *dense, cold quark matter core*



T, n Evolution in the phase diagram

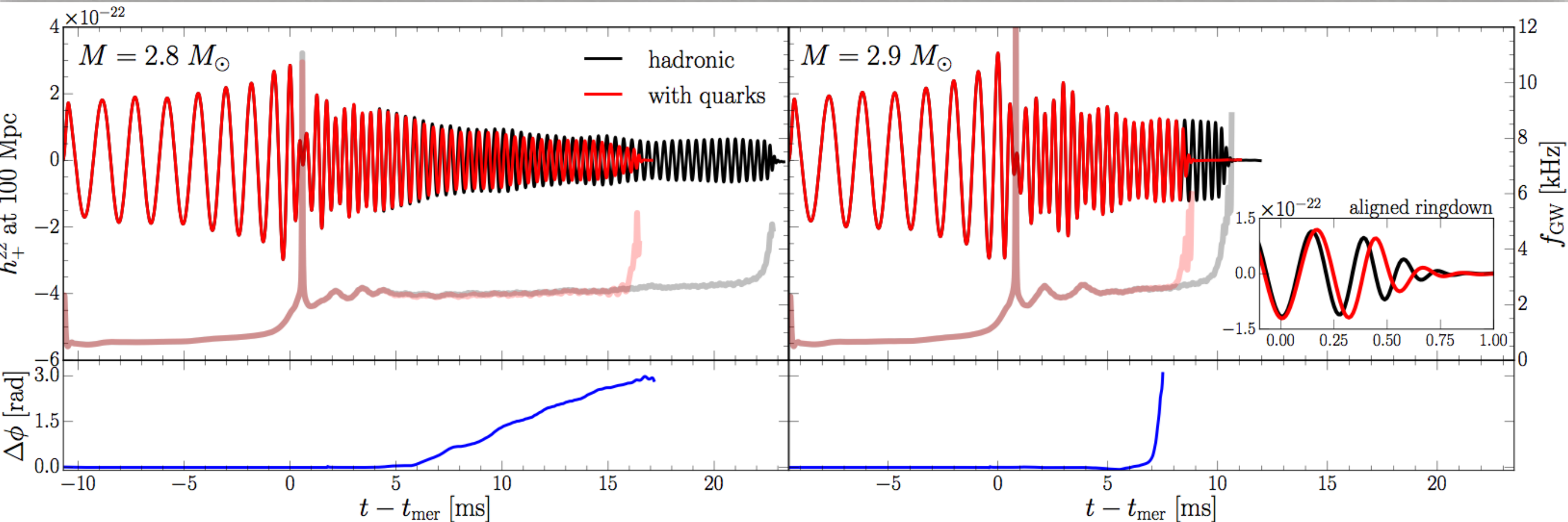


- Evolution of the max. temperature and density.
- Quarks appear early on in Torus: $T \sim 50$ MeV
- Once core reaches density $n/n_0 \sim 3.5$, transition into SQM occurs

Gravitational Wave Emission from BNSM- ML!

“low-mass” binary

“high-mass” binary



- In **low-mass binary**, after ~ 5 ms, quark fraction is large enough to change quadrupole moment and yield differences in the waveforms.

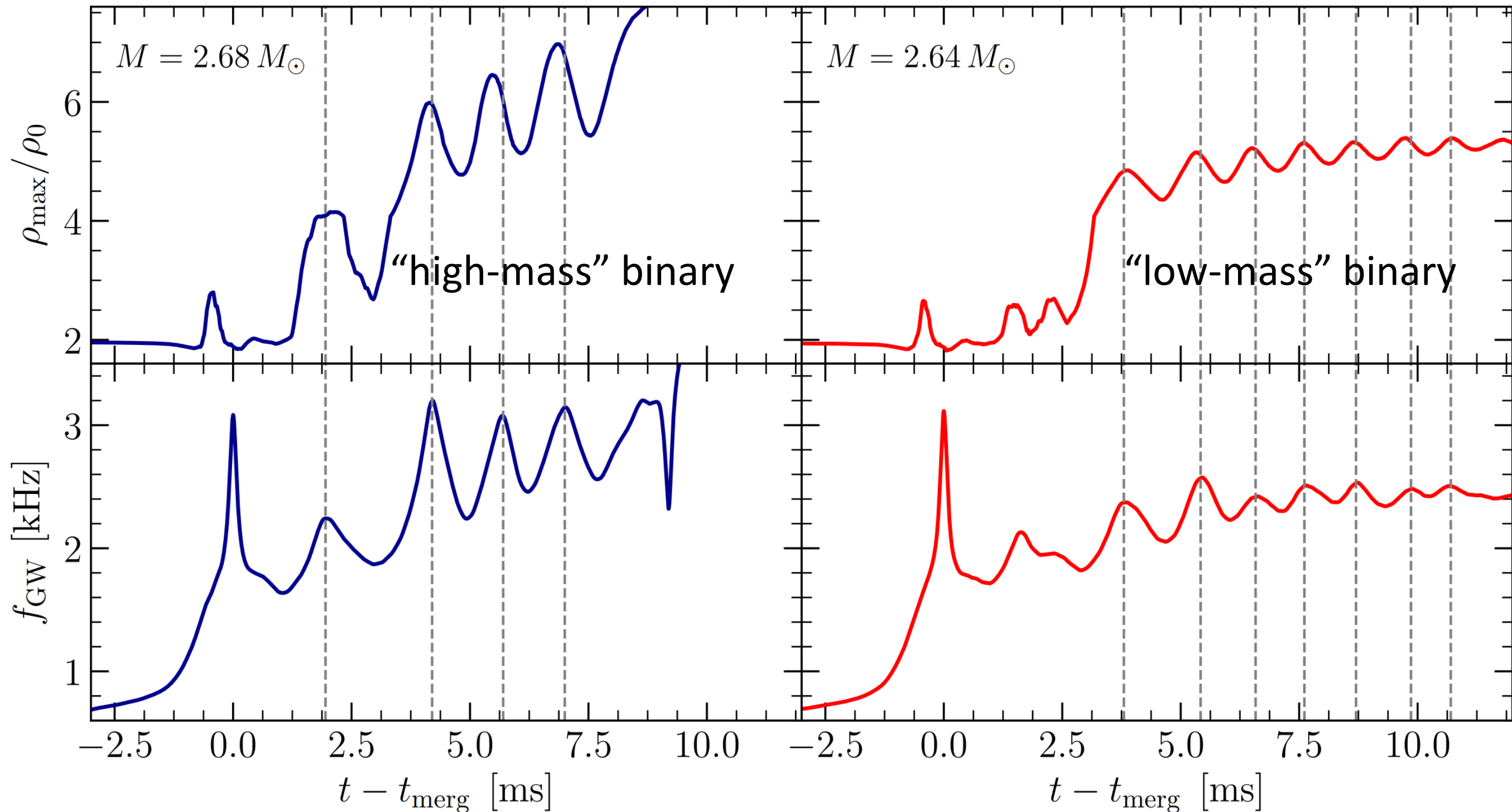
In **high-mass binary**, phase transition takes place rapidly after ~ 5 ms

• Waveforms are similar but **ringdown** is **different** (free fall for PT).

Mismatch hadronic **inspiral** and **post-merger** phase:

clear **Signature of Quark Matter - crossing or 1.OPT ?**

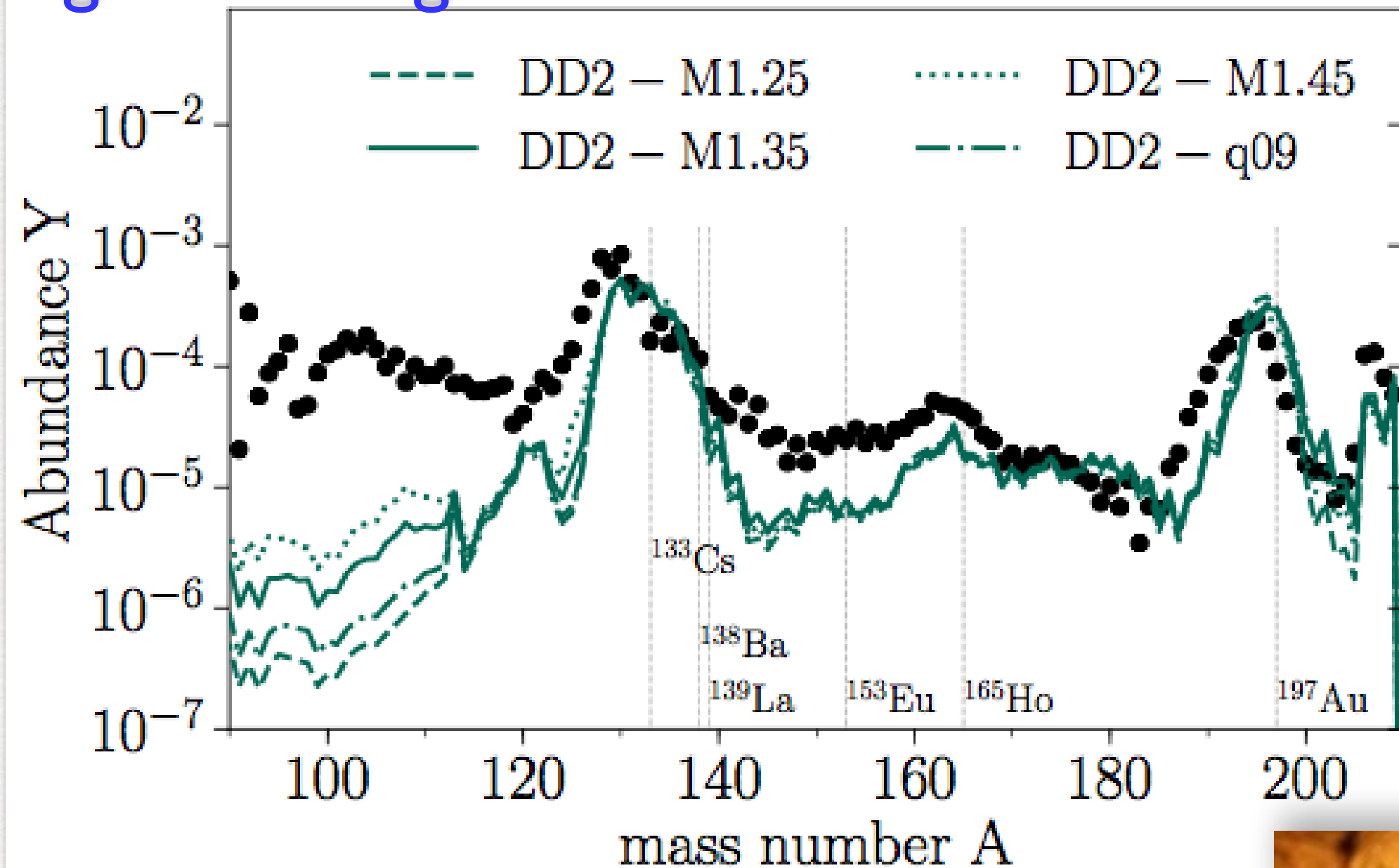
Gravitational Wave Emission from BNSM!



- Time dependence of instantaneous GW frequencies perfectly in phase with maximum density peaks

Light-Flash signals Creation of new Elements

Bovard, et al. 2017



Relative
Abundance of
cosmic elements
- Simulation vs.
Observation
- T. Kodama '77
GW170817
produces lots of
Gold, Platinum:
10x M_{earth} !

Tell Your politicians !

We found TONS of Gold!



The **CMF model** unified phenomenological approach to QCD thermodynamics, contains nuclear liquid-vapor phase transition, chiral symmetry restoration and crossover to quark matter.

- Perform phenomenological analysis of lattice QCD data
- Access high density regime of QCD thermodynamics
- Can be used as **EOS** for heavy ion collisions, neutron stars, and binary

neutron star mergers

